

INVESTIGATION OF  $\text{GH}_2\text{-GO}_2$  COMBUSTION

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Prepared For  
NASA Lewis Research Center  
Cleveland, Ohio 44135

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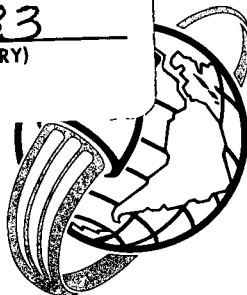
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For Period Ending 26 December 1971

INVESTIGATION OF  $\text{GH}_2\text{-GO}_2$  COMBUSTION  
NAS 3-14379

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15 January 1972

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**AEROJET LIQUID ROCKET COMPANY**

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## I. INTRODUCTION

The objective of this program is the development of an injector/combustion technology base for gaseous hydrogen-gaseous oxygen rocket engines. The end product of the program will be a design guide which includes a characterization of the injection process while relating high combustion performance and injector/chamber interactions to the design variables. Mr. L. Gordon is the NASA Lewis Research Center program manager.

In order to accomplish this objective, a six-task program is planned. Briefly, this program is structured to investigate the gas-gas mixing process from both an analytical and empirical viewpoint. Task I evaluates potential injector design concepts, culminating in selection of four element concepts worthy of further empirical investigation. Task II encompasses the fabrication, cold and combustion flow testing, and resulting data analysis of three of the four elements selected in Task I. The three element concepts cold flowed in Task II will be hot-fire tested in Task III with the intent of relating the cold flow data of Task II to the resulting single element performance and compatibility data generated in Task III. Three full-scale injectors will be designed, fabricated, and tested in Task IV. The designs will be based on the analytical and empirical information gathered in the preceding tasks. Data from Task II, Task III, and Task IV will be analyzed and correlated with the results of Task I during Task V. These correlations will form the substance of the design guide. Task VI includes the reporting requirements of the entire program.

During this reporting period, the Task II hardware was fabricated; the single-element cold flow data were generated; and the single-element hot flow data were generated. All of the above data were reduced and a large portion of the data was analyzed. The hot fire stand of Task III was fabricated and is awaiting delivery of hardware. The single-element chambers were designed as part of this task. Testing of this hardware is scheduled to begin in mid-January.

## I, Introduction (cont.)

A large portion of this quarter's effort was directed at obtaining and analyzing data from prototype  $\text{GO}_2\text{-GH}_2$  injection elements. The bulk of this testing was conducted with nonreacting propellants,  $\text{N}_2$  to simulate the  $\text{O}_2$  and  $\text{H}_2$ . A limited number of tests were conducted in a combusting environment, with the purpose of this testing being to evaluate the effects of combustion on cold flow mixture ratio and mass profiles. The cold flow testing was completed in 223 tests.  $E_m$  and  $E_c$  data have been generated for these data. Analytical model correlations of these data are well under way and will be completed in the next reporting period. The hot flow testing was completed in 36 tests; those data have been reduced and are documented in this report.

From these data, a number of significant conclusions can be drawn. These are listed as follows:

- Swirl and premix concepts are high mixing elements, insensitive to operating conditions.
- Triplet element potentially high performing, but very sensitive to design and operating variables.
- Parallel sheet element promising for HIPERTHIN application, better than doublet.
- Increased-shear elements increase mixing but not enough to warrant additional fabrication complexity.
- Coaxial element is poor mixing concept, sensitive to operating conditions.
- Combustion does impede the mixing process.

## II. TECHNICAL PROGRESS SUMMARY

### A. TASK I - INJECTOR DESIGN AND ANALYSIS

This task is complete.

### B. TASK II - COLD FLOW MODEL FABRICATION

Fabrication of the various elements was completed. These elements are illustrated in Figure 1.

A hot flow probe was constructed and the existing chamber was modified to accommodate the hot probe at three axial stations. The probe is constructed of three concentric tubes. The combustion sample is drawn through the center tube and is routed to the mass spectrometer via heated tubing. The outer two tubes form the passage for entry and return of the probe coolant fluid. In this case,  $H_2$  at approximately 250°F is used as coolant. The high temperature is required to ensure that the  $H_2O$  present in the combustion sample will be maintained in the vapor phase. This temperature is maintained throughout the system. All lines and valves associated with the mass spectrometer are steam jacketed or electrically heated. The hot flow chamber is also cooled with a high pressure steam jacket.

The cold flow chamber has been modified for the hot flow testing. Sampling bosses have been added at axial locations of 3.09, 5.15, and 7.17 in. (7.84, 13.08, and 18.2 cm) from the injector face. These locations correspond to probe locations of 11.8, 19.7, and 27.5 ox tube diameters away from the injector face.

The multiple elements have not been fabricated and will be committed to fabrication after initial analysis of the single-element cold flow data.



## II, Technical Progress Summary (cont.)

### C. TASK IIB - COLD FLOW MODEL TESTING AND ANALYSIS

#### 1. Summary

During this period a significant portion of this task was completed. The single-element testing was concluded; data reduction and analysis programs were reduced to practice; and the analysis effort was initiated and is nearing completion.

In addition, the hot flow testing of this program was completed. The intent of this testing was to ascertain if combustion could influence the cold flow mixing work. The results of this testing do indeed indicate adverse influence on mixing profiles. In general, combustion inhibits mixing so that increased chamber length is required to complete the mixing process.

The cold flow data have been dumped onto master tape files. The basic engineering unit reduction has been completed for these tests and all tests have been reduced to the form of mass and mixture ratio profiles, complete with  $E_m$ ,  $E_c$ , and other pertinent derived parameters (e.g., velocity ratio, momentum ratio, and Rupe number). Mixture ratio profiles have been developed that relate the combustion case to the identical cold flow analog.

The engineering unit file program is discussed. This program reduces the raw data to meaningful engineering parameters-such as weight flows, pressures mole fractions, temperatures and pressures-and formats the resulting data in an orderly array arranged sequentially by time and probe position. These data are then input into the Data Analysis Computer Program (DATNAL) where the key test analysis parameters are computed. Discussed in the bulk of this section are the techniques by which this program yields the parametric test data: the local mass and mixture ratio matrices, the compatibility coefficient ( $E_c$ ), and the mixing coefficient ( $E_m$ ).

## II, C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

Also included in this section is a discussion of the technique by which these parameters are evaluated. Although base bleed flow was utilized to suppress recirculation, a certain amount of recirculation could not be avoided. This is manifested in an overintegration of mass. That is, the program integrates more mass than is actually present. With base bleed, this excess mass was typically about 50% of the incoming mass flow. This was handled by only integrating radially to the point where the measured mass flux equaled the integrated flux. As an additional check, the data are tested for O/F consistency. This was established by inspection of the integrated O/F with the test O/F. Closure within 20% was defined as being valid data.

Results of the initial data analysis are presented. The results are in qualitative agreement with other cold flow testing conducted in support of the APS program. The swirl coaxial is a high mixing potential element. The increased shear element is better (higher  $E_m$ ) than the coaxial but not as efficient as the swirler. The coaxial and increased shear element are sensitive to design and operating point while the swirler is not (or at least is only slightly sensitive). The external impinging triplet has potential but is extremely sensitive to both a good mixing operating point and geometry variables. The premix designs (both the triplet and pentad) are high mixing potential elements and are influenced only slightly by design and operating variables.

Also included in this quarterly report is the modeling of the cold flow data to reduce the data to a set of equations that relate the variables to each other and mixing efficiency. Modeling has been completed for the coaxial, like doublet, and parallel sheet elements and the applicable test data has been correlated. The model is based on boundary layer approximations and has the ability to predict the effects of length, element area ratio, mixture ratio, size, propellant temperature, and impingement angle.

## II, C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

The hot flow testing was completed during the period. This testing was conducted at one atmosphere, with the identical swirl coaxial element tested in the cold flow portion of the program. The intent of this testing was to ascertain if combustion influenced the data obtained in cold flow. The results indicate that, in fact, combustion does impede the mixing process.

### 2. Data Acquisition and Reduction

#### a. The Engineering Unit File Computer Program

The initial step in reduction of a typical cold flow test was creation of a tape Engineering Unit File (E.U.F.) and paper listing.

Figure 2 shows the digital data listing for Test 122 (Run 129) of the cold test program. The E.U.F. program operates with tape input from the master raw data storage system. Card input to the E.U.F. program has been limited to the flow coefficients for the oxidizer, fuel, and helium upstream critical orifices.

The E.U.F. program lists rake pressure and composition data on the first page of the printout. The position number in column two indicates the rake position being sampled. The composition and pressure lists indicate whether the rake data at the time indicated are in the pressure or composition mode, "yes" being an affirmative answer to either. The uncorrected rake delta pressure is shown in column three. The raw signal is recorded over the linear range of the  $\Delta P$  transducer and transmitted with the units psia/volt. Stepper position 21 records the transducer tare (i.e., zero shift). To obtain the summary delta pressure readings (shown on page 5 of Figure 2), the  $\Delta P$  tare of position 21 is subtracted from the pressure reading of each rake position. These pressures are utilized in the data analysis program to calculate local mass fluxes. When the composition sampling process is taking place, the mole fraction data of columns 6 to 9 (page 1) become meaningful. For the particular test shown, the mass spectrometer

II, C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

monitored  $H_2$ , He,  $N_2$  on channels 26 to 28, respectively. Two corrections are made to specie mole fraction data before entering it in the E.U.F. summary table. The raw mass spectrometer peak voltage reading (for a particular species) is reduced according to the average voltage residual recorded during the time in which pressure data are being sampled. That is, the mass spectrometer transmits a small voltage reading (on the order of ten percent of a typical steady-state peak height sample) when it is not actually sampling gas, which is subtracted from regular composition voltage values. The second correction involves adjusting the mole fraction data to maintain consistency with a known composition calibration gas, sampled by the mass spectrometer in Stepper Switch position 22. Essentially, the calibration gas is utilized to calculate the constants  $K_1$ ,  $K_2$ , and  $K_3$  in the following equation. The equation is derived from the fact that the partial pressure of a particular species is proportional to its mole fraction in a gaseous mixture.

$$X_1 = \frac{K_1 \cdot P_{H1}}{K_1 \cdot P_{H1} + K_2 \cdot P_{H2} + K_3 \cdot P_{H3}}$$

where:  $X_1$  = mole fraction of species one  
 $P_{H1}$  = mass spectrometer peak height voltage for species one  
 $P_{H2}$  = mass spectrometer peak height voltage for species two  
 $P_{H3}$  = mass spectrometer peak height voltage for species three

When both of the aforementioned adjustments have been made, the composition data for each rake position are entered in the E.U.F. summary table.

The remaining three columns of page 1 of Figure 2 show the time-based test weight flows. They are calculated with the compressible sonic flow equation shown below, based on measured upstream orifice total pressures and temperatures.

## II, C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

$$\dot{w}_{\text{sonic}} = A C_d \cdot P_o \sqrt{\frac{\gamma \cdot g}{R \cdot T_o} \left( \frac{2}{\gamma+1} \right)^{\frac{\gamma+1}{\gamma-1}}}$$

On page 3, the remaining time-based system variables are listed. Manifold temperatures were calculated with standard chromel-alumel thermocouple response curves contained within the E.U.F. program. The three manifold and one chamber pressure transducers measure gauge pressures recorded in the units millivolts/psig, the E.U.F. program converting to psia. The remaining total and static pressures read the rake pressure data.

The test system variables are averaged over the entire test period and are shown at the top of the test summary page of Figure 2. The data for each rake position are listed for both the average of the number of samples taken with that probe and the last sample output taken with the probe. For the test shown, only one scan was taken for each probe position. Since steady-state pressure and composition data are obtained with the first sample, subsequent scans are not required. The data summary as shown is stored on tape and readily available for direct input to the data analysis program, DATNAL.

### b. The Data Analysis Computer Program (DATNAL)

Following tape storage of the engineering unit file summary block, the data analysis program computes the key test analysis parameters. Figure 3 is a seven-page detail of the DATNAL output for Test 122 (Run 129). DATNAL reads the engineering file for the particular test from tape. Input is completed by card read-in of the particular element geometric variables (flow area and injection angle).

II, C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

Parametric test data comprise the first output block of DATNAL as shown on page 1 of Figure 3. The following block details the calculated injection variables, to be used for correlative type analysis. The 24 variables listed are calculated in a separate program subroutine, based on element flow areas, manifold temperatures and pressures, chamber pressure, and measured mass flow rates. The continuity equation is the basis of calculation for parameters, including injection velocity terms.

Page 2 of the DATNAL listing shows the measured  $\Delta P$  and static pressure matrices. The data for the outside four radial positions was flopped from quadrant one (bounded by the 0- and 90-degree radial positions) to fill the nonmeasured quadrants. Figure 18 of Reference 1 shows the rake element locations. Probe 1 lies on the zero-degree boundary, while probe 8 lies on the ninety-degree boundary. The measured total pressure matrix is calculated by adding corresponding terms of the delta pressure and static pressure matrices.

Pages 4, 5 and 6 of Figure 3 detail the local mass flux and mixture ratio calculations performed in DATNAL. The local mixture ratio matrix is calculated with the equation shown below, from the mole fraction data obtained from the E.U.F. program.

$$(O/F)_L = \frac{(MF_{N2})_L \times MW_{N2}}{(MF_{H2})_L \times MW_{H2}}$$

where:  $MF_{N2}$  = local nitrogen mole fraction  
 $MF_{H2}$  = local hydrogen mole fraction  
 $MW_{N2}$  = molecular weight of nitrogen  
 $MW_{H2}$  = molecular weight of hydrogen

The subsonic compressible flow equation is used to calculate the local total mass flux.

Ref. 1 - Calhoon, D. F., Investigation of  $CH_4$ - $CO_2$  Combustion Quarterly Rpt. No. 1, 11 October 1971

II, C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

$$\dot{w} = A \cdot C_d \cdot P_o \sqrt{\frac{2g}{(\gamma-1) RT_o} \left[ \left( \frac{P_s}{P_o} \right)^{\frac{2}{\gamma}} - \left( \frac{P_s}{P_o} \right)^{\frac{\gamma+1}{\gamma}} \right]}$$

The gaseous mixture properties (ratio of specific heats, molecular weight) used to solve the equation are calculated based on the mole fraction data input from the E.U.F. program. In essence, local properties are obtained for the flowing mixture based on mass or mole weighting local nitrogen, hydrogen, and helium properties. The local oxidizer flux and fuel matrices of page 3 were obtained by multiplying the respective local mass flows by the associated nitrogen and hydrogen mass fraction, respectively. Through the first five pages of output, DATNAL has essentially summarized the chamber flow field on a local basis.

On page 6 of the DATNAL output, the local compatibility coefficient ( $E_c$ ) is displayed for the chamber flow field.  $E_c$  is calculated from the following equation, the development of which is detailed in Reference 1.

$$E_c = \frac{DB_{\ell} \left( \frac{\dot{w}}{A} \right)_{\ell}^{0.8} \left( \frac{1}{1 + T_{wg}/T_o} \right)_{\ell}^{0.8} (T_o - T_{wg})_{\ell}}{DB_n \left( \frac{\dot{w}}{A} \right)_n^{0.8} \left( \frac{1}{1 + T_{wg}/T_o} \right)_n^{0.8} (T_o - T_{wg})_n}$$

$E_c$  is currently being calculated on a local basis only for all cold flow tests. Further treatment of  $E_c$  will be made during the next reporting period. The differences in local mass distribution inherent between cold flow tests and hot firings make the  $\frac{\dot{w}}{A}$  term in the  $E_c$  calculation worthy of investigation. For this reason, calculation of  $E_c$  may change after correlations are performed between cold and hot tests. Also for the above reason, a single integrated  $E_c$  value has not been calculated for cold flow tests to date.

## II, C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

After the local mass flux and mixture ratio matrices have been established, DATNAL characterizes the total chamber flow field. The total, fuel, and oxidizer local mass flux matrices are integrated over the entire chamber. Page 7 displays the integrated flow rates, values being computed from chamber centerline through six radial positions (five rake element locations and the wall). The integrated mixture ratio through any radial location is calculated by dividing the integrated oxidizer flow rate by the integrated fuel flow rate. Typically, integrated flow rates do not equal measured flow rates when the entire chamber flow field is examined. Most tests are characterized by higher than measured integrated flow rates; the reason is suspected to be chamber recirculation zones. To characterize all cold flow tests on a common basis, key analysis parameters are typically compared at the radial location,  $\bar{R}$ .  $\bar{R}$  is the radial location at which the integrated mass flow rate (oxidizer and fuel) equals the measured flow rate. If the flow field integrates low,  $\bar{R}$  is equated to the chamber wall radius (0.75 in.).

The analysis parameters  $E_m$ ,  $N_m$  and percent  $c^*$  are also shown on page 7.  $E_m$  is the mixing coefficient, defined by the equation below with the nomenclature defined in Reference R.

$$E_m = 100 \left[ 1 - \sum_o^n \frac{A_i M_{ti}}{\dot{w}_o} \left( \frac{\dot{w}_o}{\dot{w}_t} - \frac{M_{oi}}{M_{ti}} \right) - \sum_n^{\bar{n}} \frac{A_i M_{ti}}{\dot{w}_f} \left( \frac{\dot{w}_o}{\dot{w}_t} - \frac{M_{oi}}{M_{ti}} \right) \right]$$

$E_m$  is the central parameter in cold flow element modeling. It is calculated for the six flow regions formed by considering each rake probe radial location to be the outside flow streamline.  $E_m$  is also calculated at  $\bar{R}$  by interpolating between the  $E_m$  values at the bounding radial positions. The  $\bar{R} E_m$  is the value which is usually utilized in intra- and inter-element correlative analysis. The  $E_m$  function and its role in analysis of the cold flow tests is more thoroughly discussed in Section II,C,3, Data Analysis and Correlation.



II, C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

$N_m$  (ETAM on page 7) is a mass-weighted mixture ratio distribution term defined by the following equation:

$$N_m = 100 \left[ \sum_o^n \left( \frac{\dot{w}_i}{\dot{w}_t} \right) \times \frac{(O/F)_i}{(O/F)_o} + \sum_n^{\bar{n}} \left( \frac{\dot{w}_i}{\dot{w}_t} \right) \left( \frac{(O/F)_o}{(O/F)_i} \right) \right]$$

where:

- $\dot{w}_i$  = local total mass flux (oxidizer + fuel)
- $\dot{w}_t$  = measured total mass flux, lb/sec-in.<sup>2</sup>
- $(O/F)_i$  = local mixture ratio
- $(O/F)_o$  = measured mixture ratio
- $n$  = number of samples in which  $(O/F)_i < (O/F)_o$
- $\bar{n}$  = number of samples in which  $(O/F)_i > (O/F)_o$

Effectively,  $N_m$  indicates the mass-weighted deviation from nominal mixture ratio.  $N_m$  is calculated through the same flow field boundaries as  $E_m$ . Its value at  $\bar{R}$  is also characterized in the last data block on page 7 of DATNAL. Percent nominal  $c^*$  is the final analysis parameter calculated in DATNAL. Based on a 300 psia  $GO_2$ - $GH_2$  propellant combination and the test local mixture ratio matrix, a local characteristic exhaust velocity matrix is established by interpolating with a mixture ratio versus  $c^*$  data block located in DATNAL. The local  $c^*$  distribution is mass-weighted, integrated, and divided by the total integrated mass flow rate to produce a  $c^*$  value characteristic of a particular test. Percent nominal  $c^*$  is found by dividing test  $c^*$  by nominal  $c^*$  at the flow field integrated mixture ratio. Percent  $c^*$  is calculated for the same regions and at  $\bar{R}$  in similar manner to  $E_m$  and  $N_m$ .

## II, C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

### 3. Data Analysis and Correlation

As described in the preceding paragraphs, the test data points have been reduced through DATNAL using automated data reduction techniques. These tests are summarized on Figure 4. Figure 4 tabulates a brief description of the injection element design parameters, some basic operating parameters, injection parameters, and calculated mixing efficiency parameters. Other additional correlating parameters are calculated and tabulated on individual DATNAL output sheets for each test (see Figure 3, page 1 of 7) for more detailed analysis and correlation but were omitted from Figure 4 for brevity and conciseness. Figure 4 is an informal work sheet and should be considered preliminary data.

#### a. Theoretical Background

Figure 5 is a pictorial representation of the cold flow field downstream of a typical shear coaxial element within the mixing (combustion) chamber. A high velocity axial jet exists at the chamber axis at the injector face plane. A null injection zone occurs immediately outboard of the active element to the chamber half-radius. A porous (Rigimesh) injector face plate bleeds helium from the half-radius to the chamber wall, resulting in a helium gas velocity on the order of 4.6 meters/sec (15 fps). Due to momentum transfer between the injected gas jet and relatively quiescent gases in the chamber, the jet velocity decelerates and the jet boundary spreads. Although the helium bleed is intended to suppress flow recirculation, the cold flow data indicate it is not entirely successful in doing so. The element jet entrains a portion of the chamber gases and accelerates it downstream. This results in an aspiration effect, resulting in a low static pressure zone around the element which creates a flow recirculating annulus between the element and helium bleed flow. The helium-rich flow is forced against the chamber wall and it also has its own recirculation zone.

## II, C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

The ideal situation would be to start integrating the oxidizer and fuel mass fluxes at the chamber axis and proceed radially outward until the integrated total mass flow rate (oxidizer plus fuel) identically equals the sum of the measured oxidizer and fuel flow rates and to also have the integrated O/F be identically equal to the measured (input) mixture ratio. The radial position at which the integrated flow rate equals the measured flow rate is defined as  $\bar{R}$  and the mixing efficiency calculated from all the mass contained within  $\bar{R}$  is the primary choice for the data correlation.

However, since the fuel element is outboard of the oxidizer in the coaxial, flat "I", pentad, and external impinging F-O-F triplets, the fuel diffuses radially outward faster than the oxidizer, resulting in an integrated O/F which is usually on the order of 15% higher than measured O/F. Since  $E_m$  is normalized on the basis of integrated O/F, it may sometimes be desirable to evaluate  $E_m$  at some radial position (usually outboard) other than  $\bar{R}$  in which the integrated O/F is closer to measured O/F. The automated data reduction program sets all negative dynamic pressures at zero and assumes stationary flow in the negative velocity recirculation zones because the sampling probe is not calibrated to accurately determine the magnitude of negative dynamic heads. On the other hand, all positive dynamic heads are assumed to be element flow in the forward direction and its flow rate is integrated even if it is that portion of the recirculation zone flowing in the forward direction (see Figure 5). Thus, it is not surprising that, if all flow in the positive direction is integrated from the chamber axis to the wall ( $r = 1.9$  cm), the integrated mass flow rate is on the order of 50% to 100% higher than the measured flow rate. The local mixture ratio of probe positions beyond  $\bar{R}$  and in the recirculation zone are usually fuel rich compared to the oxidizer-rich regions near the axis. The reason can be seen from Figure 5.

## II, C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

Because of the recirculatory flow field, the simplifying mathematical assumption of irrotational flow cannot be made to define the flow stream function and velocity potential. However, a qualitative schematic cartoon depicting possible "stream functions" and pseudo-equipotential "velocity potentials" is shown on Figure 5 for clarity of discussion. The maximum velocity potential occurs at the injection element plane. The potential function decreases as the jet diffuses and the streamlines diverge. The potential function decreases in a fan about the circulation point which acts like a vortex eye in the recirculation region. The minimum potential in the recirculation region occurs on a surface between the eye and the maximum potential surface at the element exit. The magnitude of the step discontinuity in the velocity potential is dependent upon the strength of the vortex circulation. The latter, in turn, is dependent on the physical spacing between the eye and jet boundary and the reduced potential recirculation gas which is accelerated by the high velocity potential jet through viscous shear forces. However, because of the rotational flow circulation induced discontinuity in the velocity potential immediately outside the element jet, a strong velocity potential gradient exists in the radial as well as axial direction. This causes the outer gas (fuel) stream function to rapidly diffuse radially outward, becoming quickly entrained in the fuel-rich recirculation zone leaving the jet core to be oxidizer-rich relative to the measured or injected O/F. The numerical values assigned to the velocity potentials shown on Figure 5 are shown to enhance conceptual understanding only and are not indicative of a quantitative analysis.

Extensive effort has been taken to understand the basic flow and mixing mechanism so that the DATNAL computer program can be modified to the extent necessary to reflect accurate and meaningful data and injection parameters prior to any attempt to correlate data. This was considered to be necessary because of the large mass of data acquired on this cold flow test program. It would be better to check the data in great detail first and acquire high confidence in the basic data rather than attempt correlations of low confidence data and encounter correlative anomalies later. With this in mind, the

## II, C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

data on Figure 4 are separated into groups of variable confidence ratings. After scanning the local mass and mixture ratio distributions at each probe position for reasonableness on each test, the integrated O/F was compared to the measured O/F at  $\bar{R}$ ; if integrated O/F is within  $\pm 20\%$  of measured O/F at  $\bar{R}$ , the  $E_m$  value at  $\bar{R}$  is given a high confidence rating indicated by an asterisk to the left of the test number in Figure 4. Of course, this assumes  $\bar{R}$  is a reasonable value consistent with similar element types, thrust per element (F/E) and axial position (L/D). Furthermore, the  $E_m$  at  $\bar{R}$  is compared vs  $E_m$  values evaluated at other nearby radial positions to check the sensitivity of  $E_m$  to assumed radial boundary.

If these conditions are not satisfied, it may be preferable to evaluate  $E_m$  at another radial boundary where the integrated O/F is closer to the measured O/F. A second condition of acceptability was selected for which integrated O/F is within  $\pm 10\%$  of measured O/F and the integrated oxidizer plus fuel flow rate is within  $\pm 25\%$  of measured flow rates. If this condition is satisfied, the data point is likewise indicated by an asterisk. On some tests, the integrated O/F is always biased higher or lower than the measured O/F at all radial positions. Nevertheless, the data are considered acceptable if the deviation from perfect mixing ( $1 - E_m$ ) varied by less than  $\pm 10\%$  at all reasonable radial boundaries; e.g., if  $E_m = 50\% \pm 5\%$ ,  $80\% \pm 2\%$ ,  $90\% \pm 1\%$ , etc., at any radius. A fourth condition of acceptability is if  $E_m$  is between 90% to 100% and does not vary by more than  $\pm 1\%$  from a nominal value over a wide range of radii, it is indicated by an asterisk.

All tests marked by an asterisk on Figure 4 are considered to be sufficiently accurate or insensitive to variation that they may be considered ready for data correlation. Some tests are characterized by widely varying values of  $E_m$  which are usually indicative of radial mixture ratio variations. Since the uncertainty associated with these tests may prejudice the data

## II,C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

correlations a tentative compromise value or a "most probable" value is indicated by an open diamond symbol ( $\diamond$ ) to the left of the test number column on Figure 4. These values when used in any potential correlation, are specially marked and viewed with suspicion until they are compared with similar elements, similar test conditions, similar L/D, etc., until the credibility of their data is established. The values in Figure 4 have been treated in this manner and represent the best possible value for that particular test.

### b. Cold Flow Data Analysis

The pertinent cold flow data of this program have been reduced by the techniques discussed earlier in this report. The resulting data are displayed in graphical form in Figures 6 through 42. The first four figures are summary graphs of ERE for all injectors as a function of thrust per element (F/E), length, element area ratio ( $A_F/A_O$ ), and mixture ratio (O/F). The remaining figures depict compatibility and mixing efficiency at a detailed level by element type.

The effect of sample position in L/D, where D is the oxidizer orifice diameter or equivalent diameter is shown in Figure 5 for the area ratio one, mixture ratio four point elements. The overall characteristics of the elements are as expected, increasing  $E_m$  with increasing length. The swirl coaxial, premix pentad, and triplet are grouped together at high mixing efficiencies. The coaxial element has the lowest  $E_m$  of any element tested on this basis. The remaining elements group between the extremes of the shear coaxial and the swirl coaxial elements. When these elements are compared on a thrust/element basis, the same effects are noted (See Figure 7); i.e., the premix designs and the swirl coaxial element are high performing elements while the shear coaxial is a low performing element. With the exception of the swirl

## II, C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

coaxial element, the data trends are in the expected direction, reduced mixing with larger elements. The swirl coaxial element maximizes at 20 lbf/element. It would appear that the fuel annulus size and radial oxidizer momentum are related. It is also interesting to note that the parallel sheet element mixes better than the like doublet elements over the thrust range tested in this program. In addition, the parallel sheet element at low (3 lbf [13 Newtons]) approaches the mixing efficiency of the best elements. For small thrust/element injectors (such as HIPERTHIN), these data indicate that the parallel sheet element is a viable element concept.

Area ratio influences for the basic element concepts are illustrated in Figure 8. Both shear mixing elements, the coaxial and increased shear element decrease in performance as area ratio is increased. It should be noted that the area ratio was varied by changing only the fuel geometry. The oxidizer diameter was held constant. The trends noted in Figure 8 are, therefore, not unexpected. Decreasing area ratio is in the direction of both smaller fuel annulus widths and higher velocity ratios--both effects which analytically are predicted to lead toward increased mixing efficiency. The swirl coaxial and premix designs are insensitive to area ratio influences, an effect that is somewhat surprising for the premix case. Cold flow testing by ALRC on an element design similar to the premix triplet design revealed that mixing efficiency was significantly impacted by orifice geometry changes. See Reference R for these data. Although the single-element injectors of both these series were similar, two important geometry differences are evident. The mixing cup length of this program was significantly longer than that of Reference 2. For this program, cup depths ranged from 1.15 to 4.75 L/D, where L is the cup depth and D is the oxidizer hole diameter. For the program of Reference 2, the ratio, on the same basis, was 0.1. The increased mixing cup depth forces mixing and therefore attenuates the effects of area ratio and mixture ratio variations. Also geometry was varied for rectangular fuel orifice shapes only; no I fuel channels were investigated on this program. Referring again to Figure 8, note that external impinging triplet data are very sensitive to area ratio influences,

Ref. 2 - Kors, D. L., Calhoon, D. F., Gaseous Oxygen/Gaseous Hydrogen Injector Element Modeling, AIAA Paper No. 71-674, June 14-18, 1971

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optimizing at an  $A_f/A_o$  of 1.25. This element type, in general, is sensitive to most geometry and hydraulic variations.

The effect of mixture ratio on  $E_m$  is illustrated in Figure 9. Again, the swirl coaxial and premix designs are reasonably insensitive to this influence, while the shear coaxial element decreases in efficiency as a function of increasing mixture ratio. The remaining element types exhibit only a small parametric change.

Detailed parametric curves of the coaxial family of elements are illustrated in Figures 10 through 19. Included in this family are the shear, increased shear, and swirl coaxial elements. Figure 10 compares these elements on a length basis ( $L/D$ ), where  $D$  is the oxidizer tube diameter. The effect of increased shear area and swirl is evident. These elements are compared on a mixture ratio basis in Figure 11, the swirl coaxial showing no influence and the shear and increased shear coaxial decreasing in efficiency with increasing mixture ratio. This effect is due to an increased  $V$  influence. The effects of area ratio (or fuel slot width) for these elements are illustrated in Figures 12, 13 and 14. In general, decreasing area ratio is in the direction of increased  $E_m$  for the three coaxial type elements. The swirl coaxial data in Figure 14 indicate an optimum in thrust size at 15 lbf/element (67 Newtons /element). This indicates that the radial component of momentum and the physical size are related or that there is a fuel momentum to oxidizer radial momentum ratio which produces optimum mixing. These effects are being investigated and will be reported in the next report period. The effect of swirl magnitude for various area ratio elements is illustrated in Figure 15. These data indicate that rather large changes in potential performance can be obtained with a rather moderate amount of oxidizer radial momentum.



## II,C, Task IIB- Cold Flow Model Testing and Analysis (cont.)

The effect of lower propellant temperature on  $E_m$  is shown in Figure 16. With the exception of the swirler data,  $E_m$  increases with decreasing temperature. This trend is contrary to hot-fire data generated with ACPS size hardware, 1500 lbf on Contract NAS 3-14352. These data resulted in a significant reduction in performance when tested with cold propellants. The resulting conclusion is that the temperature influence noted in hot testing results from the combustion influence on the mixing/reaction processes.

The compatibility characteristics of the three elements are indicated in Figures 17 through 19. Here, the compatibility is defined as being proportional to the local mixture ratio measured at the edge of the flow field,  $(O/F)_L$  nominalized by the overall integrated  $O/F$   $(O/F)_i$ . The open symbols are the worst (most oxidizer-rich)  $O/F$  measured at the flow field boundary, the closed the best (most fuel-rich), and the half-open the average value. The resulting data band accounts for circumferential variation in the element flow field. Inspection of Figure 17, where the coaxial and swirl coaxial elements are compared on the above basis, reveals that in the near zone (close to the injector face) the coaxial element is benign as compared to the swirler. This effect was noted in combustion testing of full-scale hardware in Contract NAS 3-14354. In this testing with comparable chambers, the near zone heat flux using a swirler element was higher than the equivalent coaxial element. As a function of  $A_f/A_o$ , the coaxial element becomes more benign with increasing area ratio (see Figure 19). This fuel rich boundary is reflected in the low  $E_m$  data for this element, which was previously discussed. In general, those elements that exhibit high potential compatibility suffer from a low mixing rate.

An equivalent data set for the premix designs is illustrated in Figures 20 through 27. With the exception of length, these elements are relatively insensitive to design and operating variables. As discussed earlier, the fact that they are insensitive is somewhat surprising and can be attributed to mixing cup depths that attenuated the expected differences. The compatibility variations are not negligible as shown in Figures 25, 26 and 27.

## II, C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

Large differences in maximum and minimum local O/F indicate a streak potential. Note, for the premix triplet in Figure 26, that increasing the element width ratio tend to stratify the flow field. This can be explained by considering the geometry of the injector pattern. At a narrow fuel slot width, the available fuel momentum is concentrated on the center of the oxidizer stream, penetrating the bulk of the oxidizer and resulting in a homogenous flow field. As this penetration is reduced, the fuel, rather than penetrating the oxidizer stream, displaces it radially. The net effect is to form an edge condition that is alternately fuel and oxidizer rich at 90-degree intervals. The pentad element does not appear to be as sensitive because the available momentum of any one fuel stream is only half of the equivalent triplet. In no case does the pentad completely penetrate the oxidizer stream and, in general, always tends to displace rather than penetrate. The streaking characteristics of the  $A_f/A_o = 1.0$  triplet element can be attenuated by reducing the fuel momentum. This is illustrated in Figure 27, where the observed streak characteristic was modified by reduced momentum as the fuel orifice area was increased at a constant mixture ratio.

Data similar to those presented earlier for the premix and shear designs are found for the like doublet element in Figures 28 through 32. Particular attention should be directed at Figures 28, 29 and 30, where the element spacing effects are parametrically illustrated. These data indicate that an optimum is found at a fuel to oxidizer spacing of 0.1 in. (0.254 cm). Element spacing lower than the optimum have lower mixing efficiency because, when the elements are close together, the primary fans interact strongly forming secondary fans. These fans are nonhomogenous in nature with fuel on one side of the fan and oxidizer on the other. When the doublet spacing is larger than the optimum value, mixing is inhibited simply because the elements are too far apart. Compatibility of this element, as shown in Figure 32 was not good since large circumferential variations in O/F or streaks were measured.

## II, C, Task II - Cold Flow Model Testing and Analysis (cont.)

Data for the parallel sheet elements are found in Figures 33 through 37. As a function of length, thrust/element, and propellant temperature, the data appear to be well behaved and show the expected trends. As a function of O/F, the data increase in mixing efficiency, contrary to the trend of the similar coaxial element. Compatibility effects are as expected: wide O/F variations with  $(O/F)_L$  depending on which side the element is probed.

The external impinging F-O-F triplet data are depicted in Figures 38 through 41. In general, this element configuration is very sensitive to all operating and geometry variables. Refer to Figure 38 where mixing efficiencies for various impingement angles and area ratios as a function of thrust/element are depicted. At the 15 lbf level, the extreme sensitivity of mixing efficiency with impingement angle is noted. One also notes that area ratio influences are optimized in the 1.0 to 1.25  $A_f/A_o$  range. These data are cross plotted in Figures 39 and 40. Referring to Figure 39, one notes that the  $A_f/A_o = 0.96$  mixing efficiency increases dramatically with impingement angle. Inspection of the detailed flow field reveals that, as the radial momentum component is increased by increasing the impingement angle, increased penetration of the axial oxidizer jet occurs, thus yielding a more homogenous flow field. However for the area ratio = 0.50 data, a contrary trend is noted. In this case, overpenetration is achieved and increasing the impingement angle only amplifies the excess penetration of the fuel. Mixing was also determined to be a strong function of mixture ratio coupled with impingement angle. On the fuel-rich side of the optimum, overpenetration occurred; on the oxidizer-rich side, underpenetration occurred (See Figure 41). In general, the compatibility of this element is expected to be poor. Figure 42 indicates the degree and magnitude of the potential compatibility problem for the overpenetrated oxidizer jet. The entire flow field boundary is oxidizer rich and varies widely in the circumferential direction.

## II, C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

### c. Mathematical Cold Flow Model Analysis

Approximate first order mathematical models are being developed to describe the fundamental mixing processes for the various basic element types. The solutions from these mathematical models can then be used to correlate the interdependent effects of primary design parameters and operating conditions on the various element mixing efficiencies and element compatibility characteristics. Approximate models have been completed for the shear coaxial element, like doublet element, and parallel sheet element. These models are able to predict the following experimental cold flow effects:

- (1) The effect of progressively increasing axial displacement ( $L'$  or  $L/D$ ) on maximum measured dynamic head and maximum deviation from equilibrium specie concentration on the element centerline.
- (2) The effect of injector O/F variation.
- (3) The effect of fuel to oxidizer orifice area ratio,  $A_f/A_o$ .
- (4) The effect of fuel to oxidizer injection dynamic head ( $\Delta P_f/\Delta P_o$ ) ratio.
- (5) Effect of varying element size,  $F/E$ .
- (6) Effect of propellant temperature,  $T_p$ .
- (7) Effect of impingement angle,  $\theta$ .

#### (1) Physical Basis for Mathematical Model Formulation

The cold flow tests were conducted with three distinct gaseous species. The fuel element flows actual  $H_2$ . The oxidizer element uses  $N_2$  to simulate  $O_2$ . A helium bleed flow is superimposed atop the two active propellants above to suppress element recirculation. A state of perfectly uniform mixing ( $E_m = 1.00$ ) can be defined by a gas mixture distribution in which all three gas species are in equilibrium in a fixed relative proportion

## II, C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

(constant O/F) at all points. This is the equilibrium mole fraction that each gas specie must asymptotically approach in an infinite length chamber. At the exit of the fuel and oxidizer element orifices, the initial composition must be 100% mole fraction of  $H_2$  and  $N_2$ , respectively. At the element exit,  $E_m = 0$  (by definition).

In the first approximation, the rate of change of  $E_m$  from 0 to 100% is determined by the mathematical mixing model. Early in the cold flow data analysis effort, it was noted that the empirical rate of change of species mole fraction from its 100% pure initial value to its asymptotic equilibrium value was directly proportional to the rate of change in local element dynamic head, starting from its initial injection value to its asymptotic uniform negligible value. The above merely proved that the empirical mass transfer rate was found to be directly proportional to the momentum transfer rate. The latter was calculated analytically by assuming initial potential flow characteristics at the element exit and using classical simplified boundary layer solutions to calculate the downstream momentum transfer (dynamic head dissipation) rate. Therefore, it is reasonable to assume that, if the analytical model can predict the rate of change of element dynamic head and species composition which is empirically measured, the significant parameters in the analytical solution can likewise correlate the empirical rate of change in the mixing distribution.

All of the elements tested on this program utilize sharp edge inlet orifices to minimize fabrication cost. Since all elements tested fit into a single injector/chamber fixture, they all have nearly constant orifice length. Therefore, the variation in F/E tested results in widely varying element L/D. Thus, as a preliminary step to the mathematical model formulation, it was necessary to conduct an element hydraulic analysis to define the actual

## II, C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

flow characteristics. The automated DATNAL computer program utilized the geometric orifice area and assumed that both fuel and oxidizer discharge coefficients,  $C_{Df}$  and  $C_{Do} = 1.00$ . This was done for expedience since the data reduction and DATNAL analyses had to be performed prior to the empirical data correlation and  $C_D$ 's were not available at that time.

The element  $C_D$  is calculated theoretically based upon the physical contraction coefficient at the vena contracta ( $C_{co}$ ), orifice Reynolds number, and orifice L/D using the mathematical hydraulic model developed in Reference R and using the method eluded to in Reference R. These values of  $C_D$  are then used to define an average effective element injection velocity which is related to the injection velocity originally calculated on the DATNAL program by the equation below.

$$V_{i, \text{effective}} = V_{iJ} = \frac{V_{i, \text{DATNAL}}}{C_{Di}} \quad (1)$$

Strictly speaking, the actual injection velocity on the element centerline is inversely proportional to the physical contraction coefficient at the vena contracta ( $C_{coi}$ ), resulting in a higher local velocity than that calculated by Equation (1). Elsewhere, the local injection velocity is less than  $V_{iJ}$ , but to consider the detail injection velocity and mass profile with boundary layer effects results in an unnecessarily complex mathematical solution without significantly enhancing the overall results. Therefore, using the effective  $C_D$  squares off the actual injection velocity profile, permitting it to be replaced by an equivalent potential flow jet at the injector face. By definition, the injection dynamic head is calculated as follows:

$$P_{Do_i} = 1/2 \rho_i V_{iJ}^2 \quad (2)$$

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For simple cylindrical orifices drilled in a flat plate with moderate  $L/D$ , the theoretically calculated injection dynamic head is in close agreement with the empirical injection  $\Delta P$  measured from the injection manifold pressure to  $P_c$ . This verifies the accuracy of the predicted hydraulic analyses. However, long  $L/D$  elements, swirler coaxial elements, internal premix triplet and pentad elements, and other special cases must have their experimental injection  $\Delta P$ 's reduced by the pressure losses attributed to friction, internal expansion, and turbulent dissipation to provide an accurate measure of corrected injection dynamic head at the injector face.

The element hydraulic analysis results were used to define the injection velocity, injection dynamic head, and effective element area at the initial starting point at the element exit. Downstream from the injector face boundary layer, growth rates were calculated to predict the rate of change of local dynamic head and species composition. These mathematically predicted trends were then plotted and compared with the empirical data to verify the significance of the primary design and operating parameters.

### (2) Mathematical Mixing Models for Various Element Types

First order analytical approximations have been completed for the various shear and viscous mixing elements. A brief summary of their mathematical development is described in the following subsections.

#### (a) Shear Coaxial Element

The shear coaxial element is mathematically characterized by a circular jet of effective diameter  $C_{D_o}^{1/2} \cdot D_o$  with a concentric annular fuel orifice surrounding it. The effective fuel annulus width is  $t_f = 1/2 C_{D_f} (D_{f2} - D_{f1})$ . The fuel hydraulic diameter is calculated using the standard relationship,

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$$D_{H_f} = \frac{4 \left[ \frac{\pi}{4} (D_{f2}^2 - D_{f1}^2) \right]}{\pi (D_{f2} + D_{f1})} = (D_{f2} - D_{f1}) \quad (3)$$

where:  $D_{f2}$  = outer fuel annulus diameter  
 $D_{f1}$  = inner fuel annulus diameter

The diameter-based Reynolds number is calculated for both fuel and oxidizer elements using the hydraulic diameter.

$$Re_{D_i} = \frac{\rho_i V_{iJ} D_i}{\mu_i} \quad (4)$$

The Reynolds number for gas/gas propellants is on the order of  $10^5$  so that the turbulent flat plate boundary layer solution is transformed to the form

$$\frac{\delta_o}{R_o} = \frac{0.75 (L/D_o)^{0.8}}{Re_{D_o}^{0.2}} \quad (5)$$

and

$$\frac{\delta_f}{t_f} = \frac{0.75 (L/D_{H_f})^{0.8}}{Re_{D_{H_f}}^{0.2}} \quad (6)$$

where:  $\delta$  = velocity boundary layer thickness  
 $R_o$  = oxidizer radius ( $1/2 D_o$ )  
 $t_f$  = fuel annulus width,  $1/2 (D_{f2} - D_{f1})$

Equations (5) and (6) above can evaluate the relative velocity boundary layer thickness as a function of the axial distance from the injector face, L.



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To be exact, the injection velocity profile has to be integrated to simultaneously satisfy the momentum and continuity equations in the manner described in Reference R. However, for mathematical simplicity, the assumption can be made that the initial potential flow diameter is reduced radially inward at the same rate that the boundary layer grows radially outward. Then a reduced oxidizer potential flow boundary coefficient,  $C_b$ , can be defined by

$$C_b = (\sqrt{C_{D_o}} - \delta_o/R_o)^2 \quad (7)$$

Similarly, an increased oxidizer boundary layer contraction coefficient,  $C_c$ , can be defined by

$$C_c = (\sqrt{C_{D_o}} + \delta_o/R_o)^2 \quad (8)$$

Next, it is approximated that the local oxidizer velocity profile in the boundary layer varies linearly from  $V_{oJ}$  at  $C_b$  to zero velocity at  $C_c$  as shown schematically in Figure 43. The momentum transfer (dynamic head dissipation) rate can now be calculated by integrating the dynamic head throughout the local velocity profile.

$$P_D(L) = \frac{1}{C_c \pi R_o^2} \left\{ \int_0^{R_o \sqrt{C_b}} (1/2 \rho_o V_{oJ}^2) 2\pi r dr + \int_{R_o \sqrt{C_b}}^{R_o \sqrt{C_c}} 1/2 \rho_o \left[ V_{oJ} \left[ 1 - \left( \frac{r/R_o - \sqrt{C_b}}{\sqrt{C_c} - \sqrt{C_b}} \right) \right] \right]^2 2\pi r dr \right\}$$

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which integrates to

$$P_D(L) = (1/2 \rho_o v_{oJ}^2) \left[ \frac{C_b}{C_c} + \frac{3C_c - C_b - 2 \frac{C_b^2}{C_c} - 4/3 \left[ 1 - \left( \frac{C_b}{C_c} \right)^{3/2} \right]}{\left[ \sqrt{C_c} - \sqrt{C_b} \right]^2} \right]$$

Using the definition of injection dynamic head from Equation (2), the local to initial dynamic head ratio is

$$\frac{P_D(L)}{P_{D_o}} = \frac{C_b}{C_c} + \frac{3C_c - C_b - 2 \frac{C_b^2}{C_c} - 4/3 \left[ 1 - \left( \frac{C_b}{C_c} \right)^{3/2} \right]}{\left[ \sqrt{C_c} - \sqrt{C_b} \right]^2} \quad (9)$$

Once the dynamic head ratio is mathematically accounted for, the local oxidizer composition can be calculated from

$$X_o(L) = X_{o,eq} + \frac{P_D(L)}{P_{D_o}} (1.000 - X_{o,eq}) \quad (10)$$

where:  $X_o(L)$  = local mole fraction of oxidizer propellant  
 $X_{o,eq}$  = equilibrium mole fraction of oxidizer propellant based on overall O/F and helium flow rate

To make the mathematical solution computationally tractable for manual calculation, it was discovered that the initial dynamic head decay could be adequately approximated by neglecting the contribution to the total dynamic head in the boundary layer. This is mathematically handled by neglecting the second term in the right-hand member of Equation (9) and simplifying it to

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$$\frac{P_D(L)}{P_{D_o}} \approx \frac{C_b}{C_c} = \frac{[\sqrt{C_{D_o}} - \delta_o/R_o]^2}{[\sqrt{C_{D_o}} + \delta_o/R_o]^2} \quad (11)$$

The analytically predicted local dynamic head using the approximation of Equation (11) is plotted on Figure 44 vs L/D for the 67 Newton (15 lbf) shear coaxial element. The experimental oxidizer dynamic head measured on the element axis using probe number 6 is shown for comparison. Figure 44 shows that, in spite of the many gross mathematical approximations which were made, the calculated dynamic head decay rate based on a viscous boundary layer mechanism closely approximates the experimental trend.

Likewise, the maximum measured oxidizer mole fraction on the coaxial element axis is plotted on Figure 45 vs the analytically predicted local composition using Equations (10) and (11). Again, the mathematically predicted  $N_2$  composition profile provides an adequate first order approximation to the measured local compositions.

The mathematical treatment of the annular fuel dynamic head dissipation rate is conceptually similar using the boundary layer solutions except for differences in the boundary conditions which are dictated by the fuel orifice geometry. First of all, Equation (6) shows that the fuel hydraulic diameter is used in the Reynolds number and L/D terms in the right member but the geometric annulus dimension is used for the denominator in the left member. A second difference is that the fuel viscous drag dissipates itself in two directions: radially inward toward the oxidizer and radially outward toward the chamber wall. Furthermore, since  $t_f$  is generally much less than  $1/2 D_f$ , the boundary layer expansion occurs two-dimensionally for the fuel rather than radially as for the circular oxidizer element. Therefore, the annular fuel boundary coefficient and contraction coefficients comparable to Equations (7) and (8) must be redefined as follows:

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$$C_b = C_{D_f} - 2(\delta_f/t_f) \quad (12)$$

$$C_c = C_{D_f} + 2(\delta_f/t_f) \quad (13)$$

The dynamic head associated with the two-dimensional annular fuel velocity profile described by Equations (12) and (13) was numerically integrated. The solution is shown on Figure 46. Because the fuel element potential flow width is narrow in comparison to the oxidizer,  $1/2 C_{D_f} (D_{f2} - D_{f1}) \ll \sqrt{C_{D_o}} \times D_o$ , and because the fuel drag occurs on two surfaces instead of one, a numerical comparison of Equation (12) with Equation (7) shows that the fuel potential core is dissipated in much shorter axial distances from the injector face than the oxidizer. At axial distances greater than the critical length when fuel  $C_b = 0$ , Figure 47 characterizes the local to initial fuel dynamic head ratio. The calculated fuel dynamic head profile is also shown on Figure 44. It is obvious that the calculated fuel dynamic head dissipation rate occurs considerably faster than for the oxidizer. The experimental dynamic pressure downstream of the fuel annulus was not available for direct comparison with the analysis. This is because the midpoint of the fuel annulus occurs on a 0.092-in. radius and the nearest experimental probes are on a 0.125-in. radius. Near the injector face where the gradients are steep, the 0.033-in. radial mismatch is significant in comparison with the fuel annulus dimension ( $t_f = 0.028$  in.). Nevertheless, for lack of better data, the eight probes on the 0.125-in. radius were averaged as a measured lower limit of the fuel dynamic head.

Likewise, the calculated fuel mole fraction profile is plotted on Figure 45, and the 0.125-in. radius probe measured compositions were averaged and plotted with the full realization that the actual maximum fuel mole fraction might be somewhat higher than shown.

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It should be remembered that, near the injector face, the radial dynamic head gradient and species gradient are very steep. A deviation as small as one probe diameter from perfect concentricity between the element centerline and the probe measurement position could significantly influence the measured data. Thus, it is probable that the real (undetected) data may actually be in better agreement with the analytical prediction than the experimentally measured data shown in Figures 44 and 45. Therefore, it can be concluded that the viscous boundary layer solutions provide an acceptable theoretical model of the shear coaxial mixing rate as a function of length.

Another operating parameter which was analytically evaluated was the influence of O/F on the mixing rate for a constant injection element geometry and fixed L/D. The 67 Newton (15 lbf) shear coaxial element was evaluated at  $L/D = 7$  for  $O/F = 2.0, 4.0, \text{ and } 6.5$ . At low O/F, the fuel to oxidizer injection dynamic head ratio increases and, at high O/F, it decreases. The previously developed shear coaxial model was applied to the mixture ratio survey tests. It was found that the measured fuel and oxidizer dynamic head variation with O/F variation was reasonably approximated. The fuel and oxidizer mole fractions predicted by Equation (10), however, were significantly in error. At low O/F, the oxidizer mole fraction was overpredicted and the fuel mole fraction was underpredicted. The opposite occurred at high O/F. After considerable thought, the following explanation was conceived.

Throughout the above model development, the fuel and oxidizer elements were treated independently as if each were acting alone. Then the solutions were superimposed to infer overall mixing influences. In reality, the two solutions must be coupled and the interaction of one must be considered on the other. Equation (10) is only valid upstream of the point where the oxidizer and fuel boundary layers initially come into contact. Downstream of this point, the two jets combine to act as one. The contribution of

## II, C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

each to the resultant jet must be proportional to their respective mole fractions since mixing occurs on a molecular basis. Since the rapid mixing zone near the injector face is controlled by Newton's equations of motion, the primary normalizing parameter must be the injection dynamic head since this provides the mixing potential. Therefore, define an equivalent injection dynamic head,  $P_{DE}$ , which is the overall result of the separate fuel and oxidizer contributions.

$$P_{DE} = \frac{\frac{\dot{w}_o}{MW_o} \times P_{D_o} + \frac{\dot{w}_f}{MW_f} \times P_{D_f}}{\frac{\dot{w}_o}{MW_o} + \frac{\dot{w}_f}{MW_f}}$$

The above relationship can be simplified to

$$P_{DE} = \frac{P_{D_o} + \frac{MW_o/MW_f}{O/F} \times P_{D_f}}{1 + \frac{MW_o/MW_f}{O/F}} \quad (14)$$

After a combination of analytical considerations, plus empirical trial and error, it was determined that the fuel and oxidizer compositions could best be correlated by the following equation:

$$X_i(L) = X_{i,eq} + \left( \frac{P_{D(L)}}{P_{D_{o,i}}} \right) \left( \frac{P_{D_{o,i}}}{P_{DE}} \right) (1.000 - X_{i,eq}) \quad (15)$$

The reason that the  $O/F = 4$  data shown on Figure 45 did not require the equivalent dynamic head ratio term is because the oxidizer and fuel injection dynamic heads were 6.3 and 6.8 psi, respectively. Using Equation (14),  $P_{DE} = 6.7$  psia and the factor is close to unity for both the oxidizer and fuel compositions and was not missed.

## II, C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

The problem with the shear coaxial element is that the fuel jet is diffused much faster and approaches the equilibrium fuel composition at a much faster rate than the oxidizer. This always results in an oxidizer-rich core region which is the greatest obstacle to achieving high  $E_m$ . Therefore, to achieve high mixing efficiency, the analytical model dictates the necessity of accelerating the oxidizer diffusion rate and retarding the fuel dispersion rate. The analytical model predicts that this can only be done by reducing the oxidizer injection dynamic head and increasing the fuel injection dynamic head as required by Equation (15). In practice, this is achieved by either operating at low O/F or decreasing  $A_f/A_o$ . The experimental data shown on Figures 8 and 11 confirm both analytical predictions.

Since the mass diffusion rate can be analytically described by viscous boundary layer solutions, all element design parameters and operating conditions are either automatically accounted for or implied in such parameters as the Reynolds number,  $L/D$ , propellant density, viscosity and molecular weight, pressure, temperature, orifice geometry, weight flow rate, mixture ratio, injection dynamic heads, injection velocity, etc.

It has been adequately demonstrated that, when the test design parameters and operating conditions are properly described in the mathematical model, the model will quantitatively predict the experimentally measured mixing efficiency trends. Therefore, it stands to reason that, if any single design parameter or single variation in operating condition is parametrically analyzed by the mathematical model while holding all other parameters constant, the model must be able to predict the trend which can be expected by the real world variation on the element mixing characteristics.

The one-to-one correspondence between analytically predicted mixing profiles and the experimental cold flow mixing data as shown in Figure 48 demonstrates the practical utility of developing an

## II, C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

approximate mathematical mixing model to correlate and better understand the experimental data. Much higher confidence can be placed in correlations which have a logical theoretical basis because the model can be used to evaluate subtle second and third order effects on the design extrapolation which would otherwise be neglected if based only on empirical first order correlations.

### (b) Like-on-Like Doublet Element

The like-on-like doublet element incorporates both impingement and shear principles. The impingement momentum is mathematically characterized to describe a gaseous potential flow spray fan similar to a conventional liquid propellant spray fan. Viscous boundary layer effects are assumed to occur on the spray fan surfaces and the two solutions are coupled.

A like doublet is mathematically characterized by equal stream diameters, equal density, equal injection velocity and momentum from the opposing orifices. Thus, the spray fan is symmetrical. If the resultant spray fan is initially analyzed as a bounded potential core, the spray fan propagation angle normal to the impingement plane can be mathematically shown to be

$$\alpha = \sin^{-1} (\tan \theta) \quad (16)$$

where:  $\alpha$  = spray fan half angle  
 $\theta$  = impinging doublet half angle ( $\theta \leq \pi/4$  radian)

From continuity considerations, the potential core local spray fan thickness can be shown to be

$$\frac{t_f}{D} = \frac{\pi C_D}{4 (L/D) \cos \theta \tan \alpha} \quad (17)$$



II, C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

where:  $t_f$  = potential flow spray fan thickness

The width of the spray fan is  $2L \tan \alpha$ .

The potential spray fan surfaces are acted upon by viscous forces. The flat plate turbulent boundary layer solution shows that

$$\delta = \frac{0.375 L}{(L/D)^{0.2} Re_D^{0.2}} \quad (18)$$

The viscous effects on the narrow edges of the spray fan can be neglected. However, there is a critical  $L/D$  at which the velocity boundary layers acting from both of the flat surfaces on the spray fan become equal to the potential flow spray fan thickness. Equating Equation (17) to twice Equation (18), the critical  $L/D$  is

$$\frac{L_{crit}}{D} = \frac{\pi C_D Re_D^{0.2}}{3 \cos \theta \tan \alpha} \quad (19)$$

$$t_{f,min} = \frac{\pi C_D \cdot D}{4 (L_{crit}/D) \cos \theta \tan \alpha}$$

or

$$t_{f,min} = \frac{3D}{4 Re_D^{0.2}} \quad (20)$$

$$\text{Max spray fan width} = 2L_{crit} \tan \alpha$$

Equation (19) shows that increasing the orifice  $C_D$  or Reynolds number will increase the critical  $L/D$ , whereas increasing the doublet impingement half angle decreases it. Equation (20) shows that the

## II, C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

minimum equivalent potential spray fan thickness is directly proportional to the orifice diameter (implies F/E and injection dynamic head influence) and inversely proportional to the one-fifth power of Reynolds number. The physical significance of the minimum potential spray fan thickness is as follows. When the viscous boundary layer effects propagate all the way through the potential fan, the normal impingement component of the doublet injection momentum which was assumed to cause the fan spreading rate has been largely dissipated. Therefore, beyond  $L_{crit}$  the potential core is assumed to be limited to a pure axial displacement. The experimental test data support this simplified asymptotic mathematical approximation.

Compare calculated  $\delta$  from Equation (18) with potential thickness,  $t_f$ , defined by Equation (17) if  $L < L_{crit}$ . In that case,

$$\frac{C_b}{C_D} = 1 - 2 (\delta/t_f) \quad (22)$$

$$\frac{C_c}{C_D} = 1 + 2 (\delta/t_f) \quad (23)$$

Use Equation (22) with Figure 46 to predict  $P_D/P_{D_0}$ .

If  $L > L_{crit}$ , use  $2\delta$  from Equation (18) and  $t_{f,min}$  from Equation (20) in conjunction with Figure 47 to predict  $P_D/P_{D_0}$ . In either case, the calculated  $P_D/P_{D_0}$  ratio can be used with Equation (15) to predict the axial mole fraction profile.

The above like doublet model explains the empirically observed effect of axial length variation shown in Figure 49. It also predicts the observed trends for O/F survey,  $A_f/A_0$  variation, and F/E variation.

## II, C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

The only test variation which has not yet been adequately characterized by the mathematical model has been the effect of variable spacing between doublet pairs. It is suspected that doublet spacing affects the fuel/oxidizer fan interaction and the actual secondary impingement fan deformation and distortion in the real world has not yet been characterized mathematically. However, the empirical data show this is probably a second order effect (see Figure 29) and its accurate model development has been deferred due to lack of funds.

### (c) Parallel Sheet Element

The parallel sheet element was evaluated for potential HIPERTHIN injector applications. An actual HIPERTHIN element was not cold flow tested for two reasons. Its manufacturing cost is higher on a small scale test element because of the relatively extensive fabrication setup in comparison to a single interchangeable machined orifice plate for the other elements tested. The second reason is that, because of its normally small element size, the cold flow distribution would have to be tested much closer to the injector face to be realistic. If this were done, a completely new set of instrumentation would have been required to sample the data. The parallel sheet element was tested at  $F/E = 222$  Newtons (50 lbf) and 13 Newtons (3 lbf). This was done for ease of testing with the expectation that the results could be extrapolated down to a HIPERTHIN scale.

Mathematically speaking, the parallel sheet element should be the simplest element to model based on viscous boundary layer growth rates. However, the theoretical hydraulic analysis revealed that, because of the  $60^\circ$  contracting mitre bend in the fuel orifice plate, the resulting fuel stream was canted  $0.57$  radian ( $33^\circ$ ) and  $0.37$  radian ( $21^\circ$ ) toward the axial oxidizer jet in the high and low thrust elements, respectively. The experimental cold flow

## II, C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

distribution data confirm that the fuel was indeed canted by some unknown angle toward the oxidizer. Furthermore, because the oxidizer manifold inlet diameter was smaller than the high thrust parallel sheet oxidizer element widest dimension, the oxidizer jet only effectively filled approximately one-half the geometric oxidizer width. The local species distribution data, local dynamic head data, and overall oxidizer element  $\Delta P$  data conclusively confirmed this effect. Therefore, although the geometric  $A_f/A_o$  ratio was unity, the actual ratio was closer to two because of halving  $C_{D_o}$ . Another factor to consider is that, in actual practice, a HIPERTHIN injector would have a multitude of adjacent elements surrounding and interacting with it. The tested single cold flow element only had an opposite propellant on one side, leaving the other side unconstrained to diffusion. The results of the above deviations from ideal parallel sheet design were included in the mathematical model formulation.

Based on the calculated hydraulic behavior of the parallel sheet elements as actually tested, its descriptive model is a combination of partial parallel sheet and partial unlike impinging doublet characteristics. The canted fuel stream caused the formation of a weakly divergent spray fan and, consequently, some fan spreading and potential spray fan thinning with increasing  $L$ . The like doublet equations derived in Section II,C,3,c,(2)(b) can be modified to describe unlike doublet characteristics if  $\theta$ , the effective impingement half angle, is taken to be the effective angle between the initial injected angle and the resultant hydraulic momentum angle, and the problem is treated like a mirror image for the oxidizer and fuel relative to itself. Otherwise, the basic concept of the mathematical model equations previously described for the shear coaxial and like-on-like doublet elements were used to describe the parallel sheet elements.

## II, C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

Variations in axial length, O/F, F/E, and propellant temperature were mathematically evaluated. Initially, there was some deviation noticed between measured and predicted rates of change in the species mole fractions. After a period of analytical reasoning and pondering over the physical situation, the following modification was evaluated in the predicted species mole fraction equation.

$$X_i(L) = X_{i,eq} + \left( \frac{P_D(L)}{P_D} \right) \left( \frac{P_{D_i}}{P_{DE}} \right)^f (1.000 - X_{i,eq}) \quad (24)$$

In going from Equation (10) to Equation (15), the addition of the  $(P_{D_i}/P_{DE})$  ratio was empirically justified on the basis that it accounted for interpropellant interactions. In going further from Equation (15) to Equation (24), the interaction term was raised to the exponent  $f$ . The term  $f$  is the ratio of the common fuel-oxidizer wetted perimeter available for interpropellant interaction divided by the total fuel or oxidizer wetted perimeter available for diffusion and shear mixing. For example, in the low F/E parallel sheet element, the fuel and oxidizer elements were at equal width. Neglecting end effects on the 10:1 aspect ratio slot, both the oxidizer and fuel  $f$  exponents were set equal to 0.5 since only half (side facing each other) of their total perimeter is available for interaction. In the high thrust parallel sheet element, the oxidizer  $f$  is equal to 0.5 because of the side facing the fuel. The fuel  $f$  parameter, however, is only equal to 0.25 because only the center half of the side facing the oxidizer element is interacting due to the hydraulic inlet restricted oxidizer element width. When Equation (24) was applied to all the parallel sheet element mathematical models, consistency between measured and predicted mole fractions was considerably improved. With this change, the model was able to successfully predict the empirical effects of  $L$ ,  $O/F$ ,  $F/E$ , and  $T_p$  variations.

## II, C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

These parallel sheet elements illustrate a special situation in which the quality of the pure analysis would probably be better than the quality of the experimental data. If the mathematical model were used to evaluate nonimpinging element characteristics in which both the fuel and oxidizer gas jets were truly parallel and the multiple element interactions were considered with purely viscous drag induced diffusion mechanisms, the mathematically predicted mixing efficiency would probably be more accurate than the present experimental single-element cold flow data.

In retrospect, the nominal O/F shear coaxial model should have been described by Equation (24) instead of Equation (10). The effect of  $(P_{D_i}/P_{DE})$  was not missed because both oxidizer and fuel injection dynamic heads were approximately equal and the ratio was close to unity. In the shear coaxial O/F variation model, the oxidizer f exponent was coincidentally set equal to unity as it should have been because the oxidizer element is completely surrounded by the fuel annulus. In hindsight, the fuel f exponent should have been set approximately equal to 0.5 instead of 1.0 because the interaction only occurs on the inside surface of the fuel annulus. This error in the fuel exponent was not recognized because the  $14/(O/F)$  term in the equivalent injection dynamic head parameter (see Equation (14)) heavily weights  $P_{DE}$  toward the fuel side. Consequently, the  $(P_{D_f}/P_{DE})$  ratio is close to unity and the error in the exponent was not detected at that time. In the like doublet model, both fuel and oxidizer f exponents were again set equal to 1.0. This may have been an adequate approximation because the fuel to oxidizer doublet spacing (which was experimentally varied) was small in comparison to the total spray fan width. Finally, it took the parallel sheet data to refine Equation (24) to its present status. There are probably additional modifications to Equation (24) which are required to further improve its accuracy in describing special element types.

## II, C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

The above mixing model progression graphically illustrates an intriguing dilemma. That is, an exact mathematical model which rigorously and simultaneously accounts for all physical considerations becomes cumbersome, unwieldy, and finally totally intractable mathematically. On the other hand, an approximate mathematical model such as was derived above can be relatively straightforward, easily hand calculated, and sheds considerable valuable physical insight into the process being investigated with a relatively modest expenditure of time and funding. However, it must be realized that this method too has its limitation. Its limitation is that, because it is an approximate model, exact correlation between analytical prediction and measured data cannot always be expected. Therefore, if only minor deviations occur between prediction and data because of neglected second order effects or because of coincidental test conditions, these errors must be attributed to either the analytical or measurement "noise level" without being aware of the analytical shortcomings within the approximate model. Therefore, the only way that the accuracy of the approximate model can be further improved is to encounter significant and recognizable errors between analysis and data. In other words, successful predictions cannot further improve model accuracy; only through failure can there be a possibility for further refinement. The necessary failure can only be achieved by experience. This means that, ideally, every Task IIB cold flow condition which was experimentally tested should be analytically modeled. Unfortunately, this is beyond the scope of the current program.

In spite of the limitations in the approach taken by the approximate mathematical model tempered by empirical data and experience, this method provides the maximum return for the time and money spent. A conceptually similar approach marrying theoretical/approximate mathematical analysis and experimental data has been proven by ALRC in its success liquid propellant injector hydraulic, atomization, and vaporization dependent energy release model developments.

## II,C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

### (d) Other Element Mixing Models

The approximate mathematical model development effort is currently in progress for the conventional external impinging F-O-F triplet element family.

The swirler coaxial and increased shear coaxial element model description requirement is conceptually understood but has not yet been performed. Although no significant analytical difficulties are anticipated, only peripheral evaluations are presently scoped for these elements.

No analytical effort has yet been made to describe internal premix triplet and pentad elements. The conceptual pre-mixing mechanism is understood based on a scrutiny of the experimental cold flow data. The required initial approach to the mathematical model description has been identified.

### d. Hot Flow Testing

It has been ALRC's belief that cold flow testing alone could not completely describe the mixing process. Combustion does impact the mixing profiles generated in cold flow testing. In Reference 2, this impact was described both analytically and empirically for a conventional shear coaxial element. In general, the combustion adversely biased the mixture ratio profiles; i.e., mixing profiles measured in cold flow were displaced axially by combustion. As part of this program, the effects of combustion were studied for a high mixing efficiency element, the swirl element.



## II, C, Task IIB - Cold Flow Model Testing and Analysis (cont.)

A hot flow test series was conducted with the objective of determining whether combustion influenced the profiles of a swirl coaxial element. The experimental program measured the mixture ratio distribution of both hot and cold flow gas flow fields generated with identical hardware and flow conditions. The only difference between these tests was that, in one case, the  $H_2-O_2$  propellants were burning and, in the other case, they were not. The hot flow hardware was, in fact, the hardware of the cold flow program.

This testing was conducted in the steam-cooled chamber and utilized a double-walled, hot  $H_2$  cooled probe\* to withdraw the gas sample. The sample was routed into the mass spectrometer via copper steam-heated tubing. The resulting data conclusively indicated a combustion mixture ratio profile substantially different than the cold flow profile. These data are presented in Figure 50 as a function of the probe radial and axial distance. This figure indicates that the cold flow mixture ratio gradients had essentially dissipated at the first axial position, indicative of the desirable mixing qualities of the swirl coaxial element. Comparing the hot flow profiles with the cold flow profiles at the same length, it is apparent that the mixture ratio profiles are steeper (greater deviations from uniformity) and persist to 7.17 in. (18.25 m). These data substantiate that the combustion does adversely affect the mixing. These data are plotted in a different format in Figure 51; they indicate that three mixing zones are possible:

- (1) The near zone where copious mass transfer takes place and combustion is initiated.
- (2) An intermediate zone where the large density changes of combustion products displace the oxidizer inward and the fuel outward.
- (3) A region where the continued rotation of the oxidizer-rich core promotes radial diffusion of the oxidizer-rich products into the fuel-rich mantle.

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\*Particular care must be taken in this type of testing to ensure that the combustion products ( $H_2O$ ) do not condense anywhere in the system. Thus, all components were heated to over 250°F during testing using either steam or heated hydrogen.

## II, Technical Progress Summary (cont.)

### D. TASK IIIA - SINGLE-ELEMENT HOT FIRING DESIGN AND FABRICATION

The single-element hot firing stand is complete and the hot fire hardware is being installed. The hot fire chambers have been designed and fabricated. Three 50-lbf-thrust chambers were built and are shown in Figure 52. Two chambers are 2.0 in. long with a 2.5 and 3.5 contraction ratio. The third chamber is 5.5 in. long with a 2.5 contraction ratio. All the chambers have a area ratio,  $A_e/A_t = 1.75$ . They will be heat sink in type and are designed to have a 2-sec duration while maintaining adequate thermal response. Twelve thermocouples are buried at approximately midwall depth. The thermocouples are located 0.5-in. apart axially and in three rows, 45° apart circumferentially. Provisions are made for a spark type igniter to be located in the chamber wall. The two  $P_c$  taps are located near the injector face and at the entrance to the convergent section of the nozzle.

The three injectors to be tested are the  $0.5 A_f/A_o$  swirl coaxial,  $0.5 A_f/A_o$  coaxial, and the 33% premix triplet. This hardware is currently being modified from the cold flow hardware and will be manufactured and tested during the next reporting period.

### III. CURRENT PROBLEMS

No technical problems are evident at this time. The program has slipped approximately one and a half months. It is anticipated that some portion of this time can be recovered in the hot fire testing.

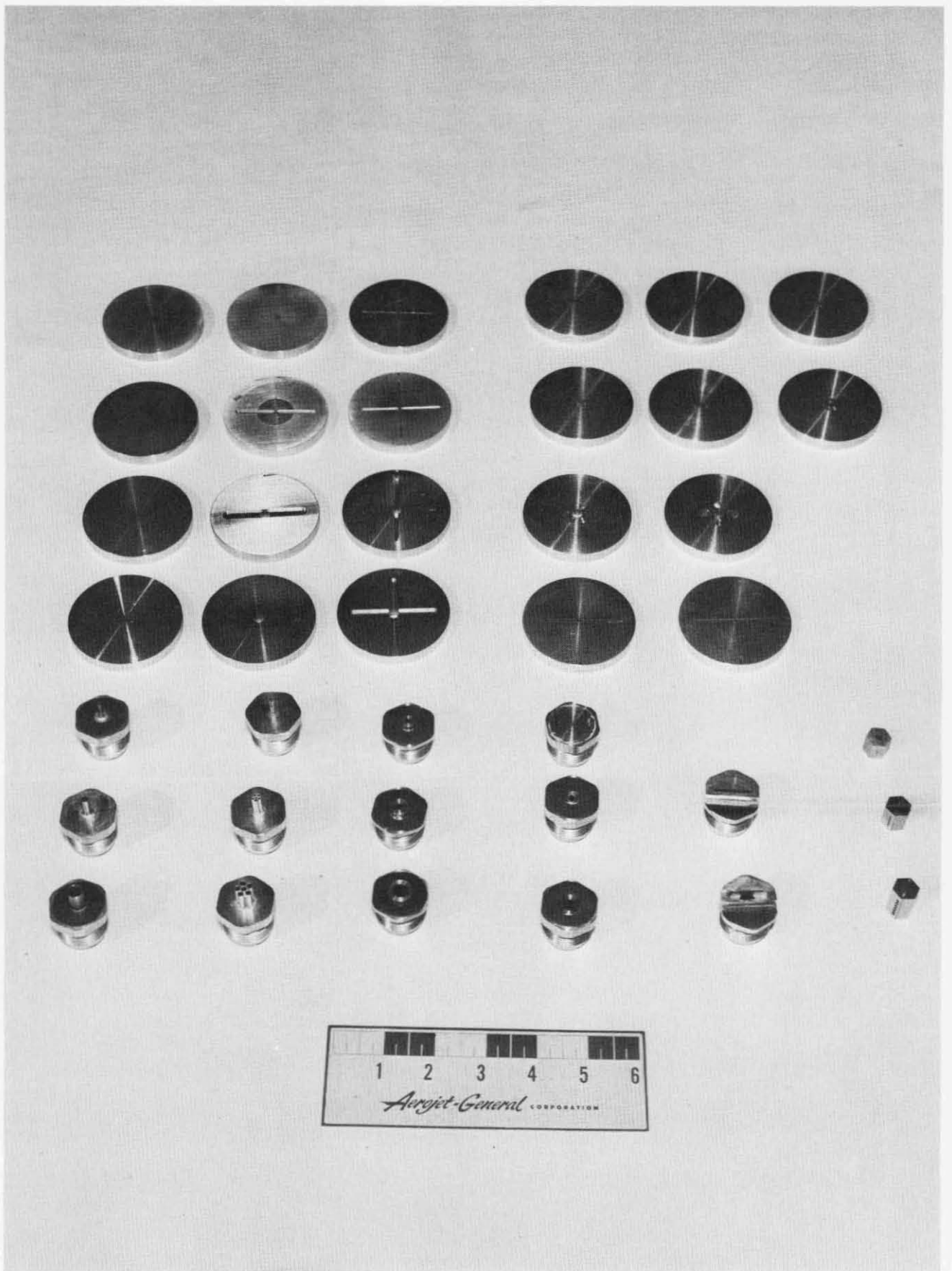
### IV. WORK PLANNED

The remaining single-element cold flow data will be analyzed in the next report period. The hot fire single-element injectors will be tested and the data analysis will be initiated.

### V. CONSUMABLES

The table below lists the consumption to date of propellants and gases together with the anticipated usage during the following month:

	<u>Consumed to Date</u>	<u>Predicted for Next Month</u>
H <sub>2</sub>	5946 lbs	200 lbs
He	1926 lbs	0 lbs
N <sub>2</sub>	13.1 tons	7 tons



SELECTED COLD FLOW ELEMENTS

## GAS/GAS COMBUSTION PROGRAM ALRC CONTRACT NAS3-14379

SPECIES ONE IS H2  
SPECIES TWO IS HE  
SPECIES THREE IS N2  
SPECIES FOUR IS NONE

## DIGITAL DATA LISTING

ALPHA DESIG. \*TRIPLET-90(15) RAKE LOC. \*L/D=7.0 1.0 IN

TEST NO. 144-122

RUN NO 129

CHANNEL	099	002	025	003	003	003	026	027	028	029	009	015	012
TIME (SEC)	POS	AP (PSIA)	COMP	PRESS	SPEC 1	SPEC 2	SPEC 3	SPEC 4	OX MASS FLOW (LBM/SEC)	FUEL MASS FLOW (LBM/SEC)	HE MASS FLOW (LBM/SEC)		
.00	1	.01	NO	YES	.1635	.6543	.1822	.0000	.0281	.0071	.0310		
1.80	2	.01	NO	YES	-.4030	1.3659	.0371	.0000	.0281	.0071	.0310		
3.80	3	.00	NO	YES	-.4869	1.3083	.1787	.0000	.0281	.0071	.0310		
5.80	4	.06	NO	YES	-.2899	1.1389	.1510	.0000	.0281	.0071	.0310		
7.40	5	.43	NO	YES	.0695	1.0742	-.1437	.0000	.0281	.0071	.0310		
9.00	6	.35	NO	YES	.1954	.7952	.0095	.0000	.0281	.0071	.0310		
10.60	7	.02	NO	YES	.2717	.4853	.2430	.0000	.0281	.0071	.0310		
12.20	8	.02	NO	YES	-.8057	1.5613	.2444	.0000	.0281	.0071	.0310		
13.80	9	.21	NO	YES	.2219	.7354	.0427	.0000	.0281	.0071	.0310		
15.40	10	.34	NO	YES	-.2067	.9376	.2691	.0000	.0281	.0071	.0310		
17.20	11	.34	NO	YES	.4654	.5237	.0109	.0000	.0281	.0071	.0310		
18.90	12	.33	NO	YES	-.0004	1.0651	-.0646	.0000	.0281	.0071	.0311		
20.50	13	.34	NO	YES	-.1572	.8792	.2780	.0000	.0281	.0071	.0311		
22.10	14	.12	NO	YES	-.0065	.9966	.0099	.0000	.0281	.0071	.0310		
23.70	15	.11	NO	YES	.2205	.7784	.0011	.0000	.0281	.0071	.0310		
25.30	16	.20	NO	YES	.0603	.9611	-.0215	.0000	.0281	.0071	.0311		
27.10	17	.10	NO	YES	*****	2.9208	-.5102	.0000	.0281	.0071	.0311		
28.90	18	.06	NO	YES	-.0492	1.1378	-.0886	.0000	.0281	.0071	.0311		
30.50	19	.55	NO	YES	.4523	.4376	.1102	.0000	.0281	.0071	.0311		
32.10	20	.03	NO	YES	.0380	1.0424	-.0804	.0000	.0281	.0071	.0311		
33.70	21	.06	NO	YES	.0548	.9170	.0281	.0000	.0281	.0071	.0311		
35.30	22	-3.94	NO	YES	*****	1.6179	.5337	.0000	.0281	.0071	.0311		
37.10	23	.04	NO	YES	-.0023	1.0176	-.0152	.0000	.0281	.0071	.0311		
38.80	24	.04	NO	YES	-.9867	2.0827	-.0960	.0000	.0281	.0071	.0311		
42.20	1	-10.64	YES	NO	.2537	.6538	.0925	.0000	.0281	.0071	.0311		
43.80	2	-10.66	YES	NO	.2681	.6441	.0877	.0000	.0281	.0071	.0311		
45.40	3	-10.67	YES	NO	.2738	.6524	.0738	.0000	.0281	.0071	.0311		
46.90	4	-10.68	YES	NO	.2716	.6555	.0729	.0000	.0281	.0071	.0311		
48.50	5	-10.69	YES	NO	.3185	.6082	.0733	.0000	.0281	.0071	.0311		
50.10	6	-10.69	YES	NO	.3424	.5832	.0745	.0000	.0281	.0071	.0311		
51.70	7	-10.68	YES	NO	.3079	.6218	.0702	.0000	.0281	.0071	.0311		
53.80	8	-10.71	YES	NO	.2787	.6479	.0734	.0000	.0281	.0071	.0311		
55.70	9	-10.71	YES	NO	.2999	.6191	.0810	.0000	.0281	.0071	.0311		
57.70	10	-10.71	YES	NO	.3167	.6065	.0768	.0000	.0281	.0071	.0311		
59.30	11	-10.72	YES	NO	.3238	.6025	.0737	.0000	.0281	.0071	.0311		
61.30	12	-10.71	YES	NO	.3383	.5914	.0703	.0000	.0281	.0071	.0311		
63.10	13	-10.71	YES	NO	.3463	.5829	.0708	.0000	.0281	.0071	.0311		
65.10	14	-10.72	YES	NO	.2705	.6640	.0646	.0000	.0281	.0071	.0311		
67.10	15	-10.72	YES	NO	.2498	.6864	.0638	.0000	.0281	.0071	.0311		
68.70	16	-10.73	YES	NO	.2630	.6765	.0605	.0000	.0281	.0071	.0311		
70.80	17	-10.72	YES	NO	.3140	.6156	.0704	.0000	.0281	.0071	.0311		
72.80	18	-10.72	YES	NO	.3089	.6202	.0710	.0000	.0281	.0071	.0311		
74.80	19	-10.72	YES	NO	.3473	.5765	.0762	.0000	.0281	.0071	.0311		
76.80	20	-10.72	YES	NO	.3224	.6059	.0717	.0000	.0281	.0071	.0311		
78.90	21	-10.29	YES	NO	.2868	.6427	.0705	.0000	.0281	.0071	.0311		

29 NOV 71

TEST NO. 11122

CHAI,NEL	099	002	025	003	003	003	026	027	028	029	009	015	012
TIME (SEC)	POS	AP (PSIA)	COMP	PRESS	SPEC 1	SPEC 2	SPEC 3	SPEC 4	OX MASS FLOW (LBM/SEC)	FUEL MASS FLOW (LBM/SEC)	HE MASS FLOW (LBM/SEC)		
80.90	22	-10.66	YES	NO	.2324	.7134	.0542	.0000	.0282	.0071	.0311		
82.80	23	-10.39	YES	NO	.2976	.6368	.0656	.0000	.0282	.0071	.0311		
84.90	24	-10.34	YES	NO	.3035	.6331	.0634	.0000	.0282	.0071	.0311		

29 NOV 71

TEST NO. 1122

CHANNEL	099	022	024	023	011	017	014	008	005	006	007
TIME	TMAN	TMAN	TMAN	TMAN	PMAN	PMAN	PMAN	PC	PTOT1	PTOT2	PSTAT
(SEC)	(DEG R)	(DEG R)	(DEG R)	(DEG R)	(PSIA)	(PSIA)	(PSIA)	(PSIA)	(PSIA)	(PSIA)	(PSIA)
00	495.4	519.8	514.7	313.4	314.5	663.7	303.2	301.9	302.5	302.4	
1.80	495.4	519.7	514.7	313.5	314.5	663.6	303.2	301.8	302.2	302.1	
3.80	495.5	519.8	514.6	313.8	314.3	663.7	303.1	301.8	302.1	302.0	
5.80	495.4	519.6	514.1	312.9	314.1	663.5	303.1	301.3	302.1	302.1	
7.40	495.6	519.8	514.2	312.5	314.0	663.7	302.9	301.9	301.9	301.8	
9.00	495.6	519.7	514.1	312.6	314.1	663.8	303.0	301.9	301.8	301.8	
10.60	495.6	519.7	513.9	313.2	314.1	663.6	302.8	301.4	302.1	301.9	
12.20	495.6	519.7	513.9	313.0	314.0	663.5	302.8	301.5	301.4	302.0	
13.80	495.7	519.7	513.8	313.0	313.9	663.6	303.1	301.6	301.3	301.9	
15.40	495.6	519.6	513.6	313.3	313.8	663.6	302.9	301.7	295.1	302.0	
17.20	495.7	519.5	513.6	313.1	313.9	663.7	302.8	301.6	301.4	301.3	
18.90	495.6	519.5	513.5	312.4	313.8	664.1	302.6	301.5	301.1	301.4	
20.50	495.7	519.5	513.4	312.7	313.8	663.9	302.9	301.2	301.7	301.5	
22.10	495.7	519.4	513.3	312.4	313.8	663.7	302.9	301.2	301.4	301.4	
23.70	495.6	519.3	513.3	312.7	313.7	663.6	302.7	301.2	301.4	301.5	
25.30	495.2	519.0	512.9	312.0	313.7	663.8	302.4	300.1	301.0	301.2	
27.10	495.3	518.9	513.0	312.0	313.8	663.6	302.8	300.6	300.8	301.2	
28.90	495.5	519.1	513.0	312.1	313.6	663.6	303.1	301.3	301.1	301.3	
30.50	495.1	518.7	512.6	313.1	313.6	663.7	302.6	299.9	301.3	301.1	
32.10	495.5	519.0	513.0	312.4	313.5	663.7	303.0	301.2	301.1	301.3	
33.70	495.5	518.8	512.9	312.6	313.6	663.9	302.9	301.3	301.1	301.4	
35.30	495.5	518.8	512.8	312.6	313.7	663.9	302.9	301.3	297.4	301.4	
37.10	495.2	518.4	512.5	313.3	313.4	663.8	302.6	300.8	301.0	301.3	
38.80	495.6	518.8	512.9	312.7	313.5	664.0	302.6	301.8	301.2	301.3	
42.20	495.1	518.2	512.4	312.0	312.7	663.6	301.6	139.1	300.3	301.1	
43.80	495.1	518.2	512.4	312.3	312.6	663.8	301.6	141.8	300.2	300.9	
45.40	495.3	518.2	512.4	311.9	312.5	664.0	301.6	141.4	300.0	300.9	
46.90	495.3	518.1	512.4	311.6	312.7	663.9	301.7	140.6	300.3	301.0	
48.50	495.2	518.1	512.3	311.7	312.6	663.8	301.4	139.1	300.2	300.7	
50.10	495.2	517.9	512.3	311.3	312.6	663.8	301.5	139.7	299.9	300.6	
51.70	495.4	518.1	512.4	311.4	312.6	663.9	301.6	145.2	300.4	300.7	
53.80	495.1	517.8	512.1	311.4	312.7	664.1	301.4	130.2	300.3	300.5	
55.70	495.0	517.8	512.1	311.0	312.6	663.9	301.4	133.0	300.2	300.5	
57.70	495.3	517.8	512.3	311.7	312.5	663.9	301.4	137.0	298.1	300.6	
59.30	494.9	517.5	512.0	311.1	312.4	664.0	301.4	138.6	300.3	300.4	
61.30	494.9	517.5	511.9	311.0	312.5	664.0	301.3	136.8	300.1	300.1	
63.10	494.9	517.4	511.8	311.3	312.5	664.1	301.2	293.4	156.1	300.2	
65.10	494.8	517.2	511.7	310.9	312.4	664.3	301.4	299.7	142.6	300.3	
67.10	494.7	517.2	511.7	310.9	312.4	664.1	301.3	299.7	139.6	300.2	
68.70	494.3	516.8	511.4	310.7	312.3	663.9	301.4	298.8	141.2	300.2	
70.80	494.4	516.9	511.5	311.9	312.5	664.0	301.3	299.7	139.9	300.2	
72.80	494.5	517.0	511.7	311.0	312.3	664.1	301.4	300.1	141.6	300.2	
74.80	494.6	517.0	511.6	310.8	312.3	664.1	301.4	299.8	147.4	300.1	
76.80	494.3	516.7	511.4	311.9	312.3	664.3	301.3	299.4	145.9	300.1	
78.90	494.4	516.9	511.5	310.8	312.0	664.1	301.3	299.5	205.3	234.1	

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TEST NO. ~~DA122~~

CHANNEL	099	022	024	023	011	017	014	008	005	006	007
TIME		TMAN OX	TMAN FUEL	TMAN HE	PMAN OX	PMAN FUEL	PMAN HE	PC	PTOT1	PTOT2	PSTAT
(SEC)		(DEG R)	(DEG R)	(DEG R)	(PSIA)	(PSIA)	(PSIA)	(PSIA)	(PSIA)	(PSIA)	(PSIA)
80.90	494.4	516.7	511.6	312.2	313.2	664.6	302.2	301.1	220.9	300.7	
82.80	494.2	516.6	511.5	311.3	311.9	664.1	301.3	292.2	202.1	231.9	
84.90	494.3	516.6	511.5	310.7	311.9	664.1	301.2	299.6	203.3	235.9	



# DATA SUMMARY TEST NO. 119122

OX	MASS FLOW (LBM/SEC)	FUEL	MASS FLOW (LBM/SEC)	HE	MASS FLOW (LBM/SEC)	TMAN OX (DEG R)	TMAN FUEL (DEG R)	TMAN HE (DEG R)	PMAN OX (PSIA)	PMAN FUEL (PSIA)	PMAN HE (PSIA)	PC	MIXTURE RATIO
TEST AVERAGE	.0281	.0071	.0311	495.2	518.4	512.7	312.1	313.2	663.9	302.2	3.9610		

## STEADY STATE PRESSURE & COMPOSITION DATA

STEPPER SWITCH POS.	SCAN1 VLV (PSIA)	***** MOLE FRACTIONS *****			SPEC 1			SPEC 2			SPEC 3			SPEC 4			PTOT 1 (PSIA)			PTOT 2 (PSIA)			PSTAT (PSIA)		
		AVE	LAST	AVE	LAST	AVE	LAST	AVE	LAST	AVE	LAST	AVE	LAST	AVE	LAST	AVE	LAST	AVE	LAST	AVE	LAST	AVE	LAST	AVE	LAST
1	.00	.00	.2200	.2200	.6744	.6744	.6744	.1056	.1056	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
2	.00	.00	.2332	.2332	.6663	.6663	.6663	.1005	.1005	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
3	.00	.00	.2387	.2387	.6766	.6766	.6766	.0847	.0847	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
4	.00	.00	.2367	.2367	.6796	.6796	.6796	.0836	.0836	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
5	.37	.37	.2798	.2798	.6355	.6355	.6355	.0847	.0847	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
6	.29	.29	.3019	.3019	.6116	.6116	.6116	.0865	.0865	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
7	.00	.00	.2701	.2701	.6487	.6487	.6487	.0811	.0811	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
8	.00	.00	.2432	.2432	.6724	.6724	.6724	.0844	.0844	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
9	.15	.15	.2624	.2624	.6443	.6443	.6443	.0933	.0933	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
10	.28	.28	.2730	.2730	.6333	.6333	.6333	.0887	.0887	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
11	.28	.28	.2847	.2847	.6300	.6300	.6300	.0853	.0853	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
12	.27	.27	.2983	.2983	.6201	.6201	.6201	.0816	.0816	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
13	.28	.28	.3057	.3057	.6121	.6121	.6121	.0823	.0823	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
14	.06	.06	.2359	.2359	.6899	.6899	.6899	.0742	.0742	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
15	.05	.05	.2171	.2171	.7098	.7098	.7098	.0730	.0730	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
16	.14	.14	.2293	.2293	.7013	.7013	.7013	.0694	.0694	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
17	.04	.04	.2757	.2757	.6430	.6430	.6430	.0813	.0813	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
18	.00	.00	.2710	.2710	.6471	.6471	.6471	.0820	.0820	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
19	.49	.49	.3064	.3064	.6050	.6050	.6050	.0885	.0885	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
20	.00	.00	.2834	.2834	.6336	.6336	.6336	.0830	.0830	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
21	.00	.00	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
22	.00	.00	.2017	.2017	.7364	.7364	.7364	.0619	.0619	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
23	.04	.04	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
24	.04	.04	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000

## \*\*\*\*\* STEPPER SWITCH POS. LEGEND \*\*\*\*\*

POS. 1-20 TOTAL PRESSURE PROBE ELEMENTS BEING READ (POS. NUMBER CORRESPONDS TO ELEMENT NO.)

POS. 21 THREE PROBE STATIC PRESSURES READ AND AVERAGED (ZERO AP CHECK)

POS. 22 CALIBRATION GAS SPECIES DATA FROM MASS SPEC

POS. 23 AMBIENT REFERENCE PRESSURES

# AEROJET LIQUID ROCKET COMPANY ANALYSIS OF COLD-FLOW INJECTOR TEST RESULTS

RUN NO. 129

TEST NO. 122

## TEST DATA

CHAMBER DIAMETER	=	1.50	INCH
AXIAL POSITION	=	1.00	INCH
OXIDIZER FLOW RATE	=	.02813	LBM/SEC
FUEL FLOW RATE	=	.00710	LBM/SEC
HELIUM FLOW RATE	=	.03107	LBM/SEC
MIXTURE RATIO	=	3.96	(COLD FLOW)
FUEL MAN. PRESS.	=	313.2	PSIA
OX. MAN. PRESS.	=	312.1	PSIA
HE MAN. PRESS.	=	663.9	PSIA
FUEL MAN. TEMP.	=	518.4	DEG RANKINE
OX. MAN. TEMP.	=	495.2	DEG RANKINE
HE MAN. TEMP.	=	512.7	DEG RANKINE

## CALCULATED TEST VARIABLES

N2 INJECTION VEL.	=	155.90	FT/SEC
H2 INJECTION VEL.	=	598.99	FT/SEC
HE INJECTION VEL.	=	15.31	FT/SEC
N2 MOMENTUM	=	4.39	LB-FT/SEC-SEC
H2 MOMENTUM	=	4.25	LB-FT/SEC-SEC
MOMENTUM RATIO	=	.97	WFVF/WOV0
VELOCITY RATIO	=	-.13	LB-FT/SEC-SEC
VELOCITY DIFF.	=	3.84	VF/V0
VEL. RATIO--HE/N2	=	443.09	FT/SEC
FUEL-OX SOURCE VEL.	=	.10	VHE/V0
DELTA P OXID INJ.	=	209.85	FT/SEC
DELTA P FUEL INJ.	=	9.92	PSI
OX INJ STIFFNESS	=	10.99	PSI
FUEL INJ STIFFNESS	=	.0328	AP/PC
OX AREA RATIO	=	.0364	AP/PC
FUEL AREA RATIO	=	.0092	AO/ACHAM
VELOCITY-AREA RATIO	=	.0088	AF/ACHAM
MIXTURE-AREA RATIO	=	3.6771	AF*VF/AO*V0
MOMENTUM-AREA RATIO	=	.2416	AF*WF/AO*W0
OX PCT TOTAL FLOW	=	.9283	AF*VF*WF/AO*V0*W0
FUEL EQ OF STATE	=	.7984	W0/W0*WF
OX EQ OF STATE	=	.8510	TF/PC*MMF
NORM/AX INJ MOM	=	.0585	TO/PC*MMO
	=	.4068	

MEASURED AP (PSIA)

ANGLE (DEG)	RADIAL POSITION (IN)	MEASURED AP (PSIA)
0.	.1250	.3750
45.	.3676	.0000
90.	.0411	.1158
135.	.2703	.2797
180.	.0000	.1158
225.	.0000	.0000
270.	.2785	.1158
315.	.4928	.1158

MEASURED P-TOTAL (PSIA)

ANGLE (DEG)	RADIAL POSITION (IN)	MEASURED P-TOTAL (PSIA)
0.	.1250	.3750
45.	.3676	.0000
90.	.0411	.1158
135.	.2703	.2797
180.	.0000	.1158
225.	.0000	.0000
270.	.2785	.1158
315.	.4928	.1158

MEASURED P-STATIC (PSIA)

ANGLE (DEG)	RADIAL POSITION (IN)	MEASURED P-STATIC (PSIA)
0.	.1250	.3750
45.	.3676	.0000
90.	.0411	.1158
135.	.2703	.2797
180.	.0000	.1158
225.	.0000	.0000
270.	.2785	.1158
315.	.4928	.1158

# CALCULATED RESULTS

## LOCAL OX FLUX (LBM/SEC-SI)

ANGLE (DEG)				RADIAL POSITION (IN)			
0.	.0000	.1250	.2500	.3750	.5000	.6250	
45.	.08803	.09697	.00000	.00000	.00000	.00000	
90.	.08803	.03130	.04969	.05097	.03002	.03422	
135.	.08803	.08081	.08539	.08783	.06577	.00000	
180.	.08803	.00000	.04969	.05097	.03002	.03422	
225.	.08803	.00000	.00000	.00000	.00000	.00000	
270.	.08803	.08275	.04969	.03002	.03422	.00000	
315.	.08803	.11679	.08539	.08783	.06577	.00000	
			.04969	.05097	.03002	.03422	

## LOCAL FUEL FLUX (LBM/SEC-SI)

ANGLE (DEG)				RADIAL POSITION (IN)			
0.	.0000	.1250	.2500	.3750	.5000	.6250	
45.	.02211	.02304	.00000	.00000	.00000	.00000	
90.	.02211	.00763	.01180	.01118	.00642	.00783	
135.	.02211	.02127	.02050	.01980	.01330	.00000	
180.	.02211	.00000	.01180	.01118	.00642	.00783	
225.	.02211	.00000	.00000	.00000	.00000	.00000	
270.	.02211	.00000	.01180	.01118	.00642	.00783	
315.	.02211	.02212	.02050	.01980	.01330	.00000	
		.02909	.01180	.01118	.00642	.00783	

2 (7)

LOCAL MIXTURE RATIO (O/F)

4.37	4.82	4.37
	4.94	
4.68	4.44	4.68
4.56	4.17	4.56
4.21	4.21	
	3.80	4.07
	4.10	
6.67	5.99	4.91
4.93	4.17	3.98
	4.21	4.21
	4.91	4.93
	5.99	6.67
	4.21	4.02
	3.74	
4.21	4.21	
4.56	4.17	4.56
4.68	4.44	4.68
4.37	4.94	4.37
	4.82	

LOCAL MASS FLUX (LB<sup>M</sup>/SEC-SI)

	.00000	
	.14392	.08749
.08749		
.07812	.19718	.07812
.12489	.19597	.12489
.13320	.13320	
	.18986	
	.00000	.07428
.00000 .00000 .00000 .00000 .19908 .22392 .00000 .00000 .00000		
	.00000	.25991
	.19280	
.13320	.13320	
.12489	.19597	.12489
.07812	.19718	.07812
.08749	.14392	.08749
	.00000	



	RADIAL POSITION INTEGRATED TO				
	.7500	.6250	.5000	.3750	.2500
MEASURED OVERALL MIXTURE RATIO =	3.9610				.1250
INTEGRATED MIXTURE RATIO =	4.4099				
MEASURED OVERALL MASS FLOW RATE =	.0663				
MEASURED OVERALL OX FLOW RATE =	.0231				
MEASURED OVERALL FUEL FLOW RATE =	.0071				
INTEGRATED MASS FLOW RATE =	.1355				
INTEGRATED OX FLOW RATE =	.0520				
INTEGRATED FUEL FLOW RATE =	.0125				
MIXING COEFFICIENT	97.61	97.22	97.18	98.05	98.85
ETAM	95.95	95.32	95.39	96.42	97.81
PERCENT NOMINAL CSTAR	99.93	99.91	99.91	99.93	99.98

LBM/SEC  
LBM/SEC  
LBM/SEC  
LBM/SEC  
LBM/SEC  
PERCENT  
PERCENT

# CALCULATED RESULTS AT RADIAL LOCATION SHOWING INTEGRATED MASS FLOW RATE (OX+FUEL) EQUAL TO MEASURED FLOW RATE

RADIAL POSITION	=	.4337
INTEGRATED MIXTURE RATIO	=	4.2966
INTEGRATED OX FLOW RATE	=	.0266
INTEGRATED FUEL FLOW RATE	=	.0067
MIXING COEFFICIENT	=	97.61
ETAM	=	95.90
PERCENT NOMINAL CSTAR	=	99.92





$$\frac{1}{11} = \frac{20}{220} = \frac{1}{11}$$
$$\frac{1}{\%} \quad \frac{1}{\%}$$

Test No.	Run No.	Base Elem.	Elem. Variations	File	Alt/A.	T <sub>0</sub>	T <sub>1</sub>	ΔP <sub>12</sub>	ΔP <sub>23</sub>	ΔP <sub>34</sub>	ΔP <sub>45</sub>	ΔP <sub>56</sub>	ΔP <sub>67</sub>	ΔP <sub>78</sub>	ΔP <sub>89</sub>	ΔP <sub>90</sub>	ΔP <sub>91</sub>	ΔP <sub>92</sub>	ΔP <sub>93</sub>	ΔP <sub>94</sub>	ΔP <sub>95</sub>	ΔP <sub>96</sub>	ΔP <sub>97</sub>	ΔP <sub>98</sub>	ΔP <sub>99</sub>	ΔP <sub>100</sub>	ΔP <sub>101</sub>	ΔP <sub>102</sub>	ΔP <sub>103</sub>	ΔP <sub>104</sub>	ΔP <sub>105</sub>	ΔP <sub>106</sub>	ΔP <sub>107</sub>	ΔP <sub>108</sub>	ΔP <sub>109</sub>	ΔP <sub>110</sub>	ΔP <sub>111</sub>	ΔP <sub>112</sub>	ΔP <sub>113</sub>	ΔP <sub>114</sub>	ΔP <sub>115</sub>	ΔP <sub>116</sub>	ΔP <sub>117</sub>	ΔP <sub>118</sub>	ΔP <sub>119</sub>	ΔP <sub>120</sub>	ΔP <sub>121</sub>	ΔP <sub>122</sub>	ΔP <sub>123</sub>	ΔP <sub>124</sub>	ΔP <sub>125</sub>	ΔP <sub>126</sub>	ΔP <sub>127</sub>	ΔP <sub>128</sub>	ΔP <sub>129</sub>	ΔP <sub>130</sub>	ΔP <sub>131</sub>	ΔP <sub>132</sub>	ΔP <sub>133</sub>	ΔP <sub>134</sub>	ΔP <sub>135</sub>	ΔP <sub>136</sub>	ΔP <sub>137</sub>	ΔP <sub>138</sub>	ΔP <sub>139</sub>	ΔP <sub>140</sub>	ΔP <sub>141</sub>	ΔP <sub>142</sub>	ΔP <sub>143</sub>	ΔP <sub>144</sub>	ΔP <sub>145</sub>	ΔP <sub>146</sub>	ΔP <sub>147</sub>	ΔP <sub>148</sub>	ΔP <sub>149</sub>	ΔP <sub>150</sub>	ΔP <sub>151</sub>	ΔP <sub>152</sub>	ΔP <sub>153</sub>	ΔP <sub>154</sub>	ΔP <sub>155</sub>	ΔP <sub>156</sub>	ΔP <sub>157</sub>	ΔP <sub>158</sub>	ΔP <sub>159</sub>	ΔP <sub>160</sub>	ΔP <sub>161</sub>	ΔP <sub>162</sub>	ΔP <sub>163</sub>	ΔP <sub>164</sub>	ΔP <sub>165</sub>	ΔP <sub>166</sub>	ΔP <sub>167</sub>	ΔP <sub>168</sub>	ΔP <sub>169</sub>	ΔP <sub>170</sub>	ΔP <sub>171</sub>	ΔP <sub>172</sub>	ΔP <sub>173</sub>	ΔP <sub>174</sub>	ΔP <sub>175</sub>	ΔP <sub>176</sub>	ΔP <sub>177</sub>	ΔP <sub>178</sub>	ΔP <sub>179</sub>	ΔP <sub>180</sub>	ΔP <sub>181</sub>	ΔP <sub>182</sub>	ΔP <sub>183</sub>	ΔP <sub>184</sub>	ΔP <sub>185</sub>	ΔP <sub>186</sub>	ΔP <sub>187</sub>	ΔP <sub>188</sub>	ΔP <sub>189</sub>	ΔP <sub>190</sub>	ΔP <sub>191</sub>	ΔP <sub>192</sub>	ΔP <sub>193</sub>	ΔP <sub>194</sub>	ΔP <sub>195</sub>	ΔP <sub>196</sub>	ΔP <sub>197</sub>	ΔP <sub>198</sub>	ΔP <sub>199</sub>	ΔP <sub>200</sub>	ΔP <sub>201</sub>	ΔP <sub>202</sub>	ΔP <sub>203</sub>	ΔP <sub>204</sub>	ΔP <sub>205</sub>	ΔP <sub>206</sub>	ΔP <sub>207</sub>	ΔP <sub>208</sub>	ΔP <sub>209</sub>	ΔP <sub>210</sub>	ΔP <sub>211</sub>	ΔP <sub>212</sub>	ΔP <sub>213</sub>	ΔP <sub>214</sub>	ΔP <sub>215</sub>	ΔP <sub>216</sub>	ΔP <sub>217</sub>	ΔP <sub>218</sub>	ΔP <sub>219</sub>	ΔP <sub>220</sub>	ΔP <sub>221</sub>	ΔP <sub>222</sub>	ΔP <sub>223</sub>	ΔP <sub>224</sub>	ΔP <sub>225</sub>	ΔP <sub>226</sub>	ΔP <sub>227</sub>	ΔP <sub>228</sub>	ΔP <sub>229</sub>	ΔP <sub>230</sub>	ΔP <sub>231</sub>	ΔP <sub>232</sub>	ΔP <sub>233</sub>	ΔP <sub>234</sub>	ΔP <sub>235</sub>	ΔP <sub>236</sub>	ΔP <sub>237</sub>	ΔP <sub>238</sub>	ΔP <sub>239</sub>	ΔP <sub>240</sub>	ΔP <sub>241</sub>	ΔP <sub>242</sub>	ΔP <sub>243</sub>	ΔP <sub>244</sub>	ΔP <sub>245</sub>	ΔP <sub>246</sub>	ΔP <sub>247</sub>	ΔP <sub>248</sub>	ΔP <sub>249</sub>	ΔP <sub>250</sub>	ΔP <sub>251</sub>	ΔP <sub>252</sub>	ΔP <sub>253</sub>	ΔP <sub>254</sub>	ΔP <sub>255</sub>	ΔP <sub>256</sub>	ΔP <sub>257</sub>	ΔP <sub>258</sub>	ΔP <sub>259</sub>	ΔP <sub>260</sub>	ΔP <sub>261</sub>	ΔP <sub>262</sub>	ΔP <sub>263</sub>	ΔP <sub>264</sub>	ΔP <sub>265</sub>	ΔP <sub>266</sub>	ΔP <sub>267</sub>	ΔP <sub>268</sub>	ΔP <sub>269</sub>	ΔP <sub>270</sub>	ΔP <sub>271</sub>	ΔP <sub>272</sub>	ΔP <sub>273</sub>	ΔP <sub>274</sub>	ΔP <sub>275</sub>	ΔP <sub>276</sub>	ΔP <sub>277</sub>	ΔP <sub>278</sub>	ΔP <sub>279</sub>	ΔP <sub>280</sub>	ΔP <sub>281</sub>	ΔP <sub>282</sub>	ΔP <sub>283</sub>	ΔP <sub>284</sub>	ΔP <sub>285</sub>	ΔP <sub>286</sub>	ΔP <sub>287</sub>	ΔP <sub>288</sub>	ΔP <sub>289</sub>	ΔP <sub>290</sub>	ΔP <sub>291</sub>	ΔP <sub>292</sub>	ΔP <sub>293</sub>	ΔP <sub>294</sub>	ΔP <sub>295</sub>	ΔP <sub>296</sub>	ΔP <sub>297</sub>	ΔP <sub>298</sub>	ΔP <sub>299</sub>	ΔP <sub>300</sub>	ΔP <sub>301</sub>	ΔP <sub>302</sub>	ΔP <sub>303</sub>	ΔP <sub>304</sub>	ΔP <sub>305</sub>	ΔP <sub>306</sub>	ΔP <sub>307</sub>	ΔP <sub>308</sub>	ΔP <sub>309</sub>	ΔP <sub>310</sub>	ΔP <sub>311</sub>	ΔP <sub>312</sub>	ΔP <sub>313</sub>	ΔP <sub>314</sub>	ΔP <sub>315</sub>	ΔP <sub>316</sub>	ΔP <sub>317</sub>	ΔP <sub>318</sub>	ΔP <sub>319</sub>	ΔP <sub>320</sub>	ΔP <sub>321</sub>	ΔP <sub>322</sub>	ΔP <sub>323</sub>	ΔP <sub>324</sub>	ΔP <sub>325</sub>	ΔP <sub>326</sub>	ΔP <sub>327</sub>	ΔP <sub>328</sub>	ΔP <sub>329</sub>	ΔP <sub>330</sub>	ΔP <sub>331</sub>	ΔP <sub>332</sub>	ΔP <sub>333</sub> </
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$$\frac{w_c}{11} \approx 0.07\%$$
[illegible]

Fuel Man: All  
 Pressure Error  
 on These Tests

FIG 4  
SNT 6 OF 11

TEST	RUN	ELOM	VELOCITY	FILE	AC/A	T <sub>0</sub>	T <sub>E</sub>	ΔP <sub>02</sub>	ΔP <sub>03</sub>	Norm. $\Delta P_{02}$	Norm. $\Delta P_{03}$	V <sub>E</sub> /V <sub>0</sub>	4/D	O/F	R	(V/F) <sub>E</sub>	E <sub>m</sub>	7 <sub>m</sub>	%C*
78.1	139	DUPLICATE	0°	15	1.00	509	525	10.81	6.66	.88	.58	3.56	3.1	4.03	.624	5.24	70.7	61.3	15.38
78.2	140	90° C.C.W.											3.1						
79.1	141	0°																	
79.2	142	90° C.C.W.																	
80.1	143	0°																	
80.2	144	90° C.C.W.																	
81.1	145	0°																	
81.2	146	90° C.C.W.																	
82.11	147	0°																	
82.12	148	0°																	
82.2	149	90° C.C.W.																	
83.2	150	90° C.C.W.																	
83.1	151	0°																	
84.11	152	0°																	
84.12	153	0°																	
84.13	154	0°																	
85.1	155	.050° SUMMA	0°																
85.2	156	90° C.C.W.																	
85.4	157	90° C.C.W.																	
85.3	158	0°																	
85.5	159	0°																	
85.6	160	90° C.C.W.																	
86	95	FLAT "I" TRIPLET		3	1.01	538	541	48.60	45.18	0.88	0.88	3.49	15	3.96	.75	5.01	82.0	71.8	98.42
87	96																		
88	99																		
Missing Cold Test - Not Recorded on Tape @ Aerophysics Lab																			
508	525	9.99	8.47	.92	.58	3.64	7	3.95	.750	5.05	85.5	76.0	98.85						
507	525	10.18	7.35	.92	.58	3.64	15	3.95	.750	4.75	95.5	91.6	98.88						
506	525	10.35	9.32	.92	.58	3.64	30	3.96	.750	4.55	97.8	95.7	99.48						
512	525	7.20	21.66	8.67	.58	7.23	7	1.97	.25	3.85	82.6	72.3	97.52						
501	525	13.61	5.68	.36	.58	2.29	7	6.36	.75	7.52	86.5	79.2	99.75						
506	525	12.89	11.40	.92	.58	3.65	7	3.96	.75	5.01	82.0	71.8	98.42						
506	525	9.86	30.80	8.68	.58	7.29	7	1.98	.375	3.32	82.3	72.8	97.85						
497	525	16.04	5.50	.86	.58	2.29	7	6.41	.541	8.29	85.6	78.2	100.02						
210.8	182.0	18.81	22.09	0.73	0.73	2.95	15	4.03	.541	7.0	2.72	2.14	296						
533	544	75.15	37.95	0.89	0.89	3.53	15	3.98	.249	4.58	98.1	97.4	99.96						

NOTE: TEST 87 DISTRIBUTION IS APPROXIMATE 1/2 PLATE ON TEST.

SHY 20F11

TEST	RUN	ELEM	VAC	F/E	AIR/A <sub>0</sub>	T <sub>0</sub>	P/S	ΔP/S	WATER VOLUME IN. MIN	U/D	O/F	R	(O/F) <sub>S</sub>	E <sub>m</sub>	η <sub>m</sub>	% C <sup>2</sup>			
* 89	100	FLAT "I" TAPER	67%	↓	0.99	517	535	41.91	36.22	0.95	0.95	3.73	7	3.91	.604	4.98	95.3	91.7	99.92
* 90	101			↓		510	531	43.74	37.99	0.94	0.94	3.70	3	3.96	.517	4.16	90.2	87.2	100.33
* 91	104			↓	1.01	480	518	34.94	31.33	0.98	0.98	3.82	3	3.89	.552	5.09	85.1	80.6	99.48
* 92	106			↓	0.98	503	528	37.99	34.79	0.95	0.95	3.76	7	3.95	.575	4.70	92.6	88.8	99.79
93	107		67%	↓	0.51	490	530	34.28	43.45	2.06	2.06	7.82	3	3.86	.611	5.99	89.6	85.1	99.79
* 94	105			↓	1.01	482	518	34.27	30.89	1.03	1.03	3.91	7	3.79	.481	4.56	97.1	95.9	99.96
* 95	103	PAINTED		↓	0.98	503	528	37.99	34.79	0.95	0.95	3.76	7	3.95	.575	4.70	92.6	88.8	99.79
* 96	102			↓		513	533	38.65	35.55	0.94	0.94	3.72	3	3.96	.506	4.20	90.3	87.5	100.26
* 97	98		34%	↓	1.00	522	539	58.94	45.33	0.91	0.91	3.61	15	3.98	.290	4.69	98.6	97.9	100.01
98	97			↓	2.04	517	535	41.91	36.22	0.95	0.95	3.73	7	3.91	.604	4.98	95.3	91.7	99.92
TEST 98 DATA INDICATES TWO PHASE OUTLET DISTRIBUTION; MIXING EFFICIENCY DATA REVEALS MEASUREMENTS																			
99	107	Co-Ax	SHEAR	↓	2.01	524	531	12.33	1.47	.45	0.00	1.77	15	3.96	.44	5.00	85.1	80.6	99.48
100	109		4 Hole Swirler	↓		521	526	16.19	1.59	.44	.28	1.76	15	3.98	.575	4.18	72.0	66.1	96.32
101	108		2 Hole Swirler	↓		524	529	19.10	1.70	.44	.59	1.76	15	3.97	.625	4.35	87.7	81.2	99.73
102	110		Increased Swirl	↓	2.87	520	525	17.14	2.16	0.32	0.00	1.25	15	3.90	.625	4.31	91.6	86.8	99.89
* 103	111		SHEAR	↓	0.99	483	519	7.03	5.56	1.03	0.00	3.93	7	3.92	.658	4.41	74.0	67.7	96.12
* 104	112			↓		481	518	7.30	5.83	1.02	0.00	3.92	3	3.84	.633	5.99	89.5	85.0	95.98
* 105	113			↓		395	425	7.05	5.21	1.00	0.00	3.89	3	3.87	.726	4.96	50.9	57.7	87.25
* 106	116		3' Hole Swirler	↓		479	515	25.20	8.13	1.01		3.90	7	3.85	.750	4.10	94.3	90.0	99.78

FIG 4  
SUT 8 OF 11

SHT 8 OF 11

TEST RUN	Elem	VAR	F/E	A/L/A	T <sub>0</sub>	T <sub>1</sub>	ΔP <sub>05</sub>	ΔP <sub>45</sub>	WAVELENGTH	WAVELENGTH	WAVELENGTH	W/D	O/F	R	(O/F) <sub>5</sub>	E <sub>m</sub>	η <sub>m</sub>	%C*
Q	107	115	Co-Ax	3 Hrs	515	515	26.43	8.03	0.98	3.83	3	3.92	.750	.750	5.44	94.5	89.8	99.87
Q	108	114			428.5 (508)	428.5 (421.5)	21.53	5.61	1.08	4.05	3	3.74	.660	.660	6.04	93.2	87.8	99.67
Q	109	117			525	525	11.55	8.58	0.98	3.68	7	3.77	.745	.745	6.12	82.0	76.6	98.36
Q	110	118									3							
(No Data Available)																		
*	111	122	TRIPLET	60° Imp.	524	524	11.12	4.84	0.96	3.83	3	3.98	.358	.358	4.61	65.0	62.7	94.12
*	112	123			497	522	10.79	4.65	0.97	3.85	7	3.97	.678	.678	5.37	82.4	72.6	98.58
*	113	124			495	522	10.87	4.78	0.96	3.84	15	3.99	.716	.716	4.59	95.0	90.8	99.93
*	114	125			496	522	10.48	4.61	0.96	3.83	30	3.99	.375	.375	4.80	98.9	98.2	99.99
*	115	126			503	522	7.80	10.08	3.80	0.44	7.57	7	1.99	.631	2.34	86.2	78.4	98.84
*	116	127			487	519	13.56	2.95	0.38	0.14	2.41	7	6.42	.314	6.68	77.3	69.6	99.02
*	117	128			279.1	289.9	6.46	2.70	1.14	0.29	4.15	7	3.64	.643	4.41	78.1	67.5	98.31
*	118	136			488	516	10.33	8.23	0.97	0.20	3.95	7	5.99	.750	5.55	57.9	49.3	93.59
*	119	134			488	513	10.40	8.70	0.98	0.20	3.87	3	3.96	.668	6.34	63.3	50.7	93.35
*	120	135			483	514	12.90	4.90	0.37	0.11	2.40	3	6.44	.375	9.01	59.1	45.7	94.42
*	121	133			497	515	7.39	20.23	3.81	0.32	7.57	3	1.99	.631	2.34	86.2	78.4	98.84
*	122	129			495	518	9.92	10.99	0.97	0.41	3.84	7	3.96	.750	5.55	57.9	49.3	93.59
*	123	130			492	516	9.97	10.76	0.98	0.41	3.86	3	3.95	.668	6.34	63.3	50.7	93.35
Q	124	132			485	514	11.96	6.35	0.38	0.21	2.41	3	6.38	.375	8.84	73.7	70.5	99.98
Q	125	131			496	515	7.69	23.59	3.85	0.73	7.62	3	1.98	.631	2.34	86.2	78.4	98.84



SHT 9 OF 11

TEST	RUN	ELEM	VAR	F/E	A/A <sub>0</sub>	T <sub>f</sub>	ΔP <sub>TS</sub>	ΔP <sub>TS</sub>	Wt % H <sub>2</sub> O	W/D	O/F	R	(O/F) <sub>S</sub>	E <sub>m</sub>	η <sub>m</sub>	%C <sup>a</sup>			
126	175	TRIPLET	60°/MP	3	1.02	515	→	10.29	6.92	0.89	0.25	3.54	15	3.98	.252	4.58	97.9	97.2	99.44
127	176	↓	↓	↓	↓	197	(Cold Propellant Test - 2 Phase Ox)	→	→	→	→	→	15	4.03	(Data Not Applicable)	→	→	→	
128	177	↓	↓	↓	↓	503	→	10.38	18.89	2.51	0.40	6.02	15	2.40	.316	2.98	92.2	88.4	99.55
129	173	↓	↓	↓	↓	521	→	5.47	105.07	7.17	0.50	14.18	15	1.98	.249	2.27	97.8	97.0	99.99
130	174	↓	↓	↓	↓	519	→	9.84	20.05	.79	.23	4.69	15	5.96	.266	6.95	93.2	90.2	99.59
* 131	121	FLAT "I" TRIPLET	→	→	2.02	519	→	38.59	27.03	0.45	0.45	1.77	15	3.98	.630	4.64	95.6	92.8	100.01
132	168	↓	↓	↓	↓	486	→	35.77	27.30	0.57	.57	1.97	3	3.83	.486	4.73	88.9	83.5	99.43
133	167	↓	↓	↓	↓	492	→	54.41	51.94	1.95	1.95	3.79	3	1.94	.381	2.68	89.2	85.2	99.46
134	169	↓	↓	↓	↓	485	→	27.66	16.67	.23	.23	1.31	3	5.77	.720	6.50	84.0	74.8	99.00
* 135	119	FLAT "I" TRIPLET - 34%	→	→	2.02	529	→	40.52	32.67	0.46	0.46	1.78	15	5.90	.278	4.32	98.9	98.2	99.97
* 136	120	PENTAD 34%	→	→	↓	520	→	47.30	36.57	0.44	0.44	1.76	15	3.99	.249	4.73	99.1	98.4	100.04
137	170	↓	↓	↓	↓	50	→	35.30	60.77	2.02	2.02	7.74	3	3.84	.682	5.36	90.0	85.7	98.52
(138 Missing)																			
139	214	TRIPLET	45°/MP	→	0.50	483	→	10.60	22.91	2.03	.27	7.73	4.9	3.81	.621	4.81	91.0	86.1	99.80
140	204	↓	↓	↓	↓	479	→	9.03	→	→	→	→	3	3.83	.240	3.88	83.4	81.1	97.06
240	205	↓	↓	↓	↓	482	→	9.02	25.05	2.03	.37	7.78	7	3.84	.594	4.64	96.2	93.0	99.87
340	206	↓	↓	↓	↓	479	→	8.97	24.50	2.01	.37	7.77	4.9	3.86	.435	4.49	90.8	85.7	99.21
141	216	↓	↓	↓	↓	481	→	7.37	38.07	4.99	.78	12.44	4.9	2.49	.393	3.48	83.8	76.2	97.87
142	210	↓	↓	↓	↓	484	→	9.56	22.40	2.13	.60	8.10	4.9	3.80	.427	5.22	84.0	75.9	97.70
143	212	↓	↓	↓	↓	477	→	9.90	14.66	1.34	.49	6.46	4.9	4.83	.441	6.96	85.2	77.3	98.37

FIG. 4  
SWT 10 OF 11

SWT 10 OF 11

TEST	RUN	Elem	VAR	F/E	Ac/A <sub>0</sub>	T <sub>0</sub>	T <sub>F</sub>	ΔP <sub>0.5</sub>	ΔP <sub>2.5</sub>	W <sub>2</sub> W <sub>1</sub> ΔP <sub>0.5</sub>	W <sub>2</sub> W <sub>1</sub> ΔP <sub>0.5</sub>	LD	O/F	$\bar{E}$	(O/F) <sub>2</sub>	E <sub>m</sub>	$\eta_m$	%C <sup>+</sup>		
(145)	144	213	TRIPLET	60°/mp	50	0.96	481	508	9.82	6.36	1.06	.28	4.01	4.9	3.80	.585	4.57	97.2	95.7	99.97
	146	207				2.00	486	511	9.55	3.81	.50	.17	1.92	4.9	3.86	.697	4.78	93.2	88.3	99.83
	147	208				481	509	7.93	8.45	1.33	.31	3.13	4.9	2.35	.715	3.21	92.3	86.5	98.93	
	148	209				476	510	10.50	1.31	.22	.092	1.28	4.9	5.83	.653	6.72	78.6	69.6	98.48	
149	178	TRIPLET	60°/mp	3	2.00	505	536	7.67	2.10	.47	.13	1.86	1.5	3.93	.270	4.93	94.2	92.1	99.99	
151	223					511	523	13.23	1.04	.46	.16	1.80	7	3.95	.250	4.70	83.3	79.3	98.74	
152	222					512	526	10.55	2.69	1.46	.32	3.23	7	2.21	.367	2.57	95.1	91.7	99.75	
153	221					508	521	13.64	?	.26	.086	1.20	7	5.96	.580	6.90	75.0	73.7	101.91	
TEST → 154 192 Co-Ax SUEAR 50 1.98 16.5 (No Data)																				
*	254	193				480	513	8.96	3.09	0.49	0.00	1.93	3	3.90	.750	4.50	41.2	42.0	80.01	
*	354	194				481	514	9.23	3.39	0.60	0.00	1.95	3	3.86	.750	4.84	49.1	47.7	83.14	
	454	195				482	513	9.22	3.29	.51	0.00	1.95	3	3.84	.363	3.77	41.8	49.6	77.62	
*	155	196				483	512	7.07	5.02	1.23	0.00	3.03	3	2.46	.750	3.21	42.9	40.8	81.10	
*	156	197				479	512	9.70	1.51	.22	0.00	1.29	3	5.83	.750	5.55	47.8	44.5	83.41	
*	157	199				482	510	23.74	2.85	.51	.36	1.94	3	3.84	.576	4.49	94.9	91.5	99.81	
*	158	198				491	512	18.36	4.71	1.14	.37	2.89	3	2.54	.750	1.85	39.1	39.4	85.53	
*	159	200				481	511	25.61	1.29	.22	.73	1.29	3	5.78	.750	7.11	94.1	89.8	99.96	

154 192 Co-Ax Suave 50 1.98

154 193

154 194

154 195

155 196

156 197

157 199

158 198

159 200

3 Hole Suave

(K<sub>W</sub>)

(O<sub>W</sub>)

85% Mass Integration

70% Mass Integration

99% Mass Integration

Sheet 11 of 11

TEST	RUN	ELEM	VAR	F/E	A/R	T <sub>0</sub>	ΔP <sub>3</sub>	ΔP <sub>5</sub>	Wt/Wt <sub>0</sub> W <sub>avg</sub> /W <sub>thm</sub>	L/D	O/F	R̄	(O/F) <sub>5</sub>	Em	γ <sub>m</sub>	%C <sub>5</sub>		
* 160	201	C-Ax	Incandescent Screen	50	2.12	490	510	6.10	4.46	0.94	0.00	2.53	3	2.70	.750	3.91	56.8	87.99
* 260	202					482	510	9.63	5.20	0.46	0.00	1.78	3	3.90	.750	6.27	48.7	86.44
* 360	203					483	510	8.29	1.59	0.23	0.00	1.27	3	5.44	.750	8.62	44.5	85.31
161	179	Flat T	Tuner	33%	15	0.99	510	40.32	37.51	.94	.94	3.70	3	3.93	.750	4.74	55.6	84.4
162	180					506	530	36.71	34.38	.93	.93	3.70	7	3.96	.750	4.54	93.3	90.0
163	181					507	530	36.66	34.24	.93	.93	3.70	15	3.96	.250	3.82	94.9	90.6
164	182					509	530	36.52	33.91	.93	.93	3.68	30	3.96	.750	5.04	95.3	91.1
165	183					515	530	56.37	68.35	3.70	3.70	7	1.97	.749	2.26	92.4	86.5	99.64
965	184					510	530	56.95	69.27	3.68	3.68	3	1.99	.750	1.99	88.8	83.5	95.43
166	185					496	530	32.77	25.28	.36	.36	2.33	3	6.44	.250	6.13	96.6	99.34
168	191	Pentad	33%			502	530	38.94	36.09	.94	.94	3.73	30	3.96	.750	5.70	94.0	89.9
169	189					501	530	39.24	36.28	.94	.94	3.73	7	3.97	.625	4.77	93.0	91.7
170	190					502	530	38.82	35.92	.95	.95	3.74	15	3.95	.750	4.57	98.1	99.99
171	188					499	530	40.33	38.00	.95	.95	3.75	3	3.97	.595	4.21	92.3	88.3
172	187					506	530	58.92	65.85	3.73	3.73	7.40	3	1.98	.375	1.98	93.1	89.5
173	186					506	530	32.56	24.19	.36	.36	2.31	3	6.35	.250	7.57	91.3	89.5

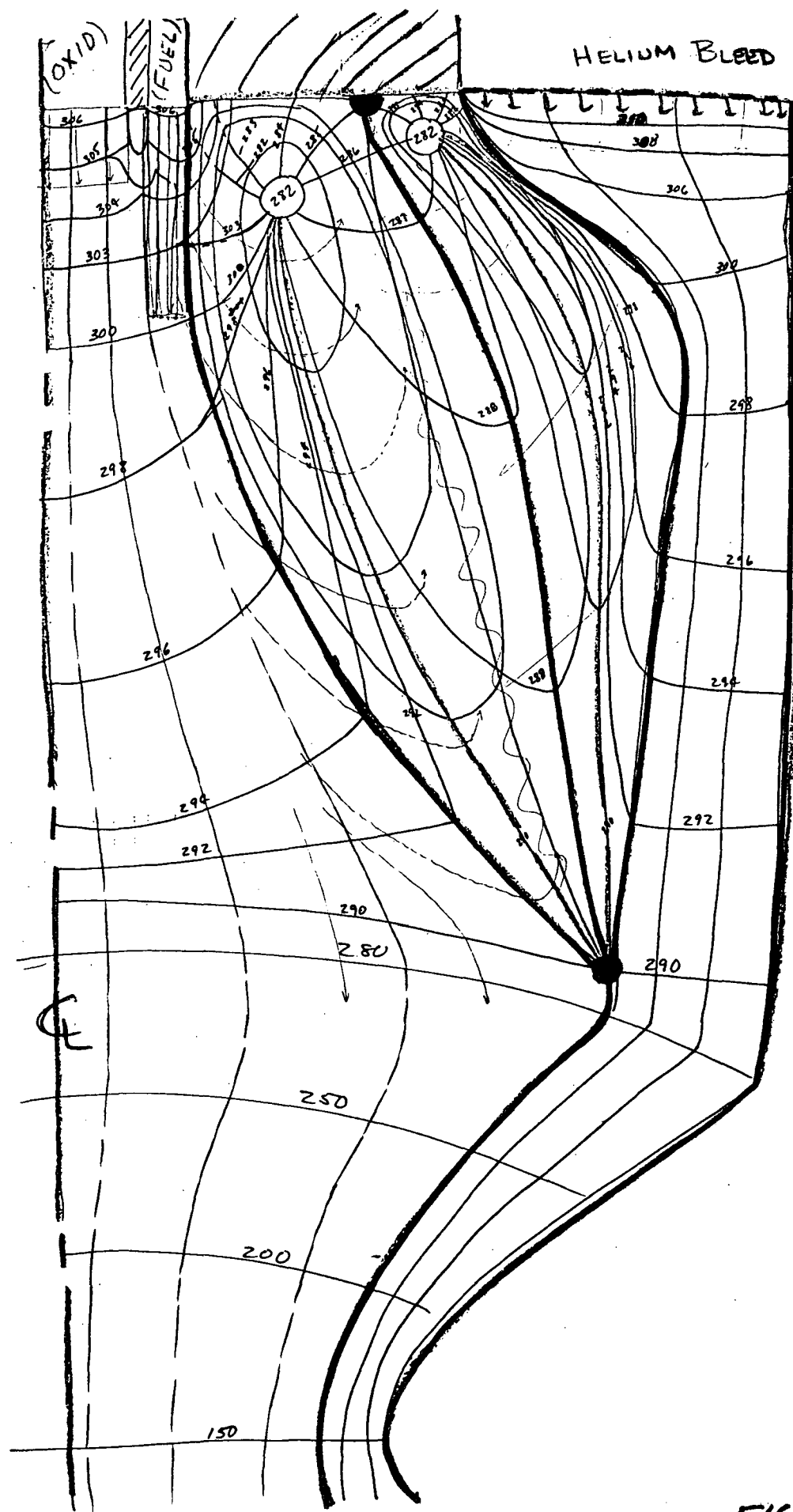
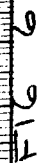


FIG 5



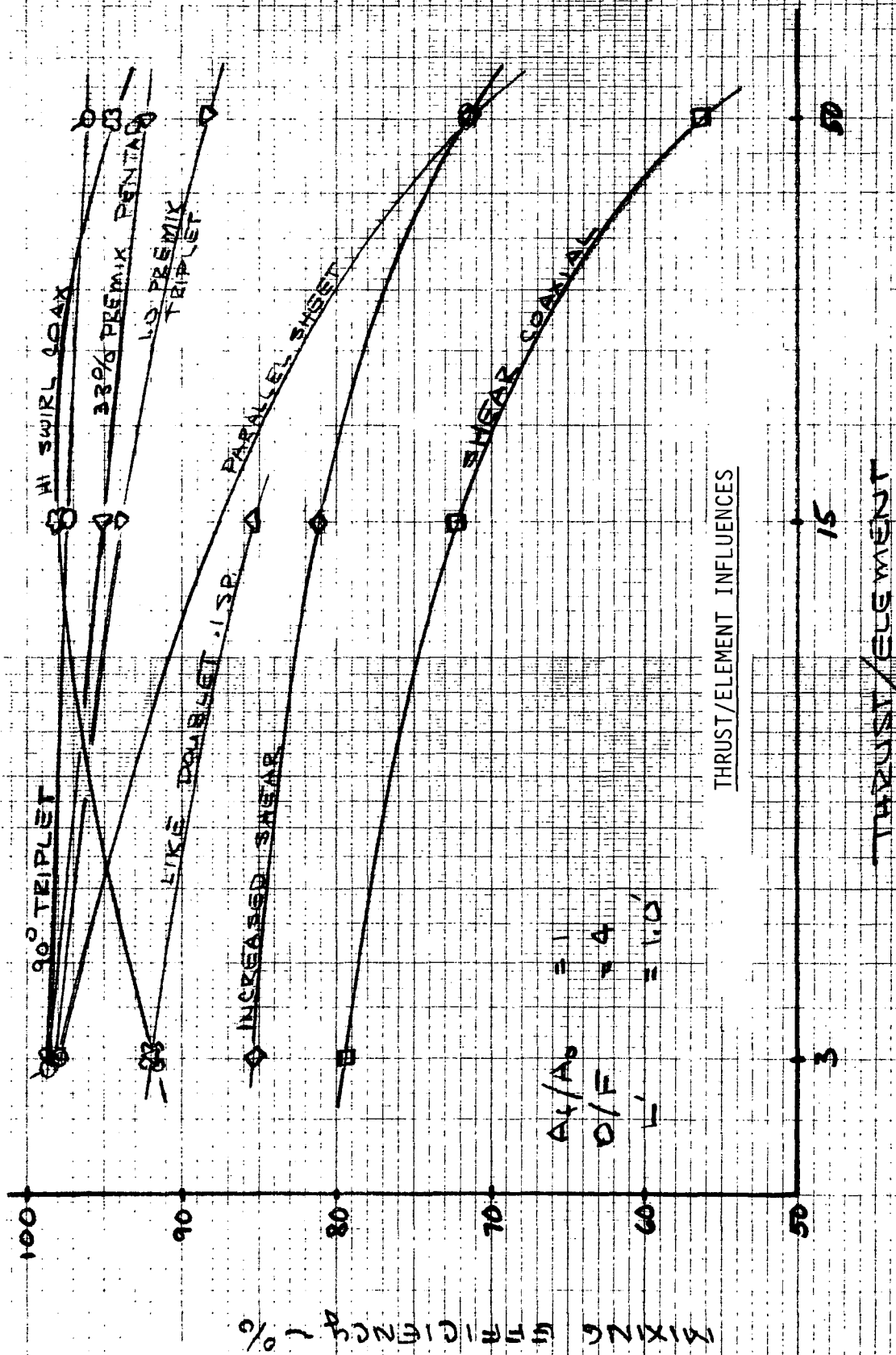


FIG 7

THE EFFECT OF AREA RATIO

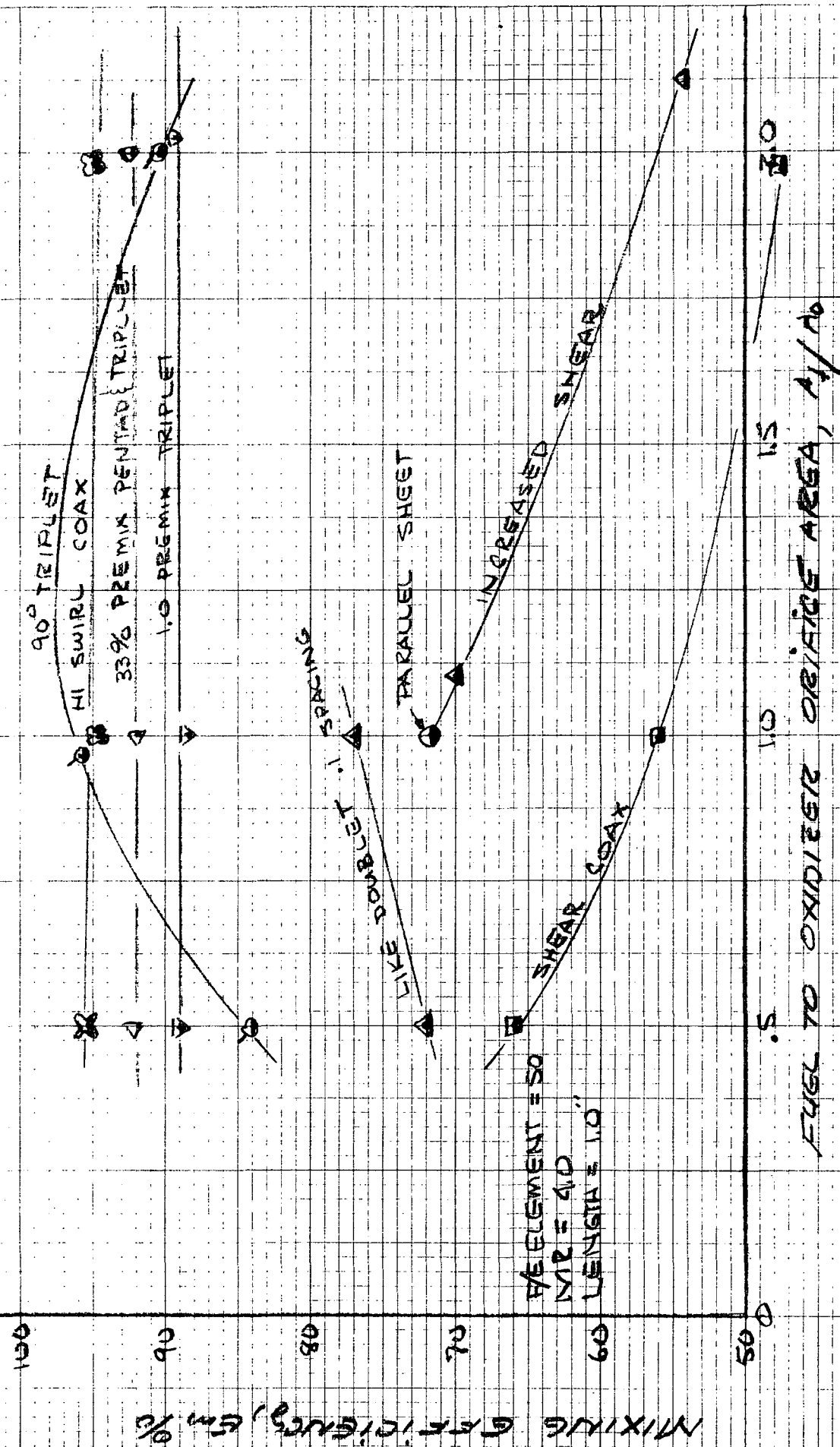


FIG. 8

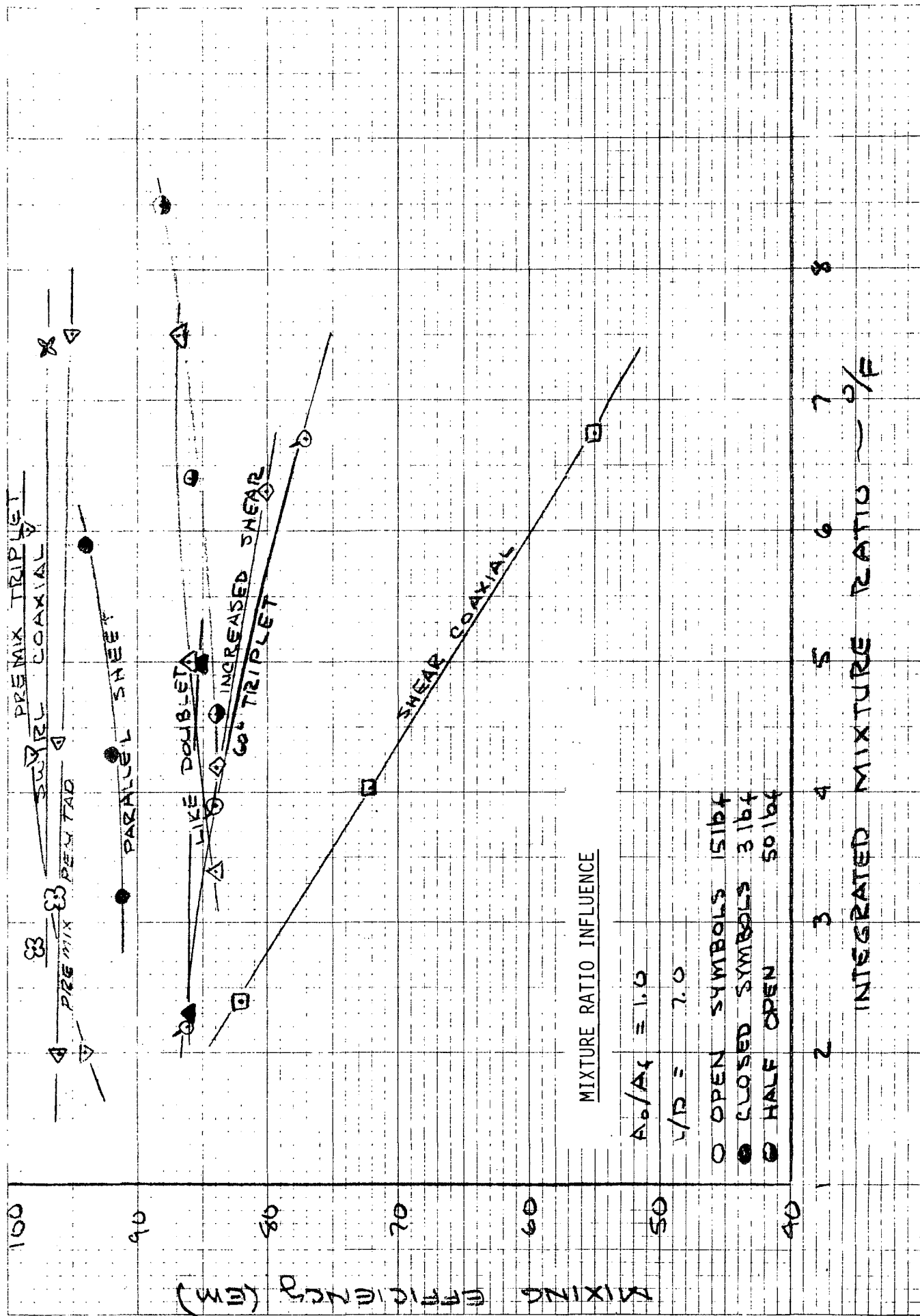


FIG. 9



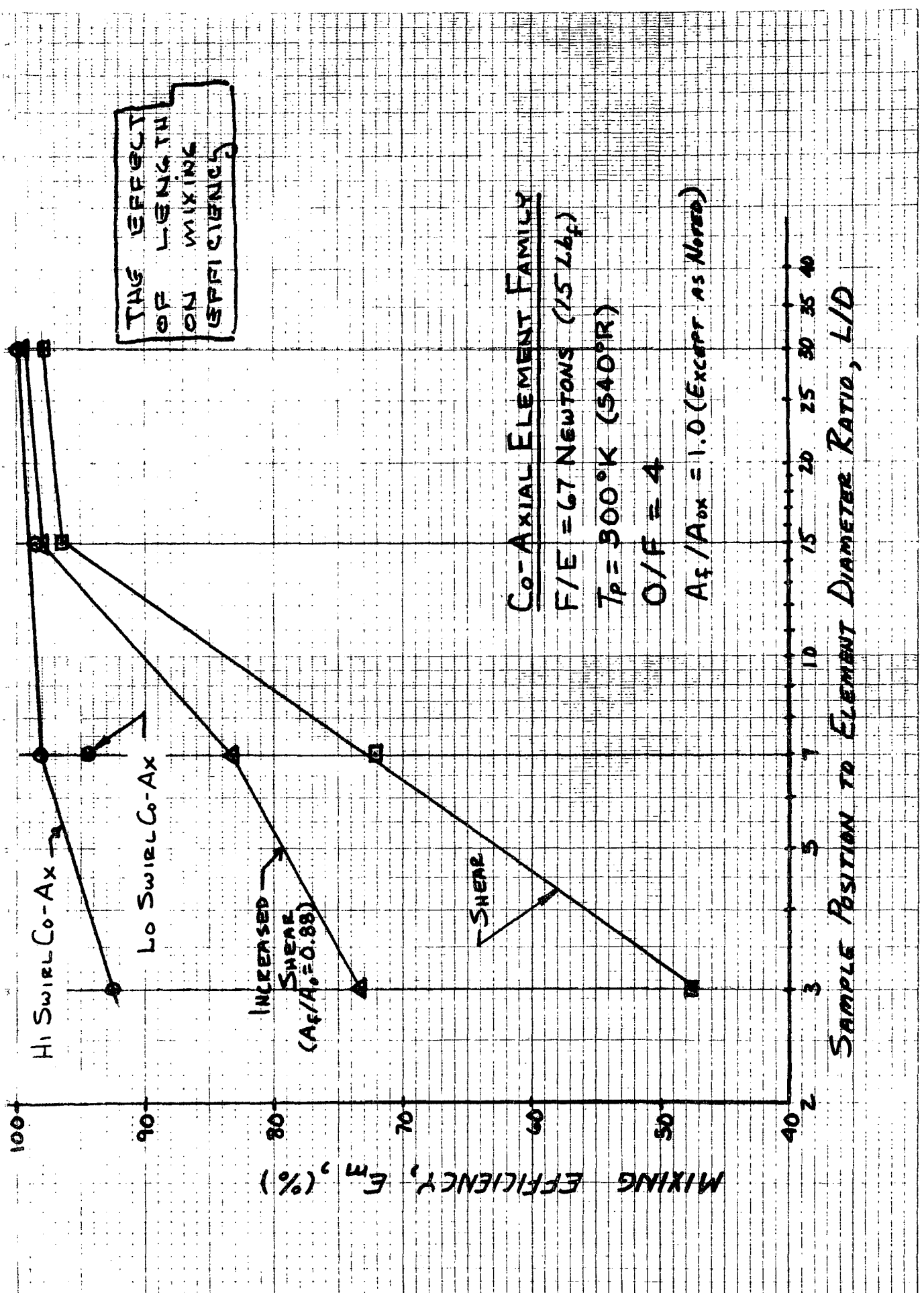


FIG 5

# THE EFFECT OF MIXTURE RATIO ON MIXING EFFICIENCY

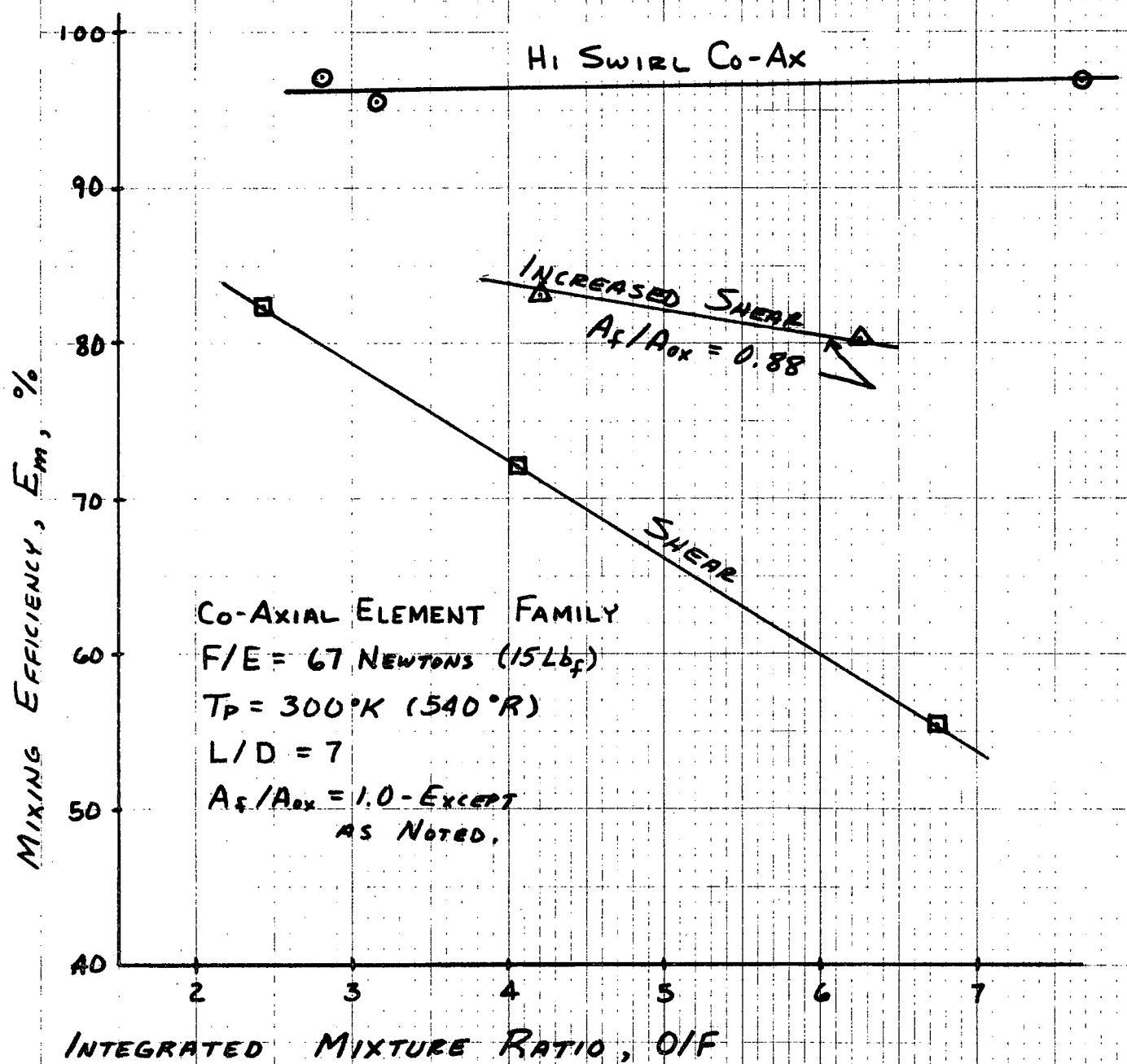
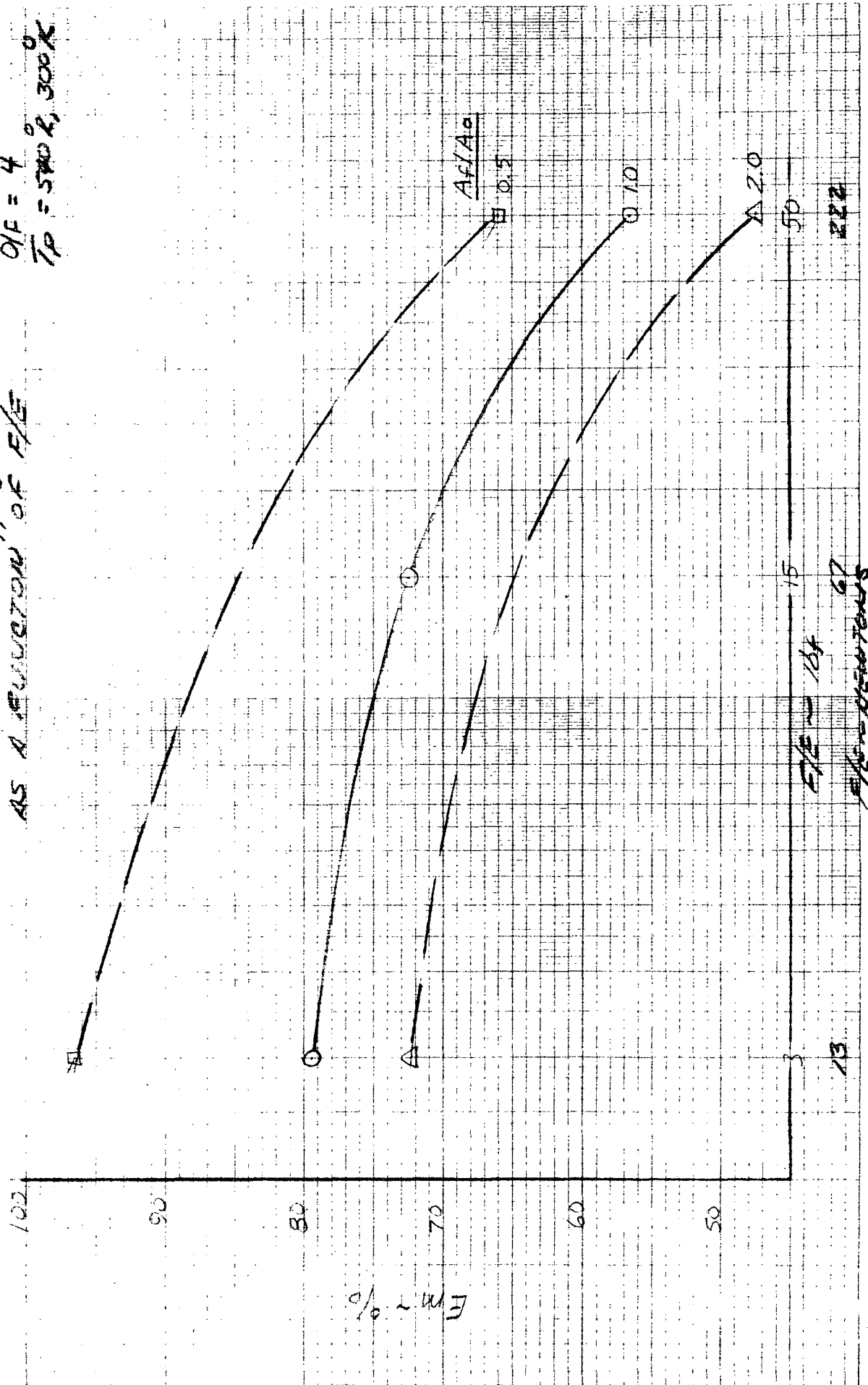


FIG. 7

# COAXIAL

THE EFFECT OF  $A/A_0$   
AS A FUNCTION OF  $F/E$

$L' = 1 \text{ IN, } 258 \text{ CM}$   
 $O/E = 4$   
 $T/P = 5800 \text{ K, } 3000^\circ$



# INCREASED SHEAR COAXIAL

THE EFFECT OF  $A_f/A_0$   
AS A FUNCTION OF  $F/F_0$

$L' = 6.58 \text{ cm.}$   
 $O/F = 4$   
 $T_p = 540^\circ, 300^\circ$

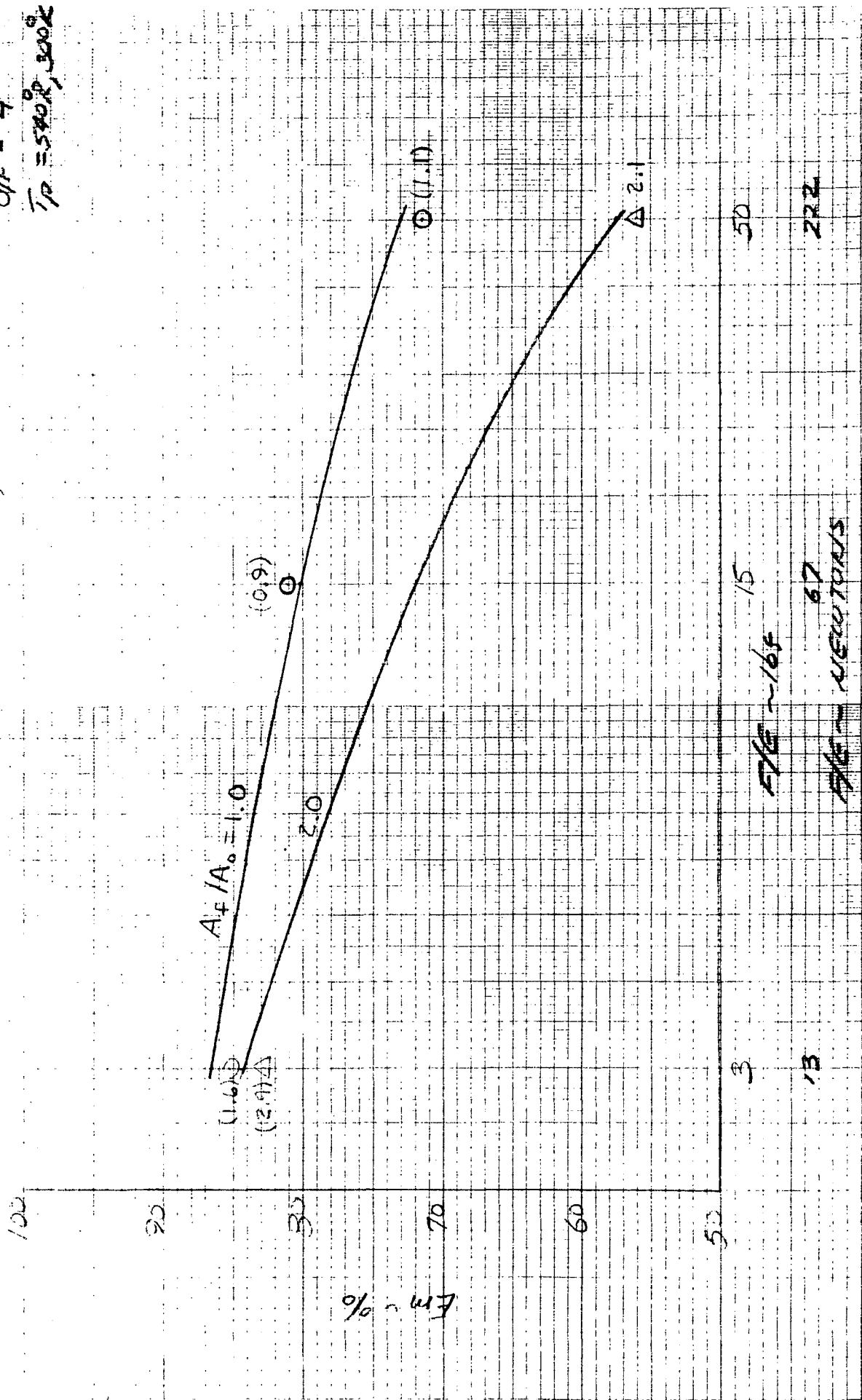
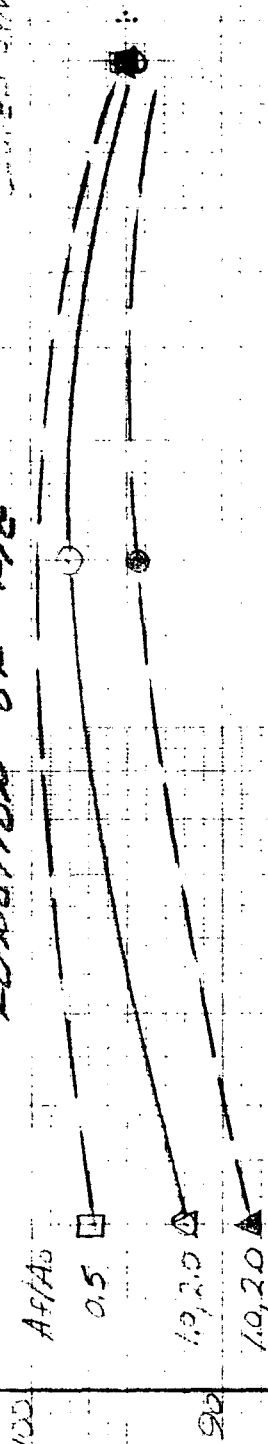


FIG. 13

# SWIRL OXIDIZER COAXIAL

THE EFFECT OF  $A/A_0$  AS A  
FUNCTION OF  $A'/A_0$

OPEN SYMBOL:  $H/V_{SW}$   
CLOSED SYMBOL:  $4.0 V_{SW}$



$A' = 1.0, 2.54 \text{ cm}$   
 $O/F = 4.0$   
 $T_0 = 500^\circ \text{K}, 300^\circ \text{K}$

FIG - 16F

FIG - 16F

FIG. 14

1/2" X 1/2" PER INCH

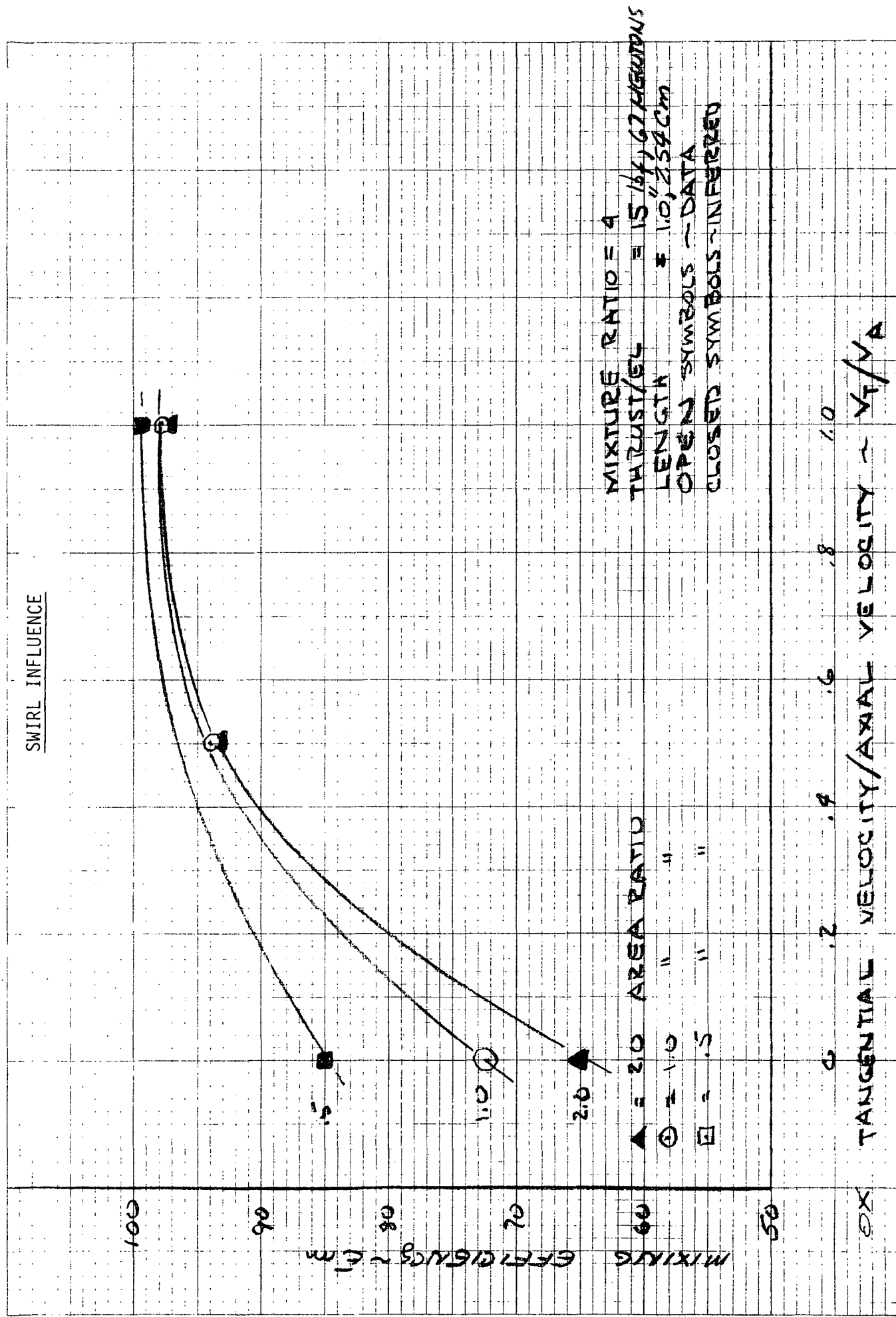


FIG. 15

(°R)

THE EFFECT OF TEMPERATURE  
ON MIXING EFFICIENCY

H1 SWIRL Co-Ax

MEAN PROPELLANT TEMPERATURE  
DEFINED BY  $\bar{T} = [\dot{w}_o C_{p_o} T_{ox} + \dot{w}_f C_{p_f} T_f] / [\dot{w}_o C_{p_o} + \dot{w}_f C_{p_f}]$

MIXING EFFICIENCY,  $\eta_m$ , %

$T_{ox}$

$T_f$

INCREASED SHEAR  
 $A_f/A_{ox} = 0.88$

Co-AXIAL ELEMENT FAMILY

F/E = 67 NEWTONS (15 Lbf)

L/D = 7

O/F = 4

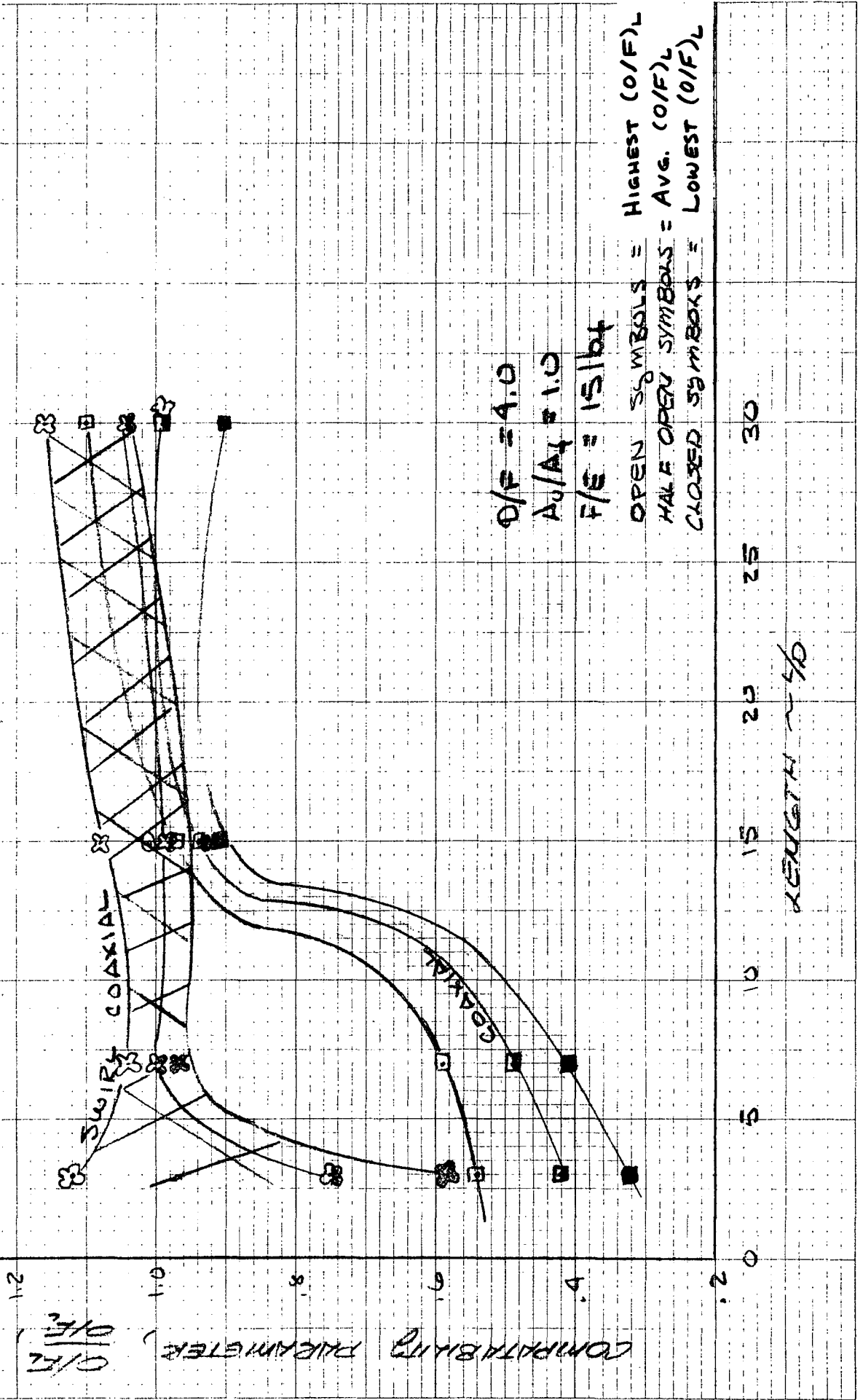
$A_f/A_{ox} = 1.0$  EXCEPT AS NOTED

SHEAR Co-Ax

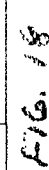
PROPELLANT TEMPERATURE,  $T_p$ , (°K)

FIG 16

# COMPATIBILITY OF SWIRL COAXIAL & COAXIAL CHARACTERISTICS







۱۹۹۹

# COAXIAL ELEMENT COMPATABILITY CHARACTERISTICS

$F/E = 50 \text{ lbf}, 222 \text{ NEWTONS}$

$-P = 3$

$O/F = 4$

OPEN SYMBOL = HIGHEST (O/F)

HALF OPEN SYM = AVG. (O/F)

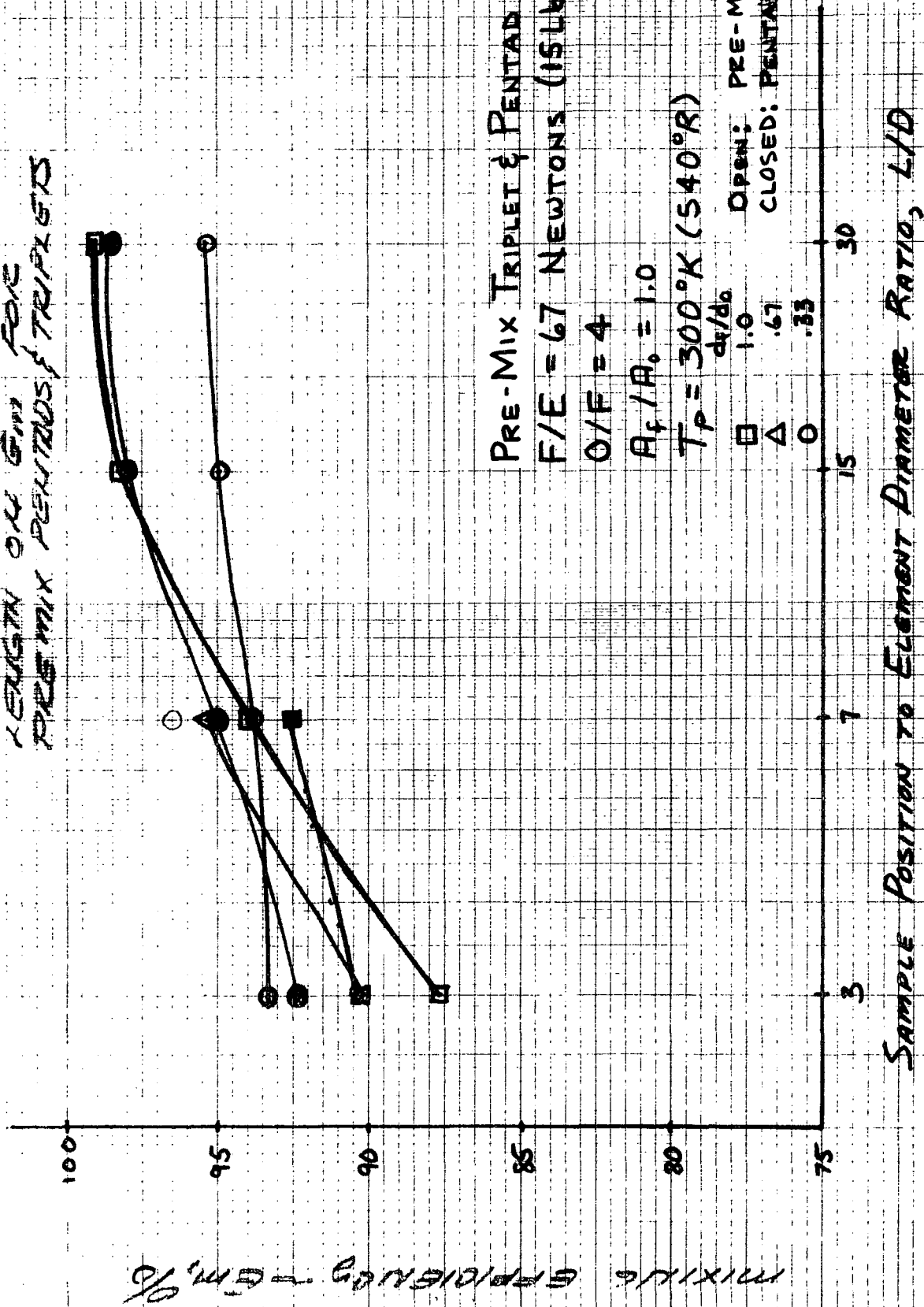
CLOSED SYMBOL = LOWEST (O/F)

COMPATABILITY  
PARAMETER  $C_P$   
 $O/F$

COMPATABILITY  
PARAMETER  $C_P$   
 $O/F$

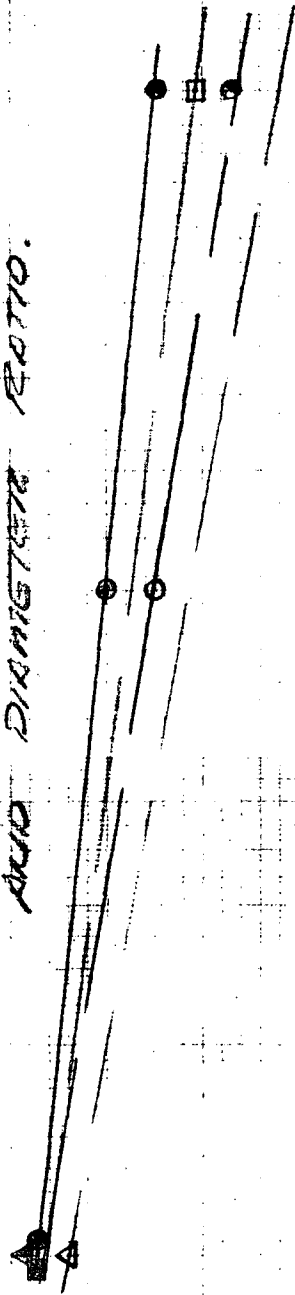
AREA RATIO,  $A_1/A_0$

THE EFFECT OF  
LENGTH ON G<sub>m</sub> FOR  
PREMIX PENTADS & TRIPLETS



PREMIX PENTAD

THE EFFECT OF AREA RATIO  
AND DIAMETER RATIO.



50 - 100

A<sub>2</sub>/A<sub>1</sub>

0.5

1.0

2.0

OPEN SYMBOLS

HALF OPEN

CLOSED SYMBOLS

9/11 = 4

7/2 = 300% - 500%

3

15

50

F/G ~ 16.5

67

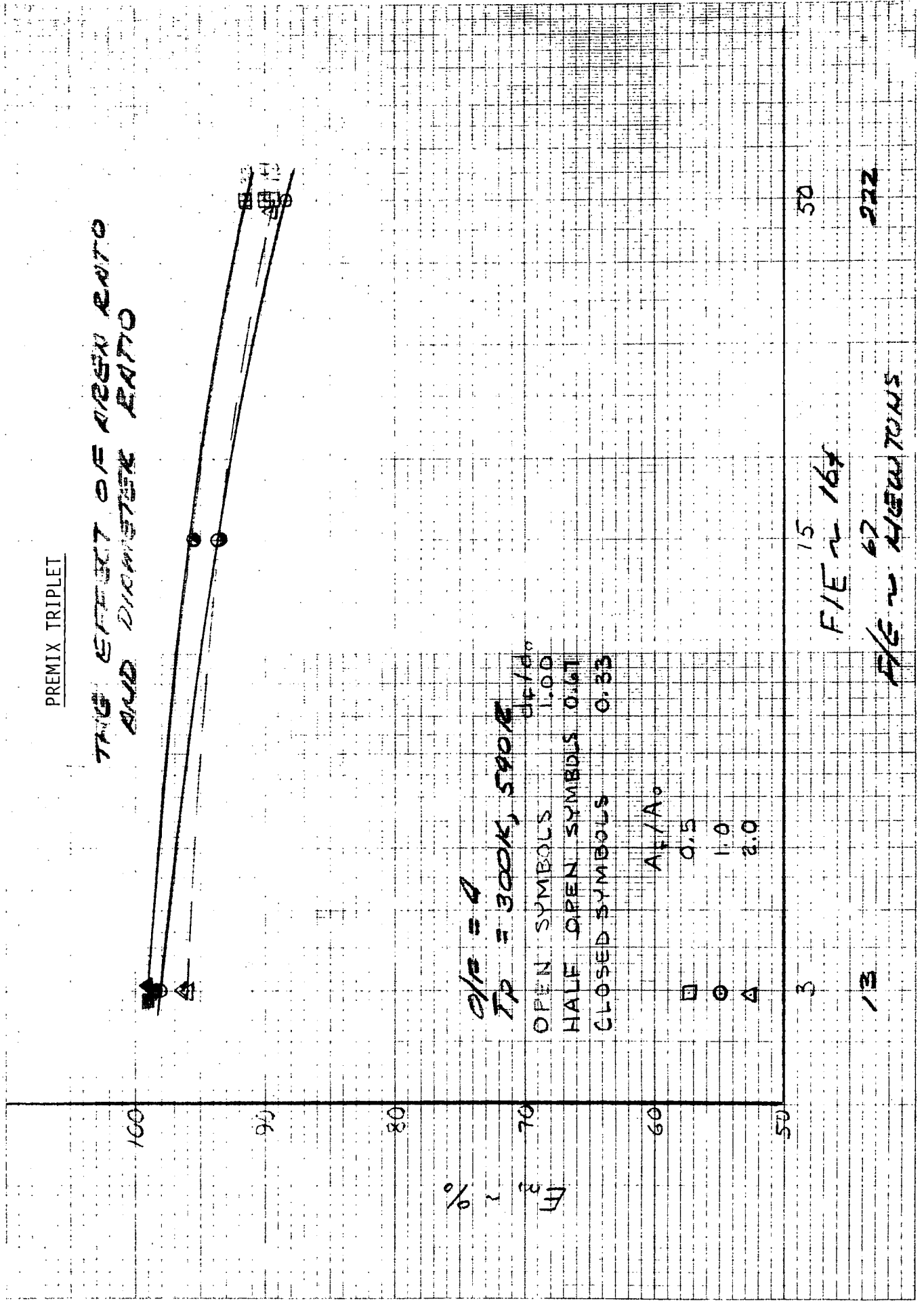
22.2

P/G ~ 1000000

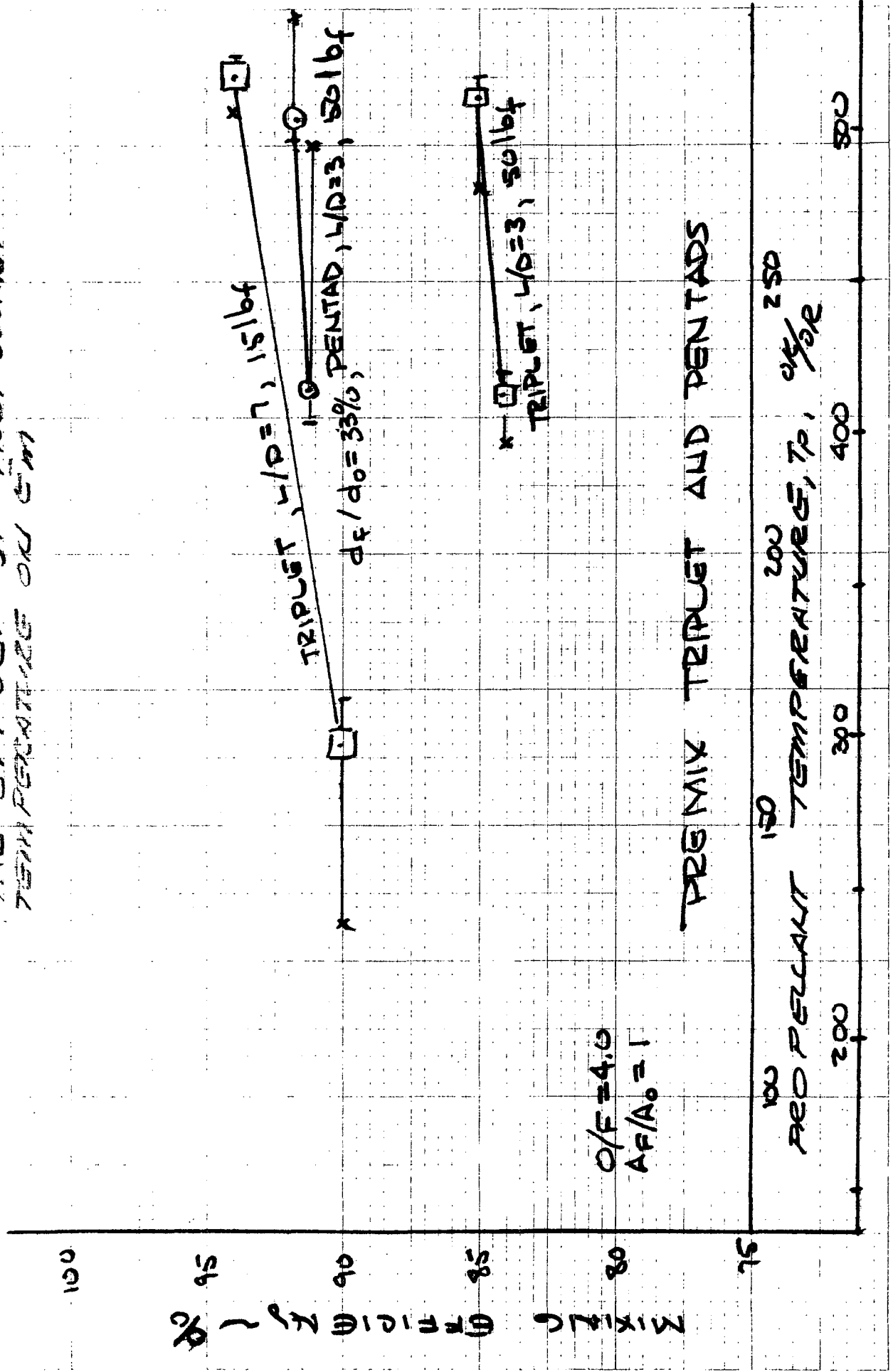
13

PREMIX TRIPLET

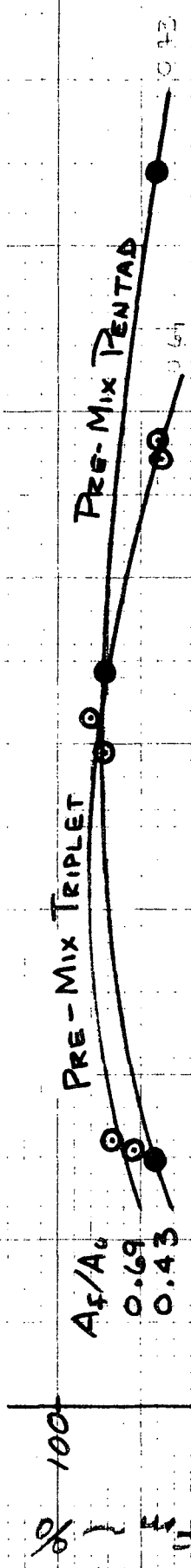
THE EFFECT OF AREA RATIO  
AND DIAMETER RATIO



THE EFFECT OF PROPORTION  
TEMPERATURE ON  $\epsilon_m$



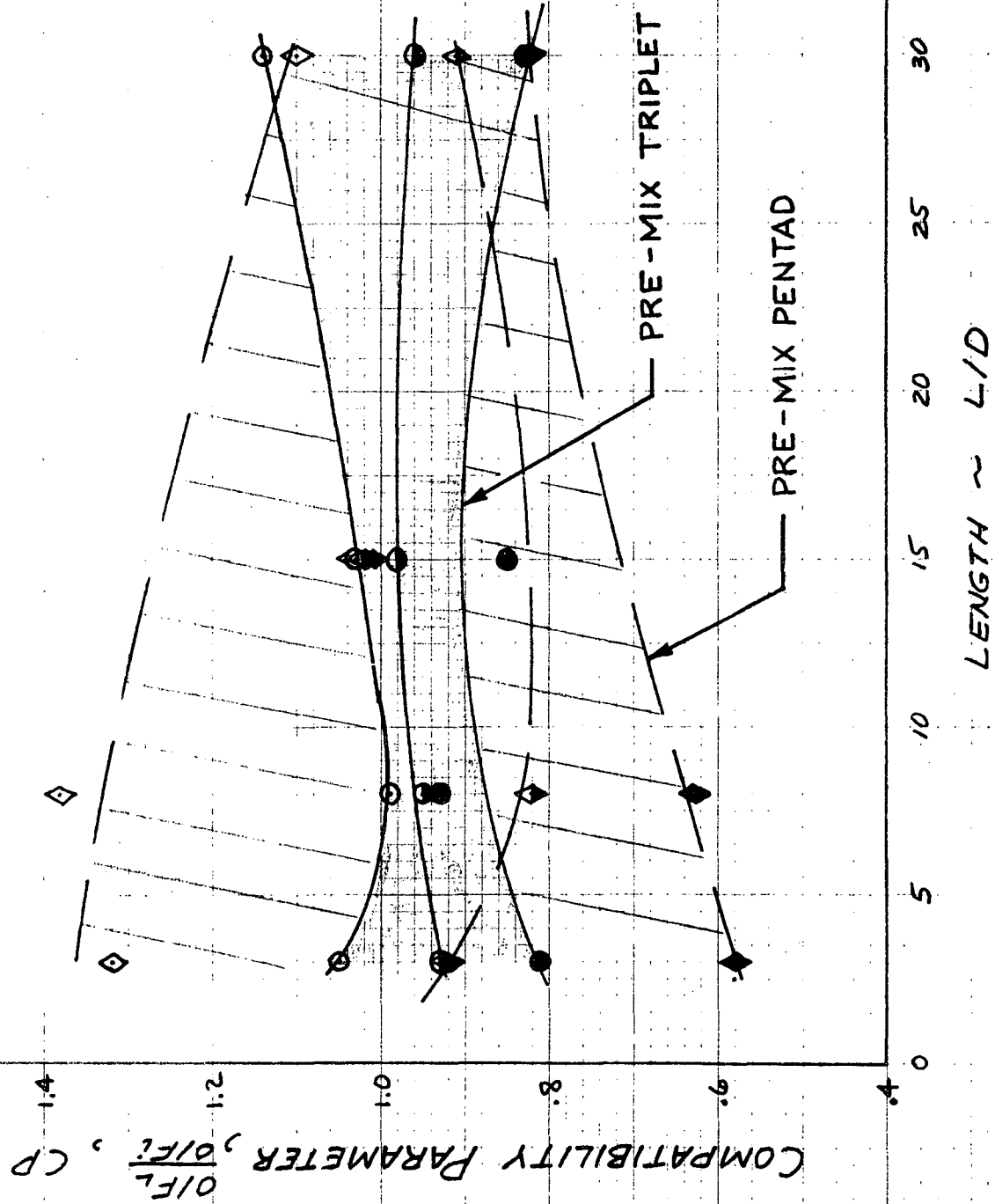
# THE EFFECT OF MIXTURE RATIO ON $\epsilon_m$



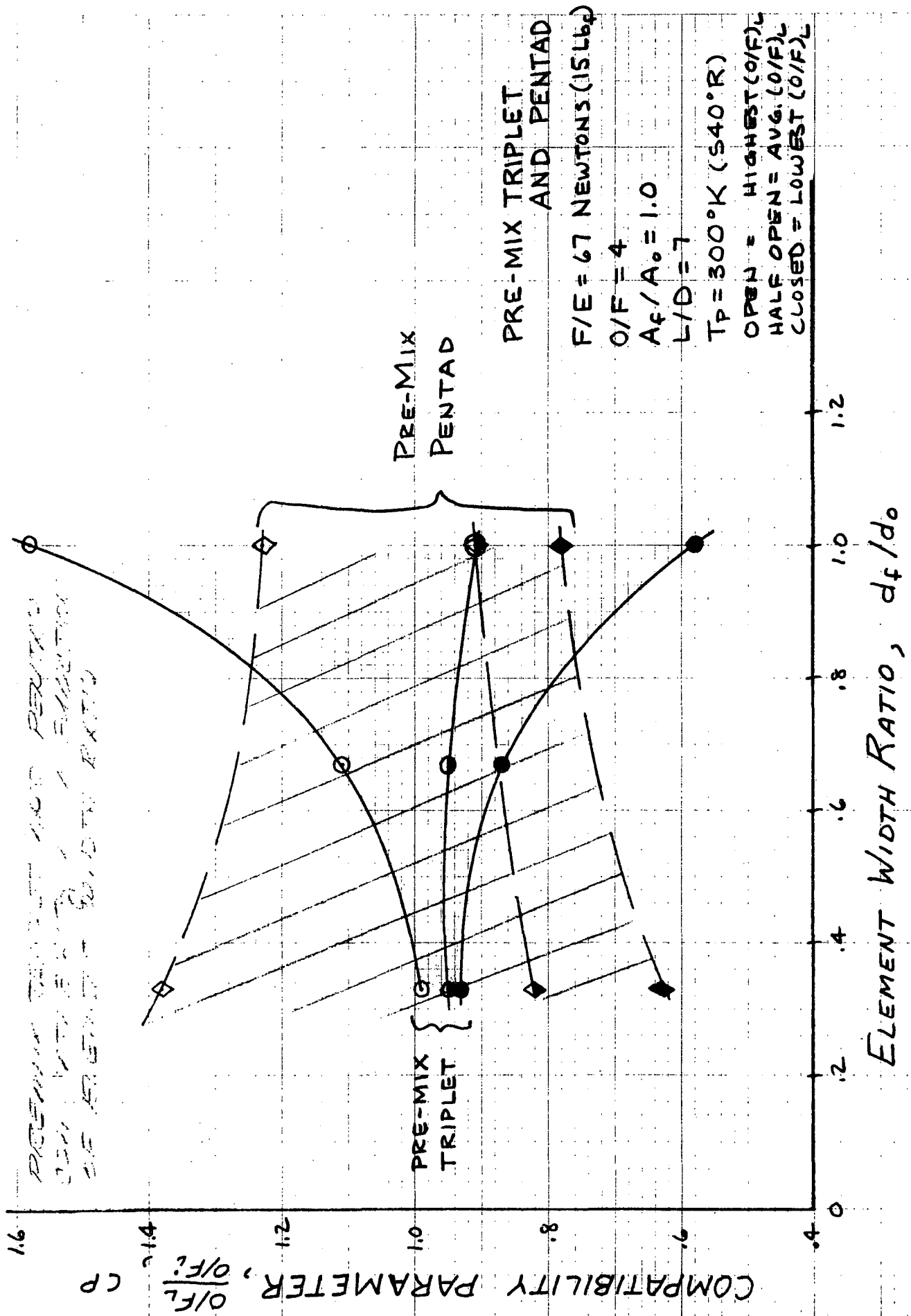
PRE-MIX TRIPLET & PENTAD FAMILY  
 $F/E = 13$  NEWTONS (3Lbf)  
 $T_p = 300^\circ K$  (540°R)  
 $L/D = 15$   
 $d_f/d_o = 0.33$

DESIGN TRIPLET AND PENTAD COMPATIBILITIES  
 OF THE PRE-MIX

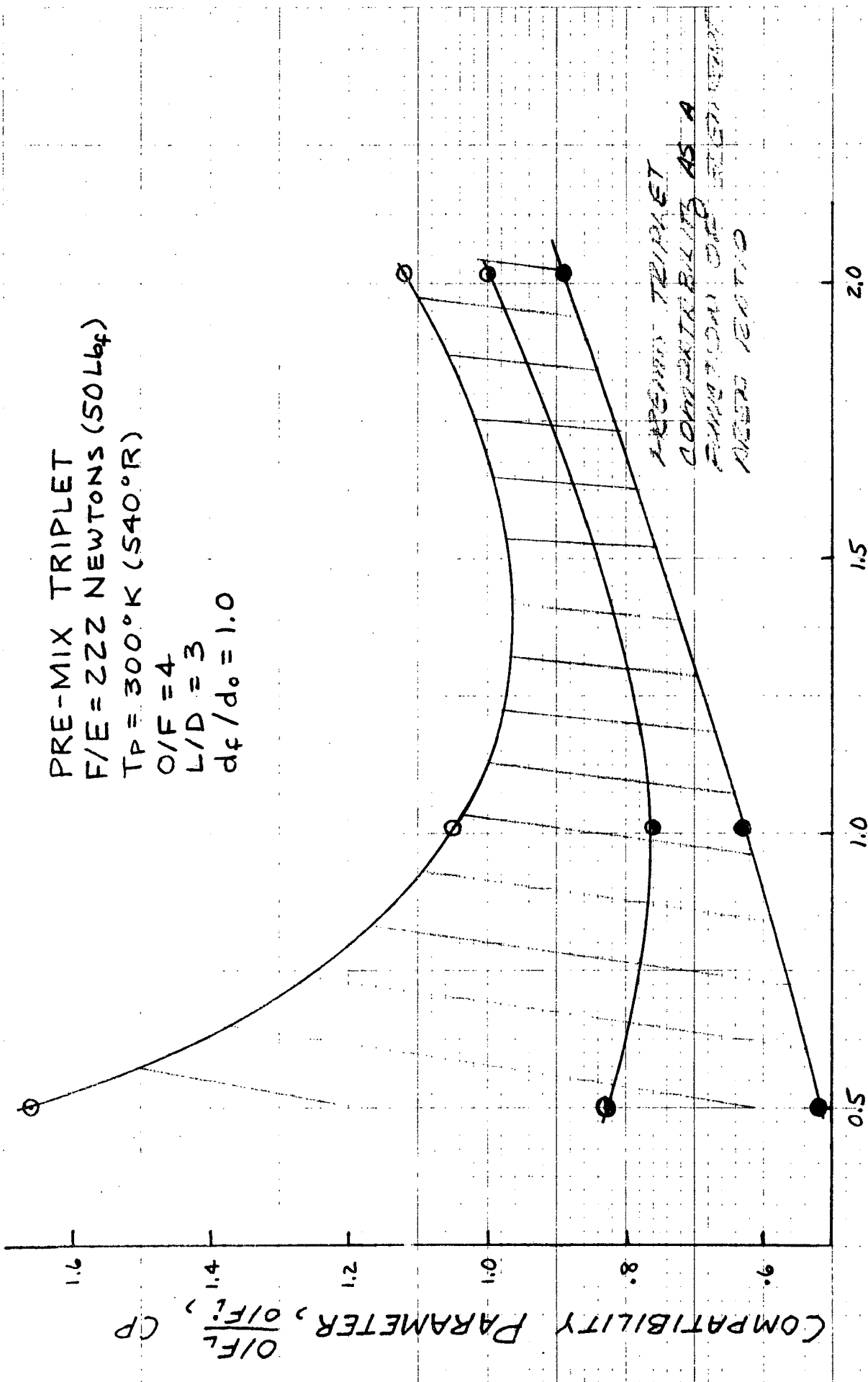
$F/E = 67 \text{ NEWTONS (15 LB}_f\text{)}$   
 $A_f / A_o = 1.0$   
 $d_f / d_o = 0.33$   
 $O/F = 4$   
 OPEN SYMBOLS = HIGHEST  $(O/F)_L$   
 HALF OPEN SYM = AVG.  $(O/F)_L$   
 CLOSED SYM = LOWEST  $(O/F)_L$





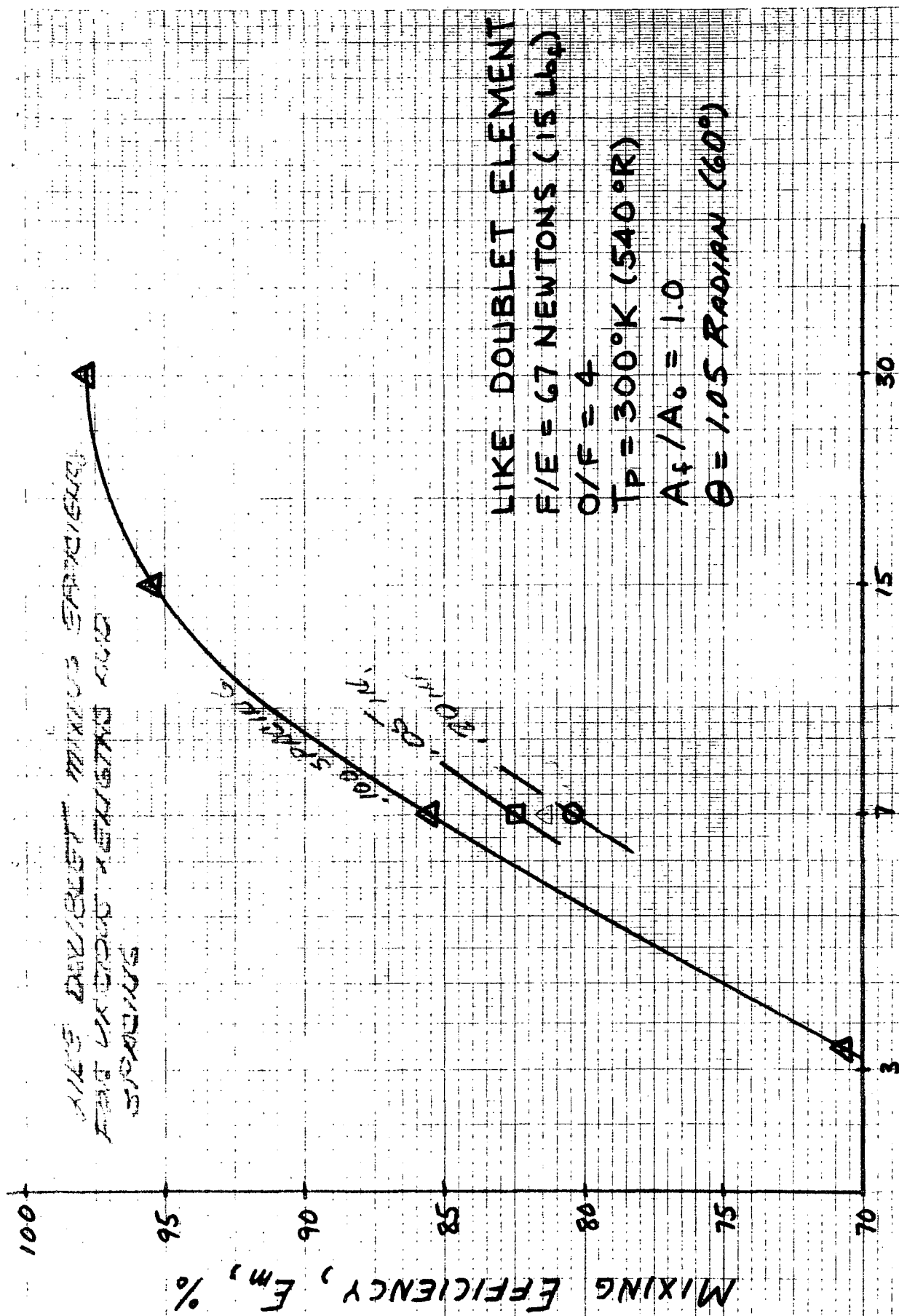


PRE-MIX TRIPLET  
 $F/E = 222 \text{ NEWTONS (50 Lbf)}$   
 $T_P = 300^\circ \text{K (540}^\circ \text{R)}$   
 $O/F = 4$   
 $L/D = 3$   
 $d_f/d_o = 1.0$



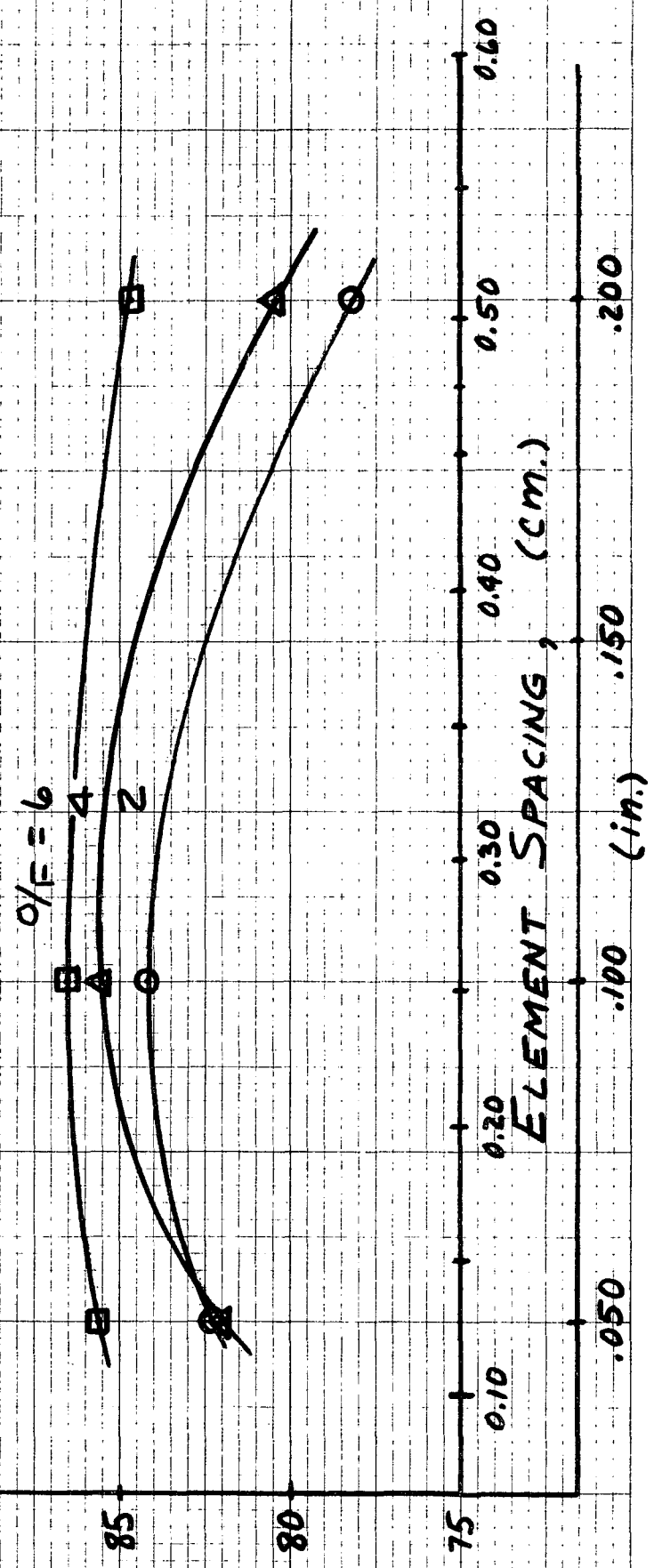
PRE-MIX TRIPLET  
 COMPUTED AS A  
 FUNCTION OF FUEL  
 AREA RATIO

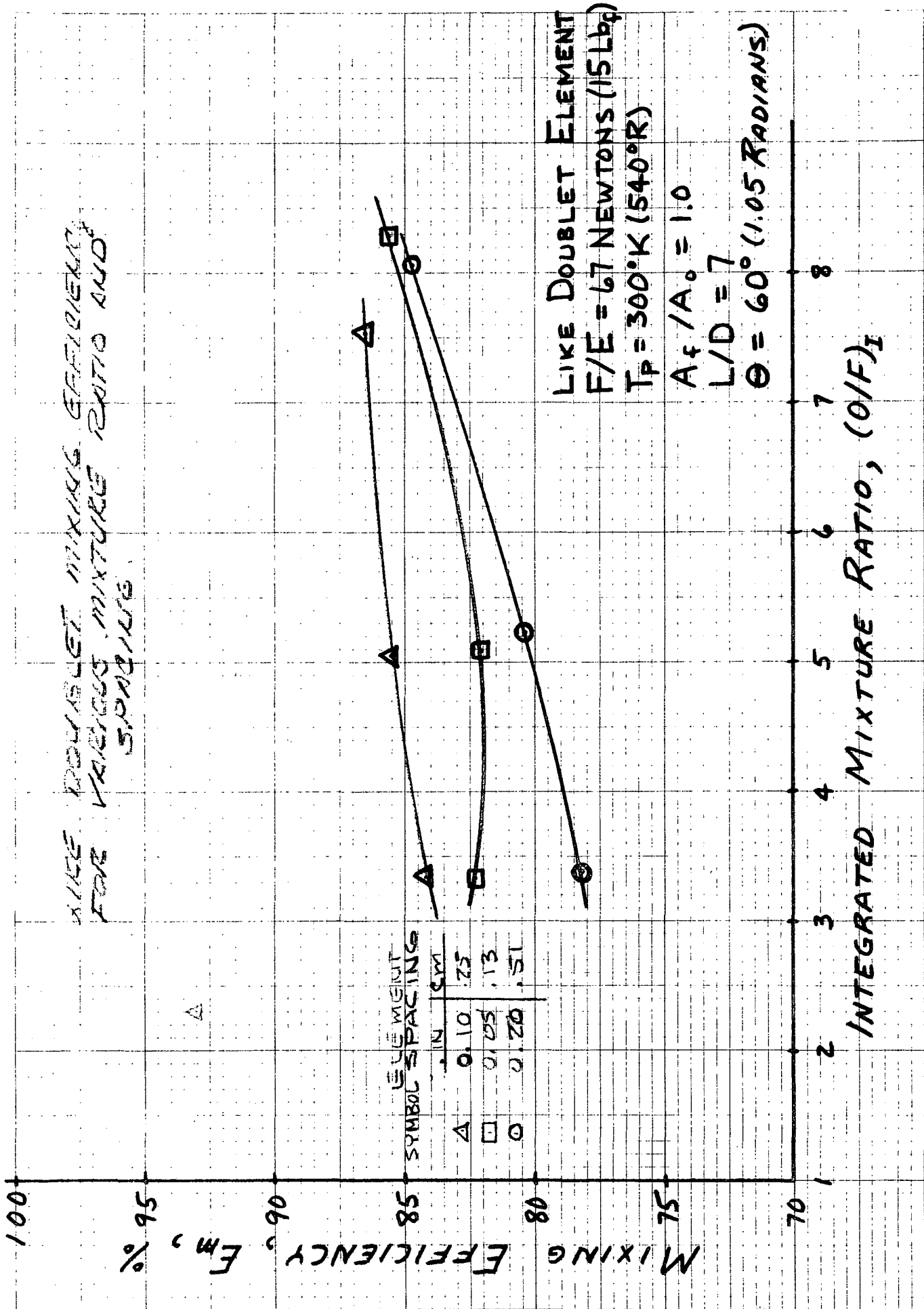
FUEL TO OXIDIZER ORIFICE AREA RATIO,  $A_f/A_o$



LIKE DOUBLET MIXING EFFICIENCIES  
FOR VARIOUS MIXTURE RATIOS AND  
SPACINGS

LIKE DOUBLET ELEMENT  
 $F/E = 67 \text{ NEWTONS (15 LB}_f\text{)}$   
 $T_P = 300^\circ\text{K (540}^\circ\text{R)}$   
 $A_f/A_o = 1.0$   
 $L/D = 7$   
 $\Theta = 1.05 \text{ Radian (60}^\circ\text{)}$





LIKE DOUBLET MIXING  
EFFICIENCY AS A FUNCTION  
OF AREA RATIO

LIKE DOUBLET ELEMENT  
F/E = 67 NEWTONS (15 lb<sub>f</sub>)  
T<sub>p</sub> = 300°K (540°R)

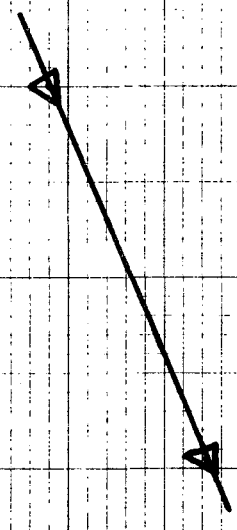
O/F = 4  
L/D = 7

$\theta = 1.05$  RADIAN (60°)

ELEM. SPACING = 0.25 cm. (0.100 in.)

MIXING EFFICIENCY,  $F_m$ , %

FUEL TO OXIDIZER ORIFICE AREA RATIO,  $A_f/A_o$





5/6.32

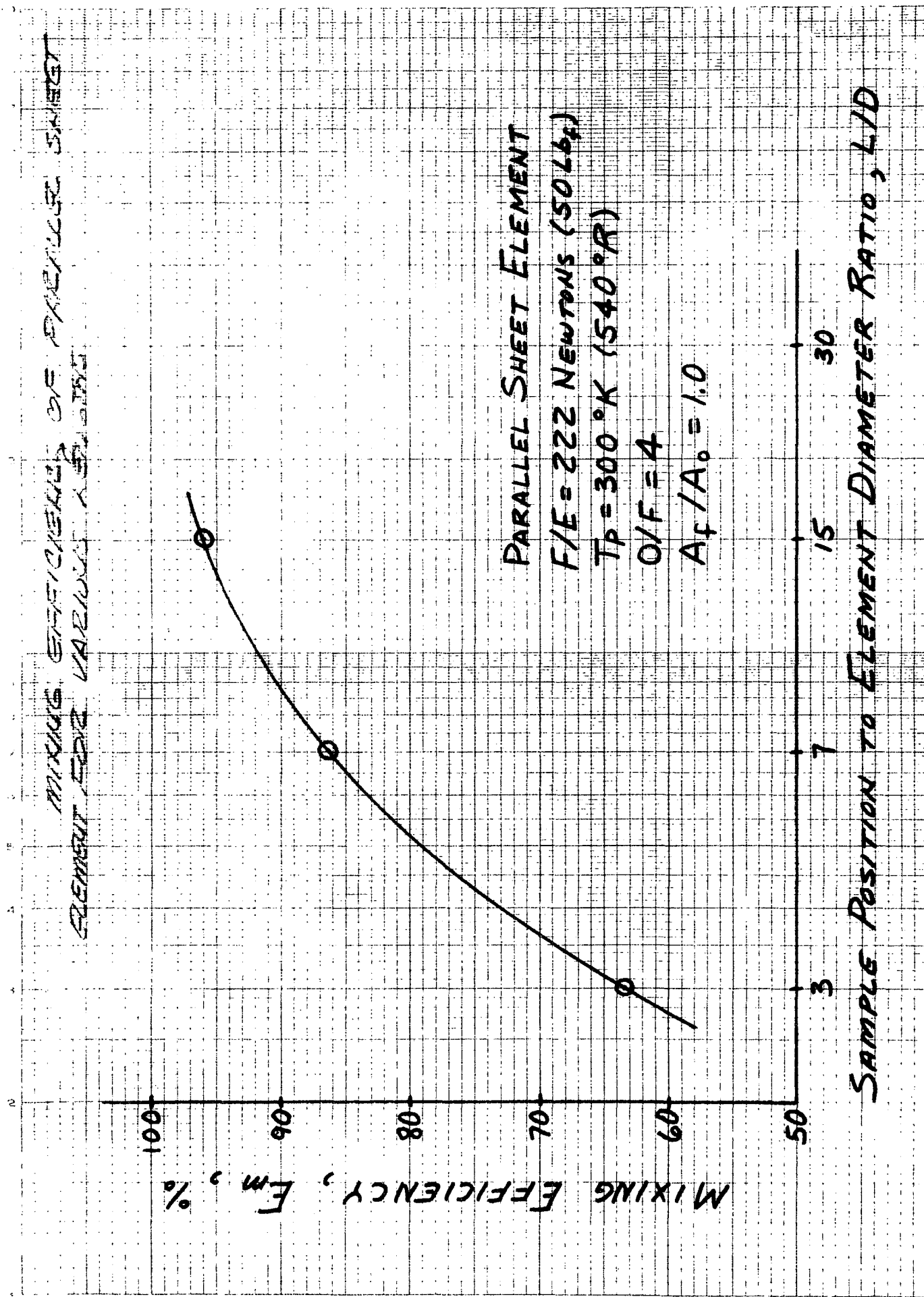


FIG 33



PARALLEL SHEET ELEMENT

$T_p = 300^\circ K (540^\circ R)$

$A_f/A_o = 1.0$

$O/F = 4$

$L/D = 7$

MIXING EFFICIENCY

OF PARALLEL SHEET

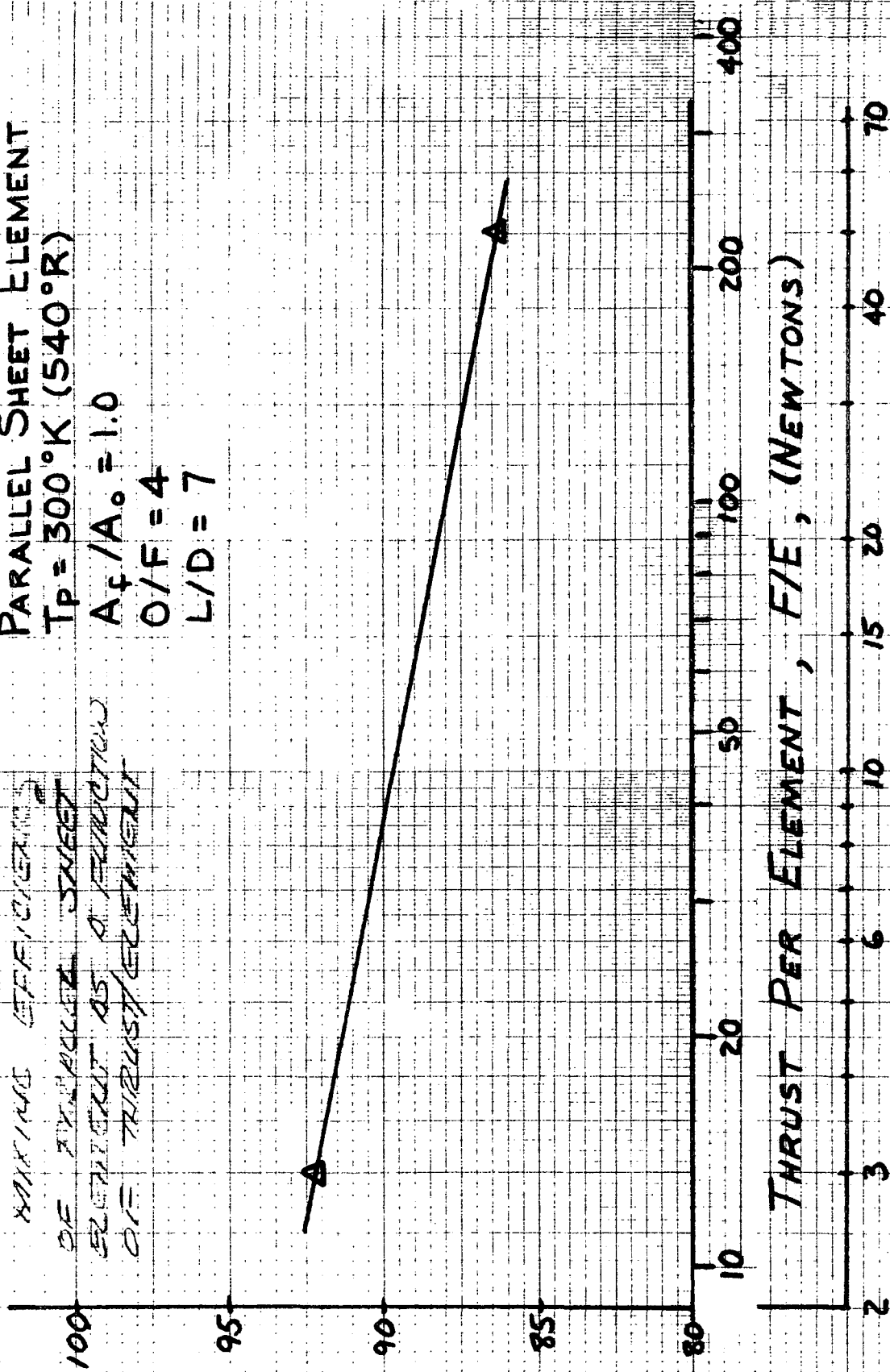
ELEMENT AS A FUNCTION

OF THRUST/ELEMENT

MIXING EFFICIENCY,  $E_m$ , %

THRUST PER ELEMENT,  $F/E$ , (NEWTONS)

( $Lb_f$ )



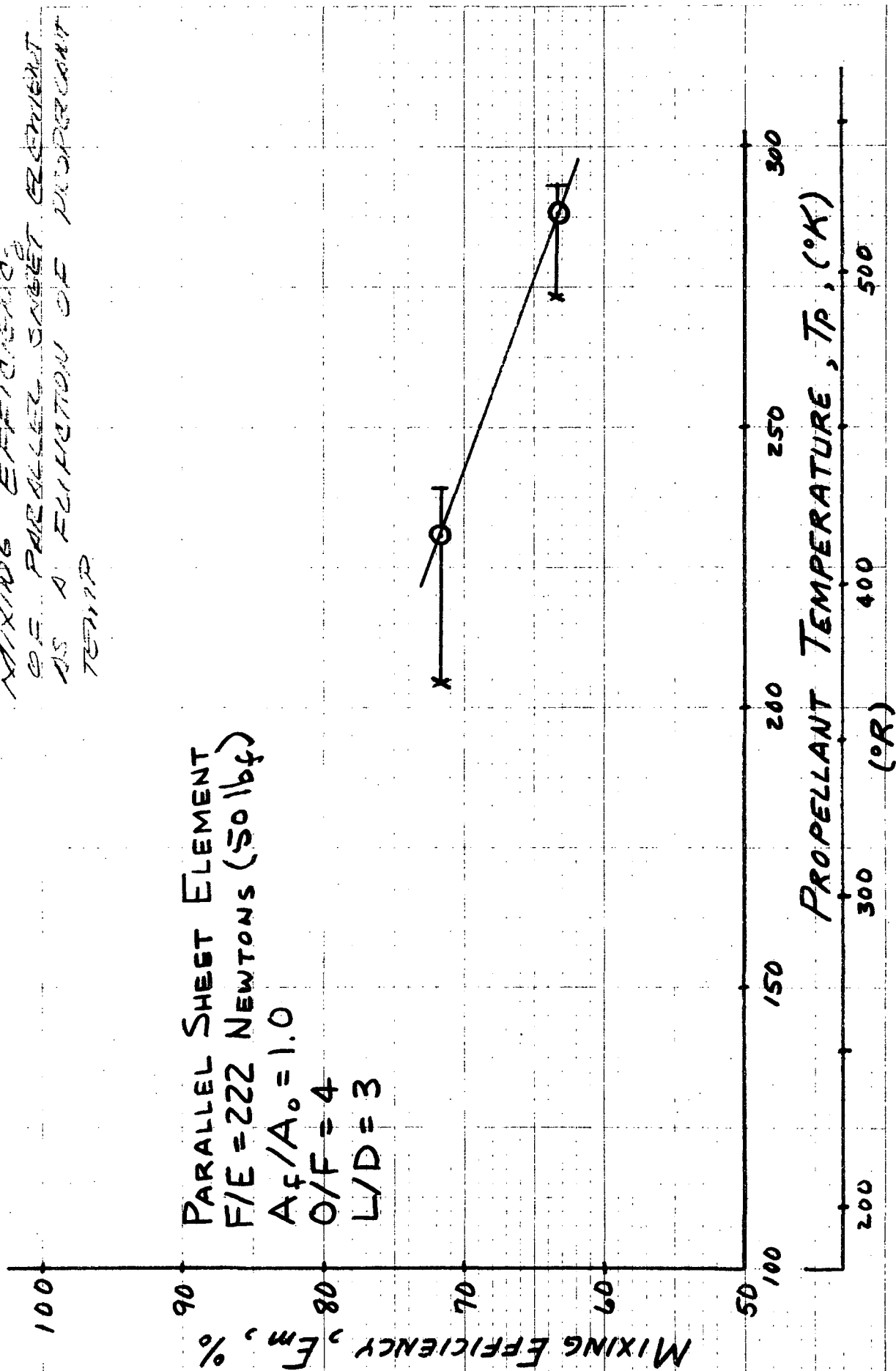
MIXING EFFICIENCY  
OF PARALLEL SHEET ELEMENT  
AS A FUNCTION OF PROPELLANT  
TEMP

PARALLEL SHEET ELEMENT  
F/E = 222 NEWTONS (50 lbf)

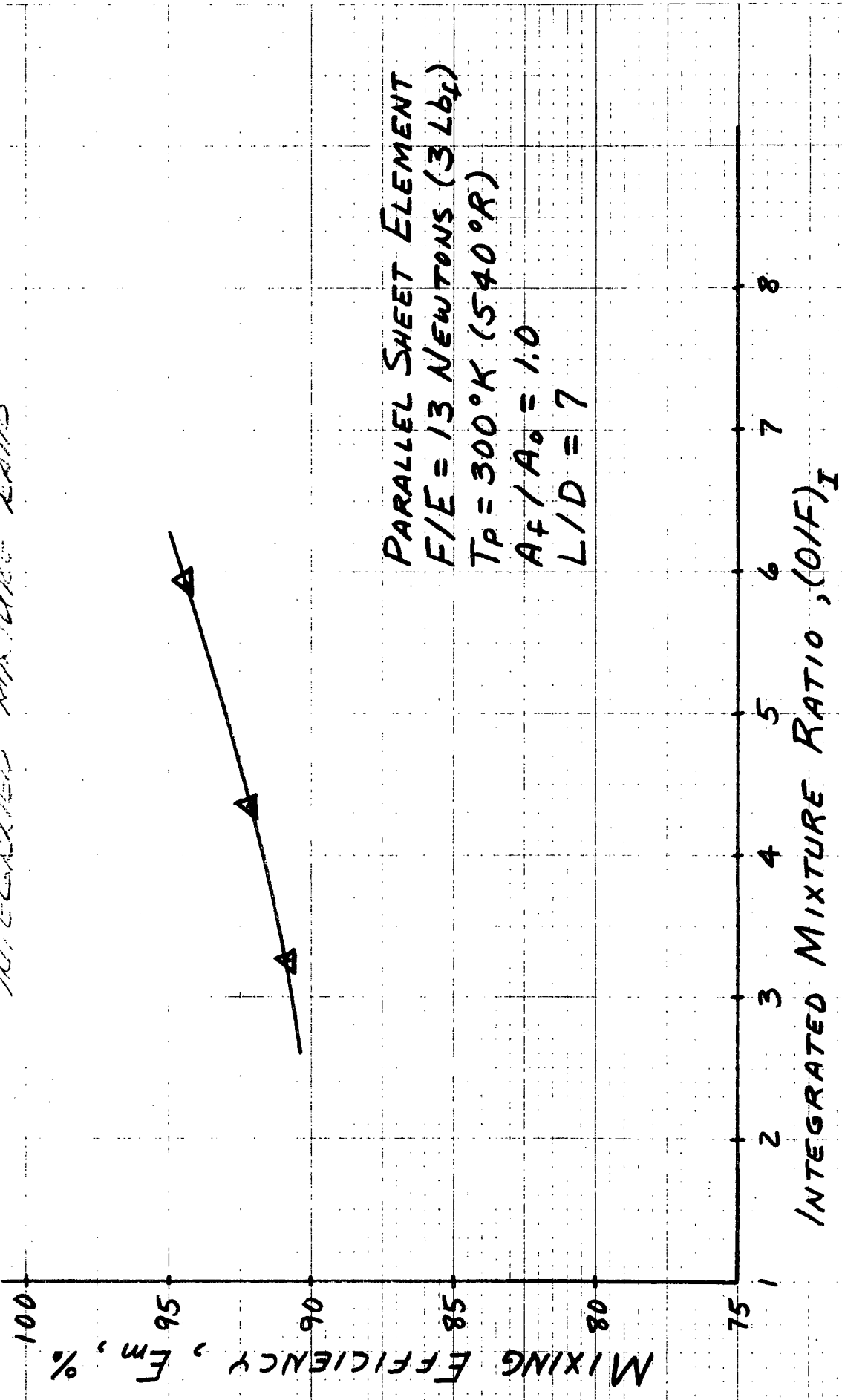
$A_f/A_o = 1.0$

$O/F = 4$

$L/D = 3$

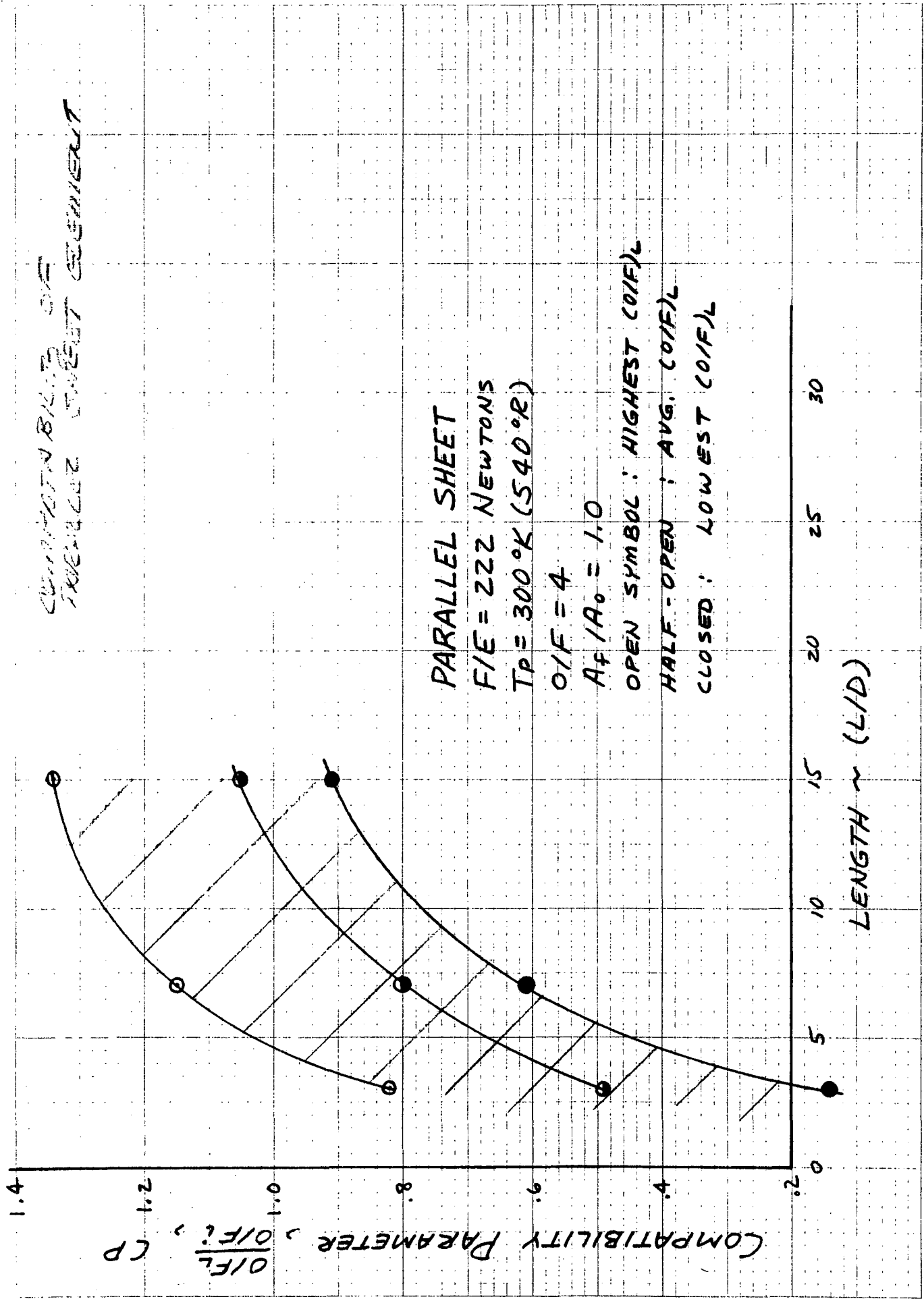


MIXING OF PARALLEL SHEET  
ELEMENT AS A FUNCTION OF  
INTEGRATED MIXTURE RATIO



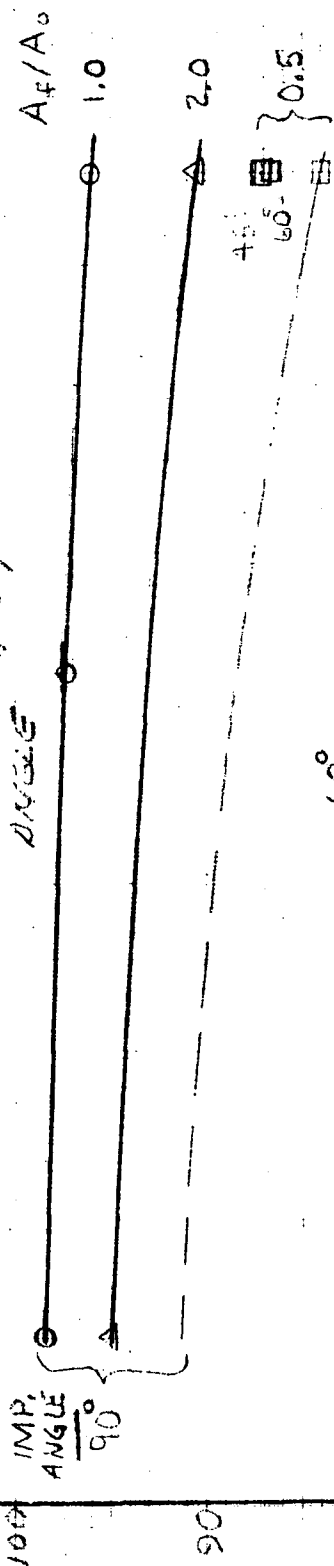
PARALLEL SHEET ELEMENT  
 $F/E = 13 \text{ NEWTONS (3 Lbf)}$   
 $T_p = 300^\circ\text{K (540}^\circ\text{R)}$   
 $A_f / A_o = 1.0$   
 $L/D = 7$

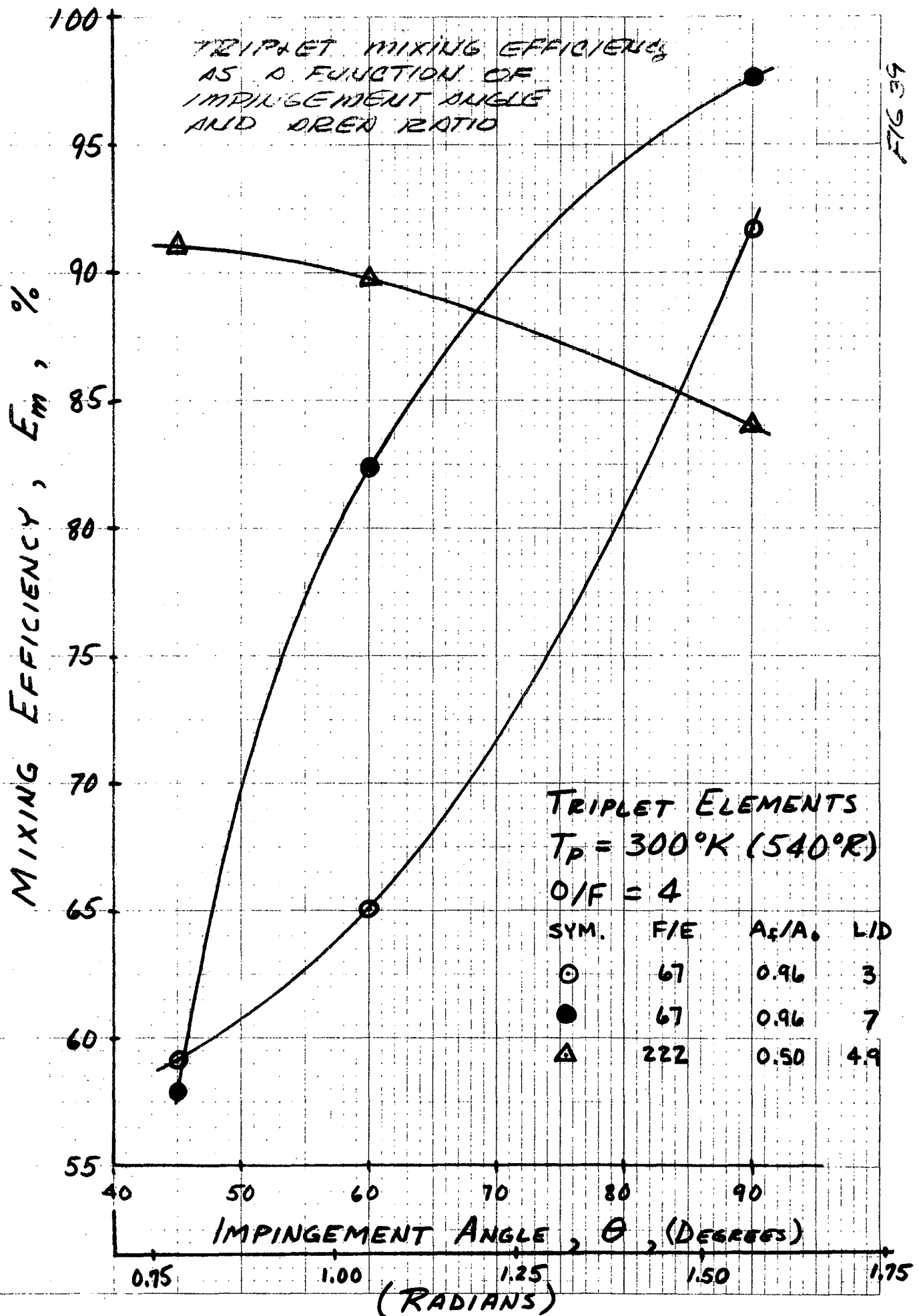
FIG. 36

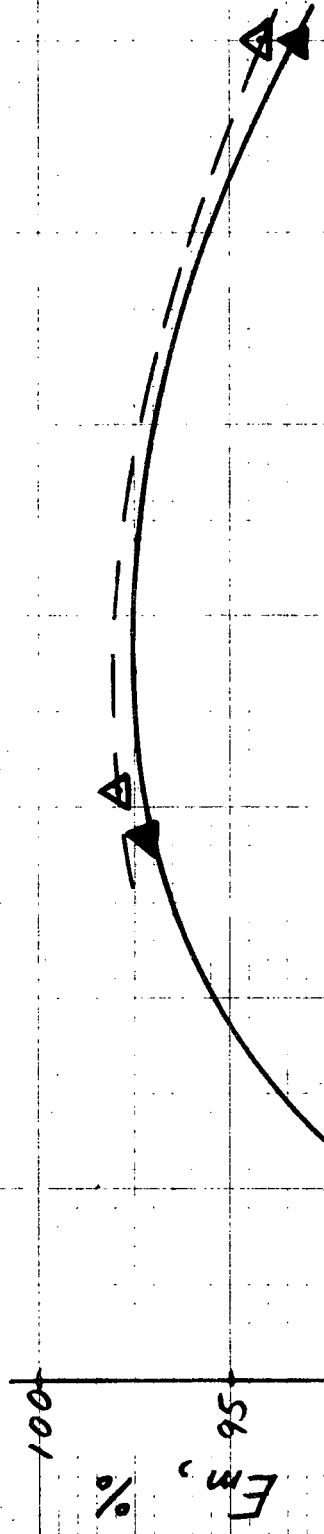


# F-O-F TRIPLET

MIXING EFFICIENCY AS A  
FUNCTION OF IMP. ALIGNMENT  
ANGLE







TRIPLET MIXING EFFICIENCY AS A  
FUNCTION OF  
AREA RATIO

TRIPLET ELEMENT  
 $T_p = 300^\circ K (540^\circ R)$   
 $\theta = 60^\circ$

$O/F = 4$

SYMBOL	L/D	F/F
$\Delta$	15	13 NEWTONS
$\blacktriangle$	4.9	222 NEWTONS

FUEL TO OXIDIZER ORIFICE AREA RATIO,  $A_F/A_O$

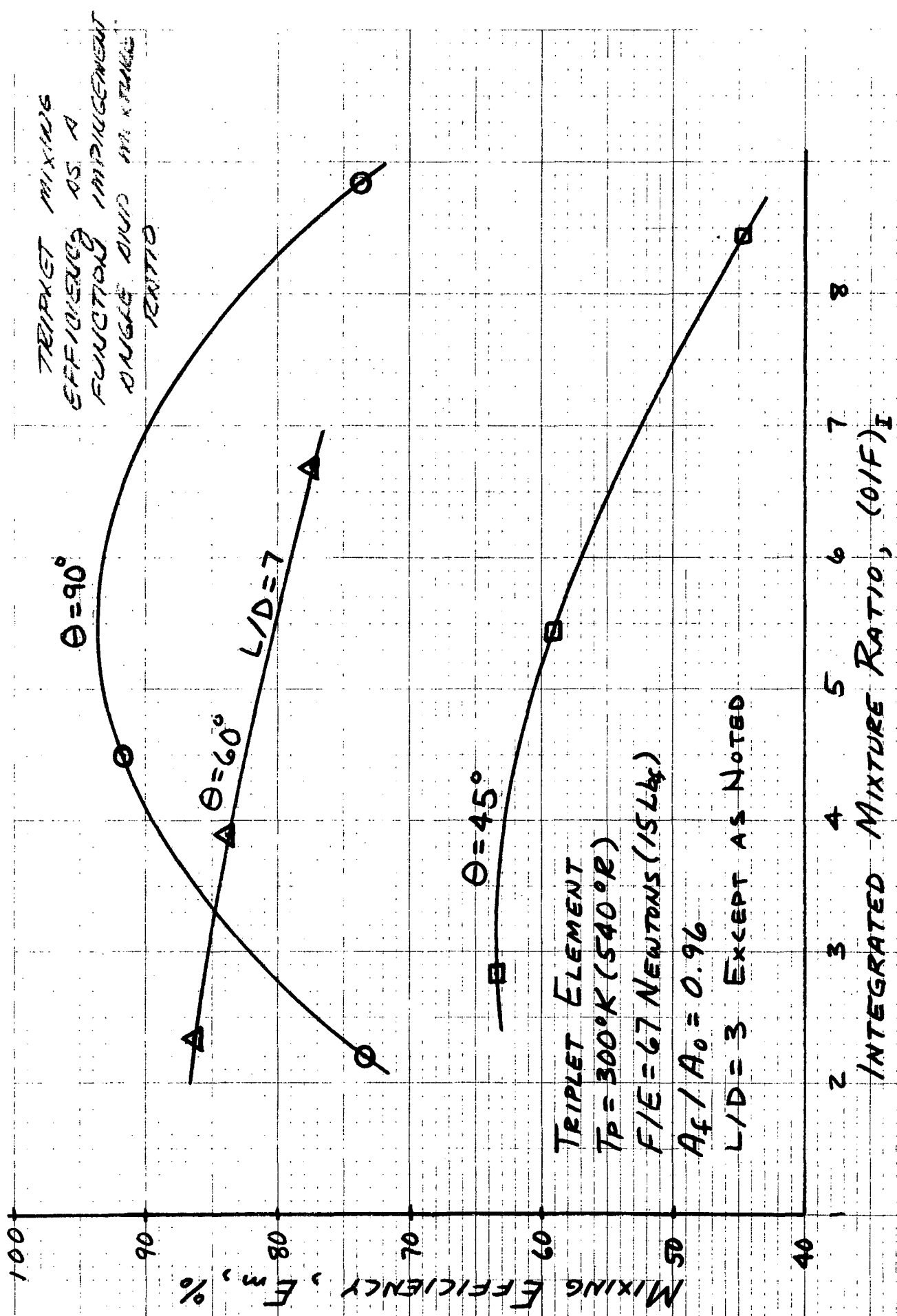


FIG 41



# TRIPLUST ELEMENT COMPATIBILITY CHARACTERISTICS

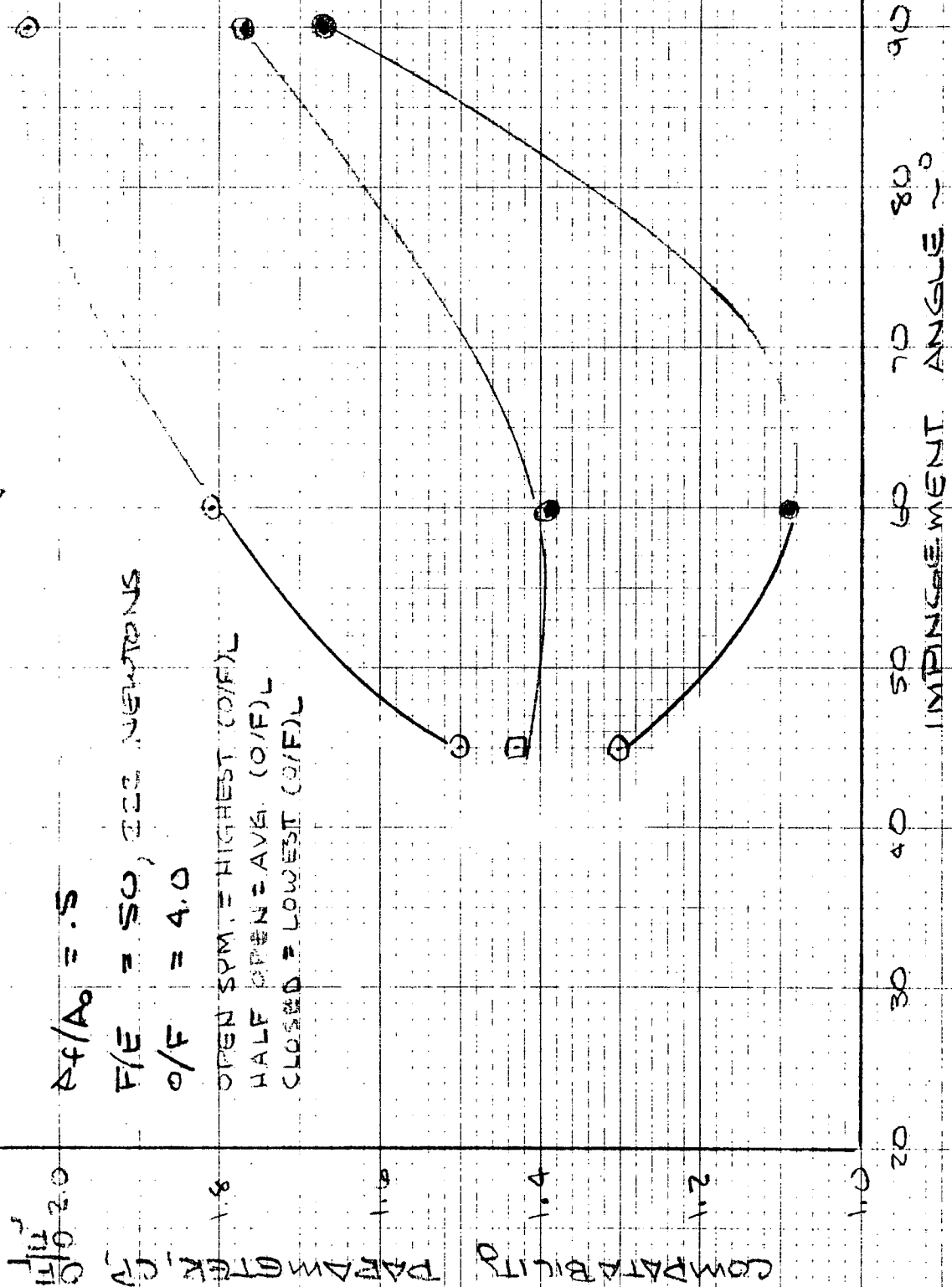


FIG. 42

VELOCITY AND DENSITY

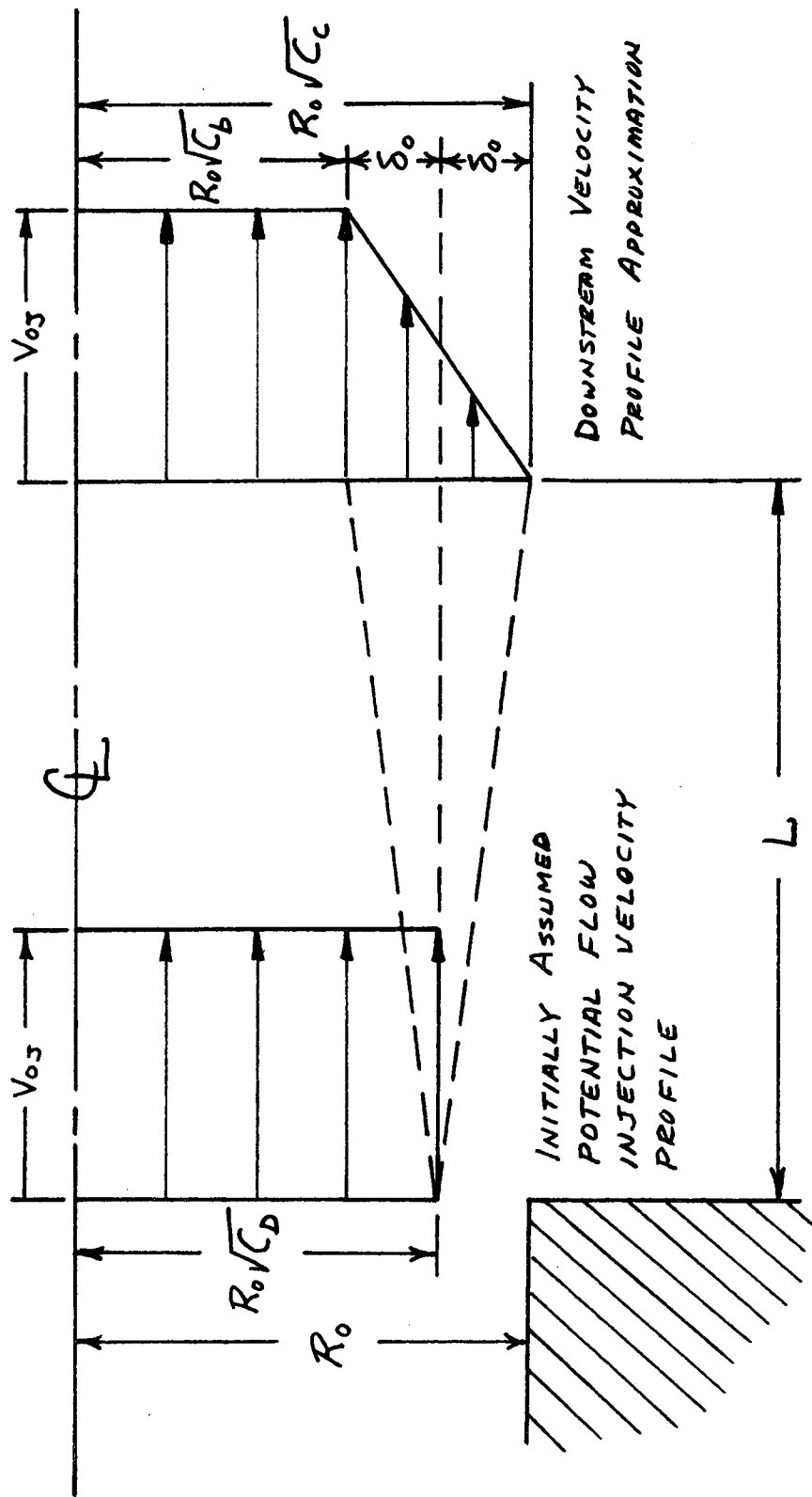


FIG. 43

# DYNAMIC HEAD DECAY

SHEAR CO-AXIAL ELEMENT

$F/E = 67 \text{ NEWTONS (15 Lbf)}$

$T_p = 3000^\circ\text{K (5400^\circ\text{R})}$

$A_f/A_o = 1.0$

$O/F = 4$

▲ MEASURED OXIDIZER DYNAMIC HEAD

● MEASURED FUEL DYNAMIC HEAD @ 1.2 FUEL ANNULUS WIDTH FROM FUEL CENTERLINE

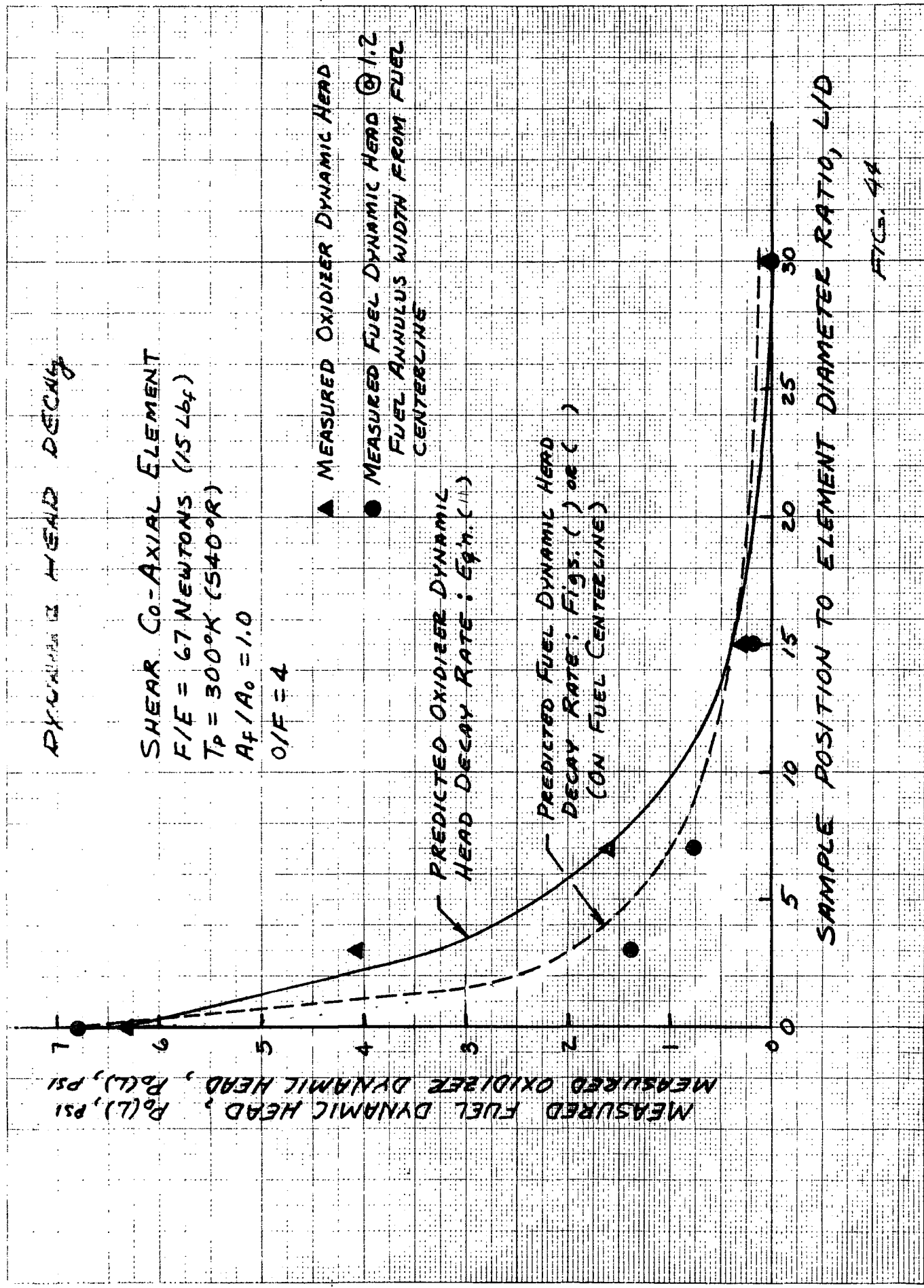
PREDICTED OXIDIZER DYNAMIC HEAD DECAY RATE: Eq'n. (1)

PREDICTED FUEL DYNAMIC HEAD DECAY RATE: Figs. ( ) or ( ) (ON FUEL CENTERLINE)

MEASURED FUEL DYNAMIC HEAD,  $P_o(L)$ , PSI  
MEASURED OXIDIZER DYNAMIC HEAD,  $P_o(L)$ , PSI

SAMPLE POSITION TO ELEMENT DIAMETER RATIO,  $L/D$

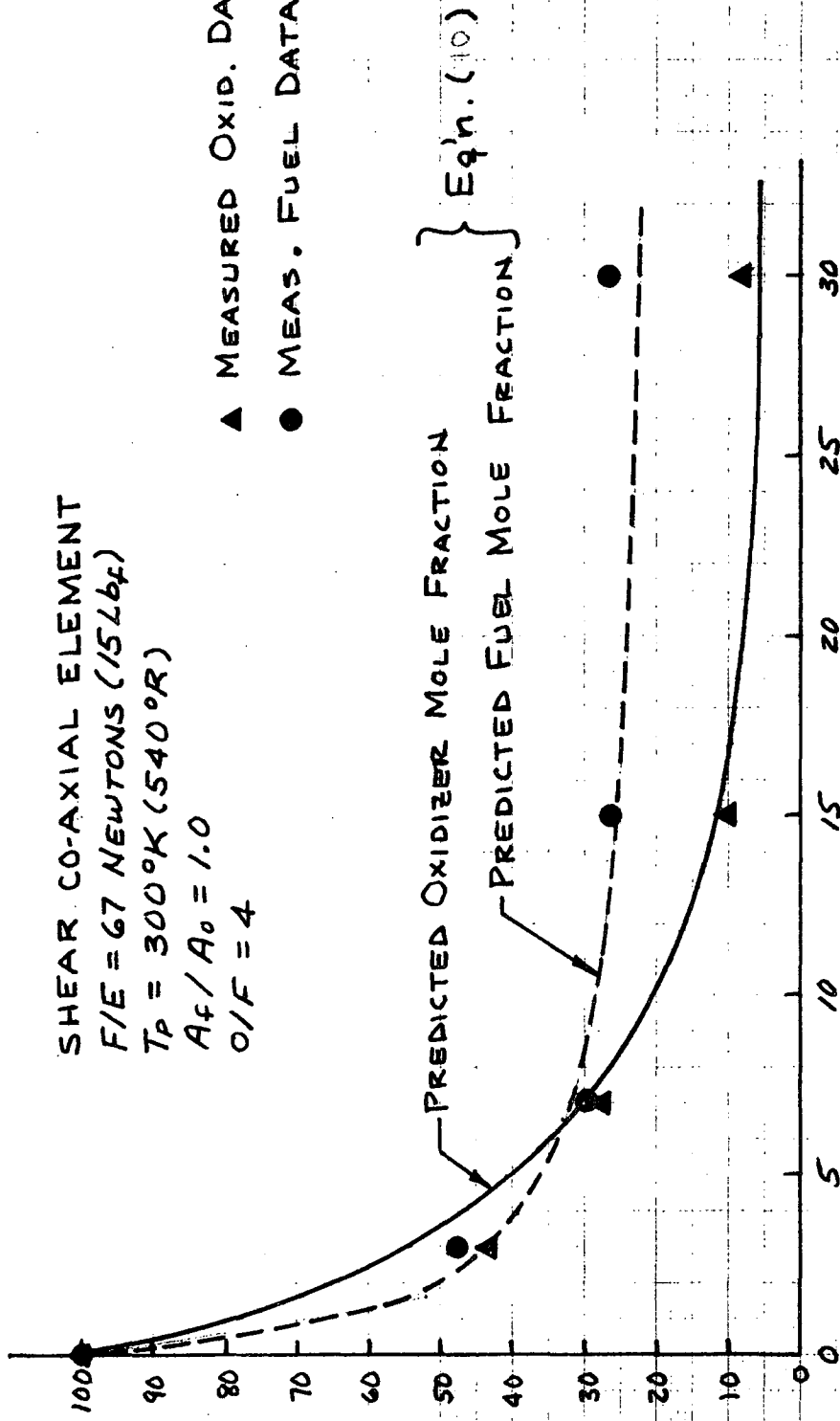
FIG. 44



MOLE FRACTION DECAY

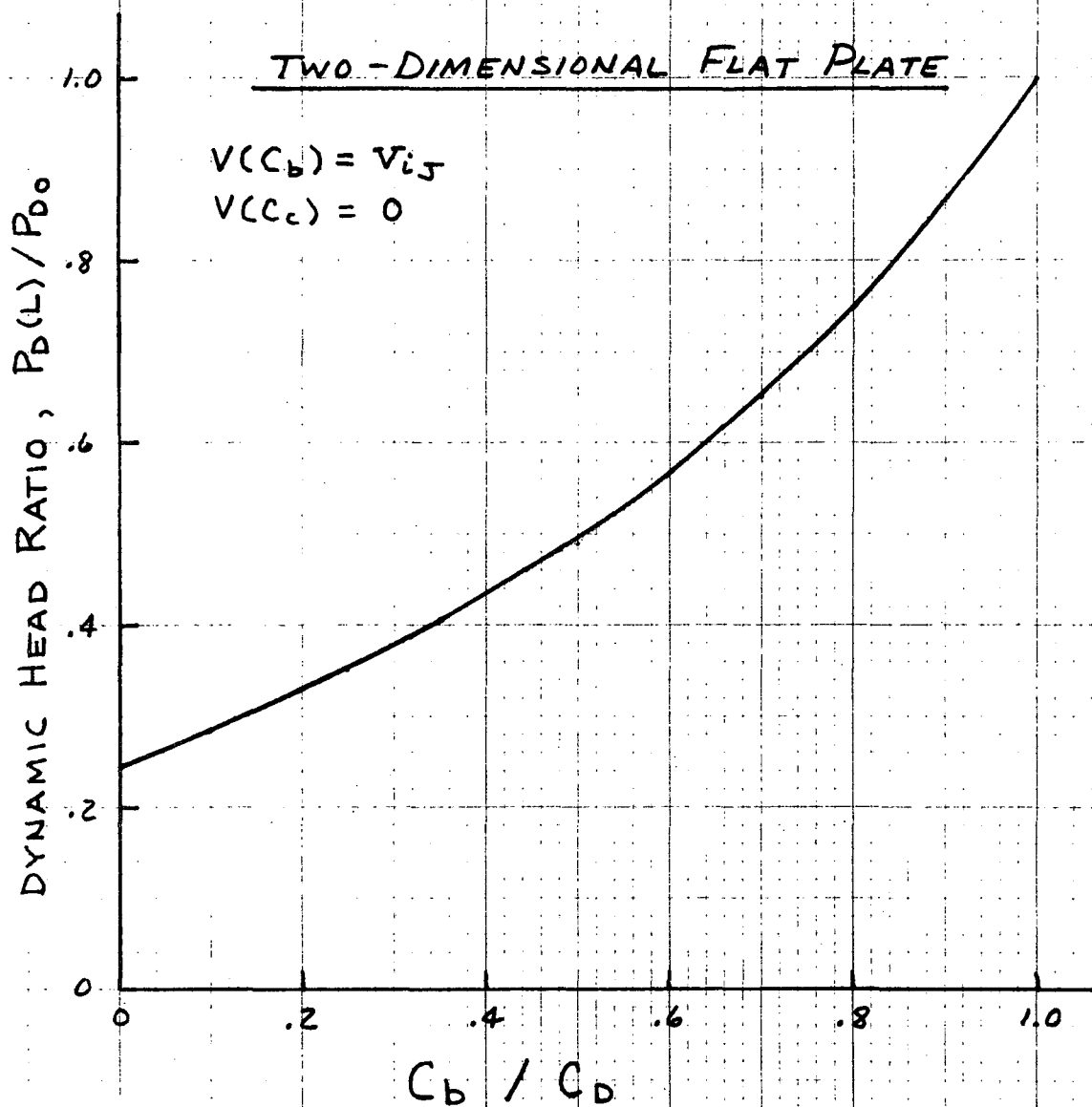
SHEAR CO-AXIAL ELEMENT  
 $F/E = 67$  NEWTONS (15 Lbf)  
 $T_p = 300^\circ K$  (540°R)  
 $A_f/A_o = 1.0$   
 $O/F = 4$

MEASURED FUEL MOLE FRACTION,  $X_{H_2}$ , %  
 MEASURED OXIDIZER MOLE FRACTION,  $X_{H_2}$ , %



SAMPLE POSITION TO ELEMENT DIAMETER RATIO,  $L/D$

FIG. 45



Figure

EFFECT OF POTENTIAL FLOW RATIO ON  
TWO DIMENSIONAL JET DYNAMIC HEAD RATIO

FIG 46

TWO-DIMENSIONAL FLAT PLATE  
(BEYOND FULLY DEVELOPED FLOW PROFILE,

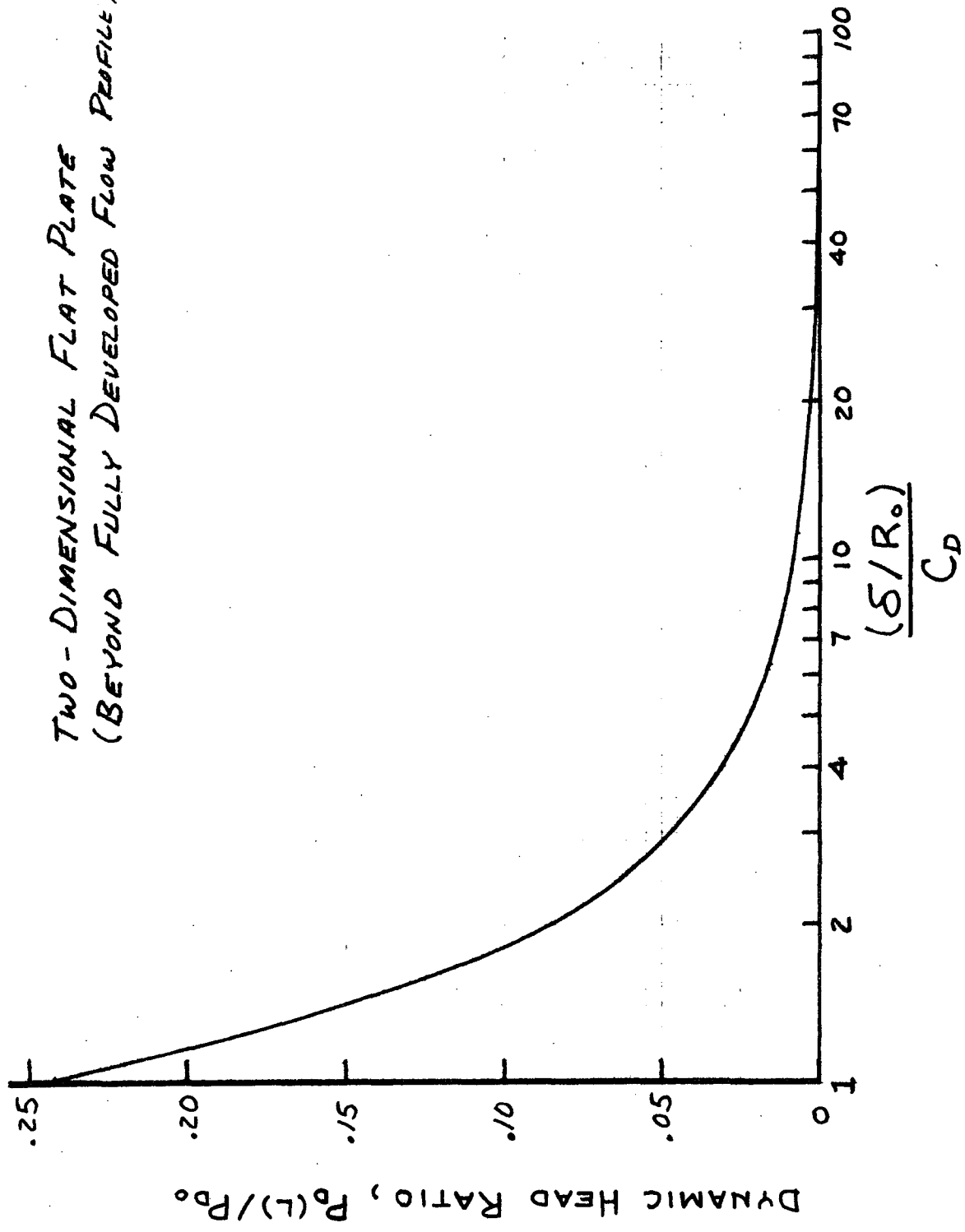


FIG 47

# ANALYTICAL CORRELATION OF EXPERIMENTAL DATA

SHEAR CO-AXIAL ELEMENT  
 $F/E = 67$  NEWTONS (15 Lbf)  
 $T_p = 300^\circ K$  (540°R)  
 $A_f / A_o = 1.0$

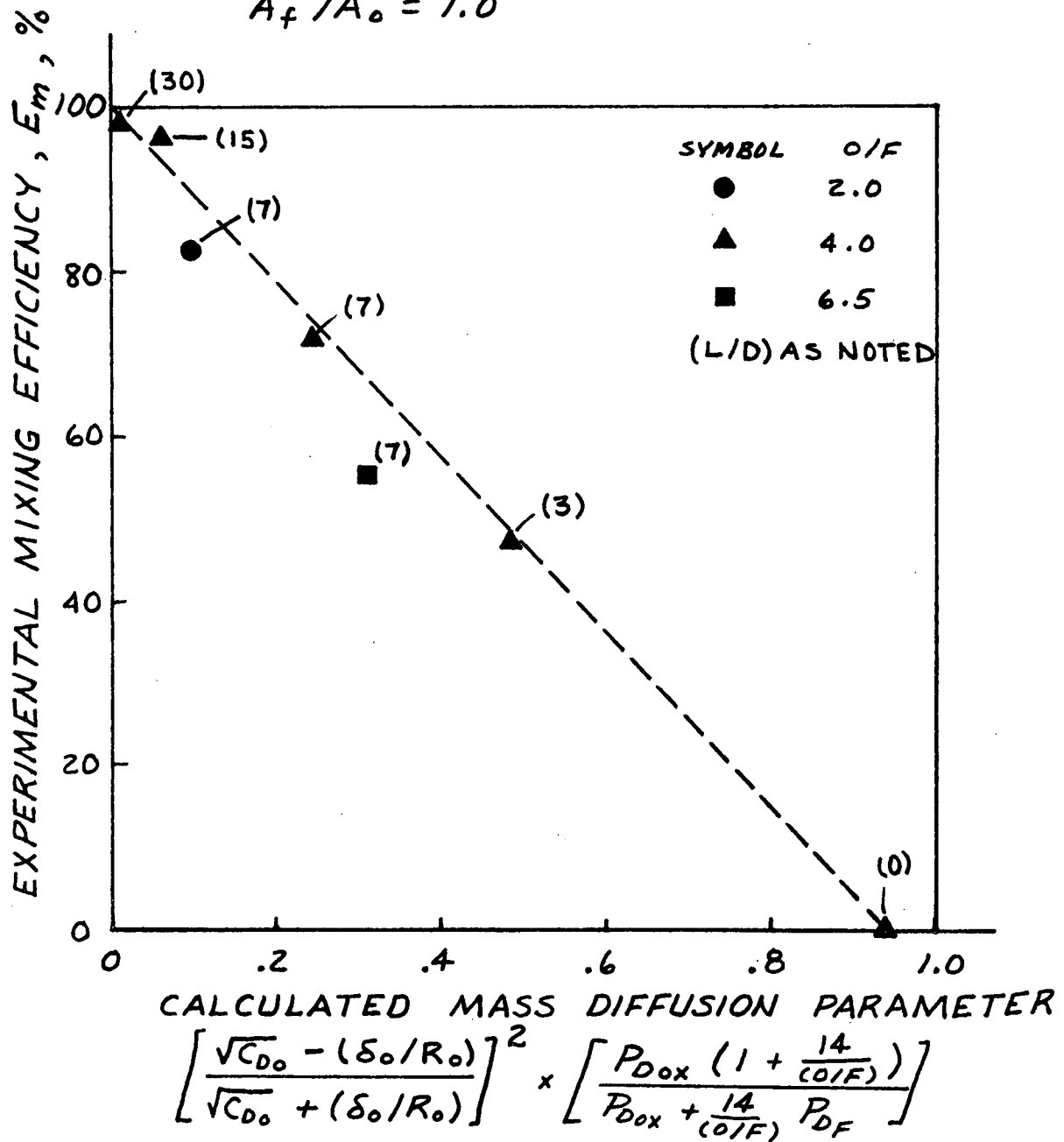
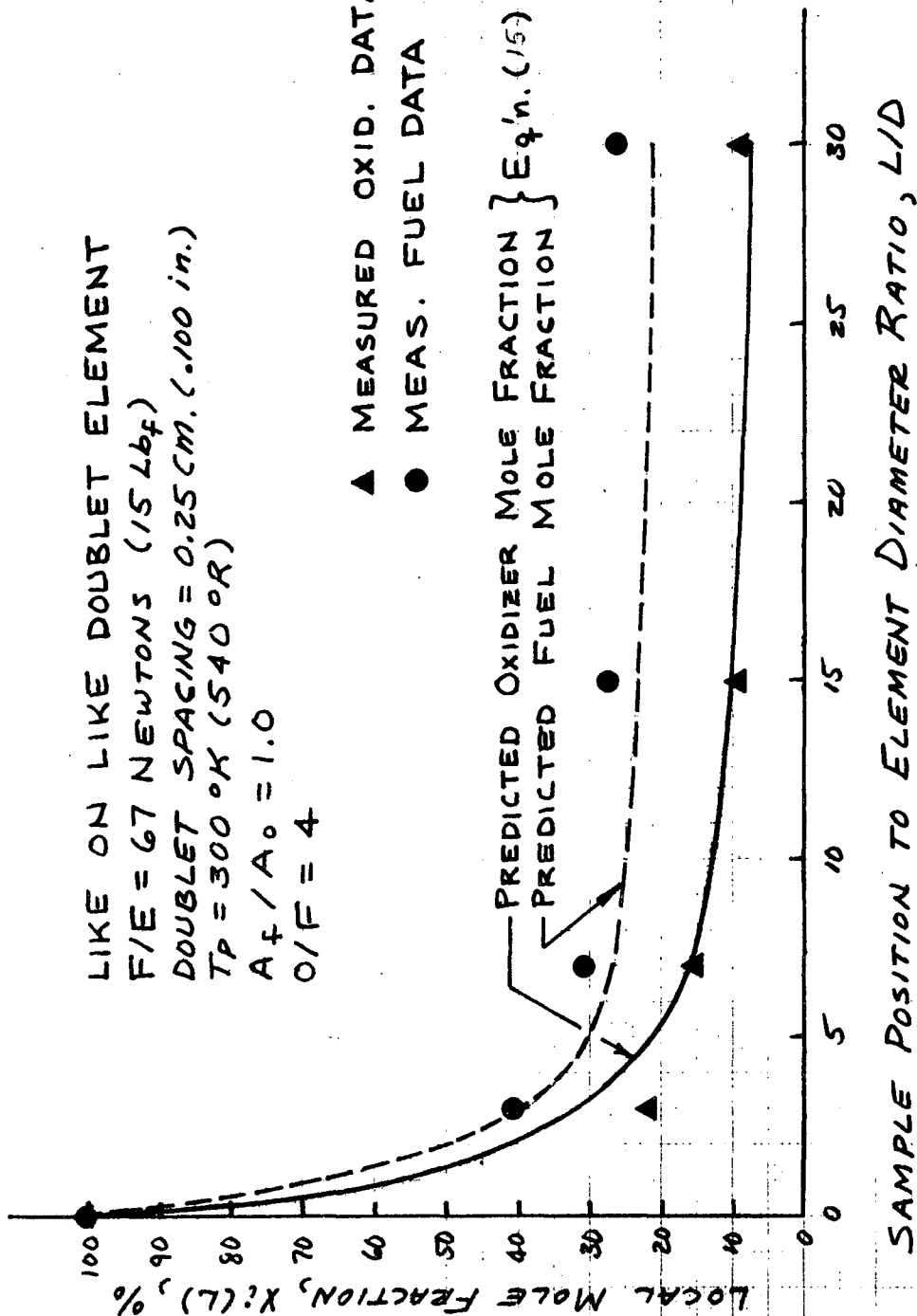


FIG 48

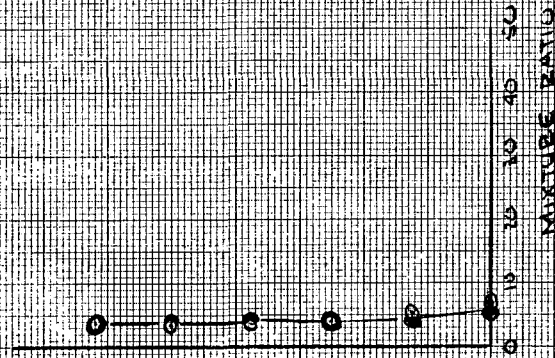
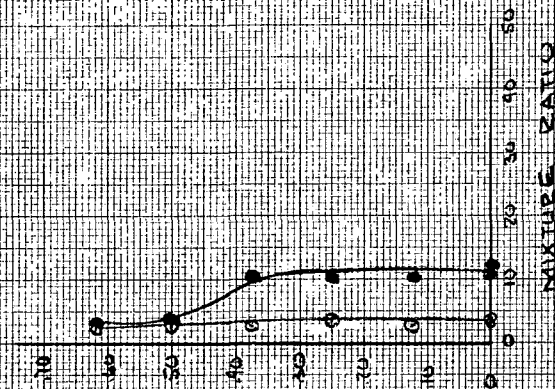
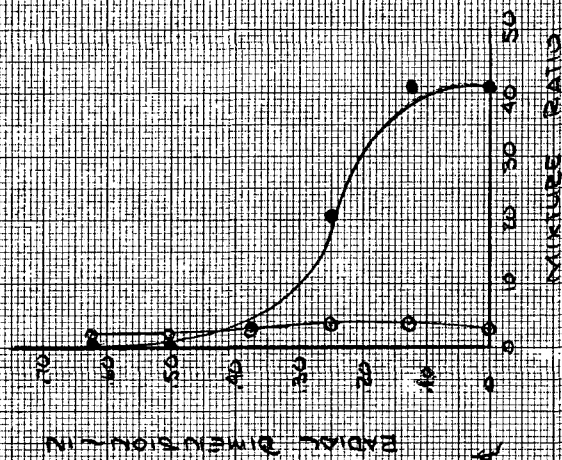
# AXIAL LENGTH VARIATION OF MOLE FRACTION

LIKE ON LIKE DOUBLET ELEMENT  
 $F/E = 67$  NEWTONS (15 Lbf)  
 DOUBLET SPACING = 0.25 CM. (.100 in.)  
 $T_p = 300^\circ K$  (540 °R)  
 $A_f / A_o = 1.0$   
 $O/F = 4$

▲ MEASURED OXID. DATA  
 ● MEAS. FUEL DATA



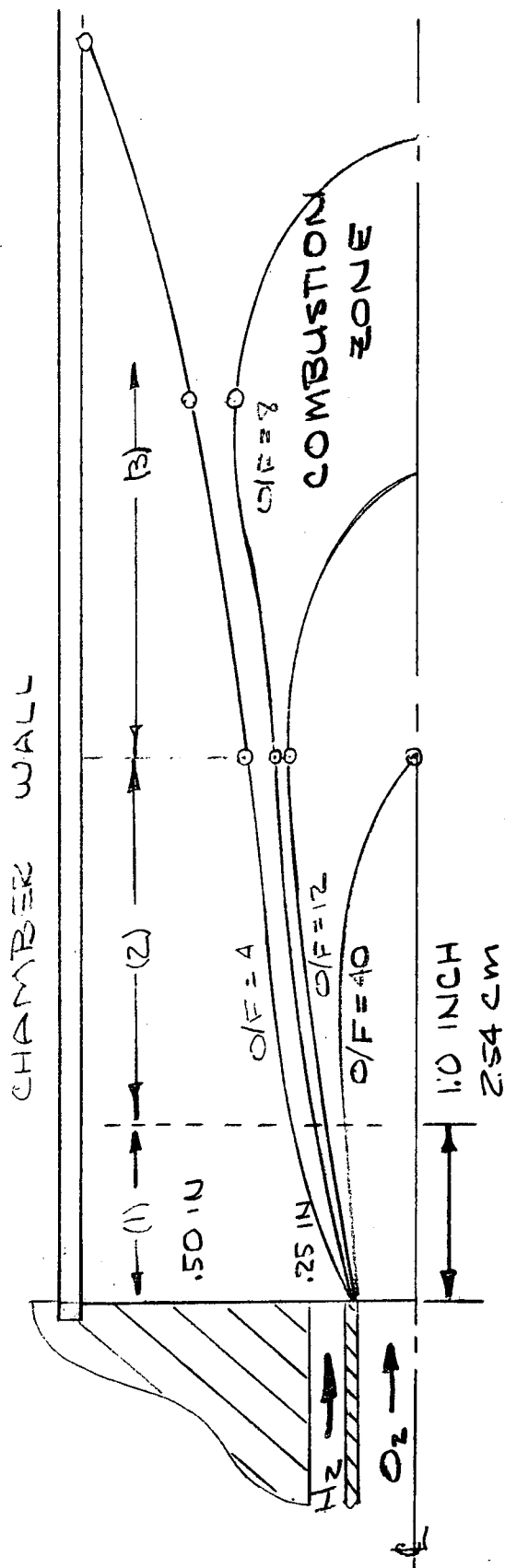




OVERALL MIXTURE RATIO = 4  
CHAMBER PRESSURE = ONE ATMOSPHERE  
CLOSED SYMBOLS = HOT FLOW  
OPEN SYMBOLS = COLD FLOW

THE COMPARISON OF HOT & COLD  
MIXTURE RATIO PROFILES  
FOR A SWIRL COAXIAL  
ELEMENT

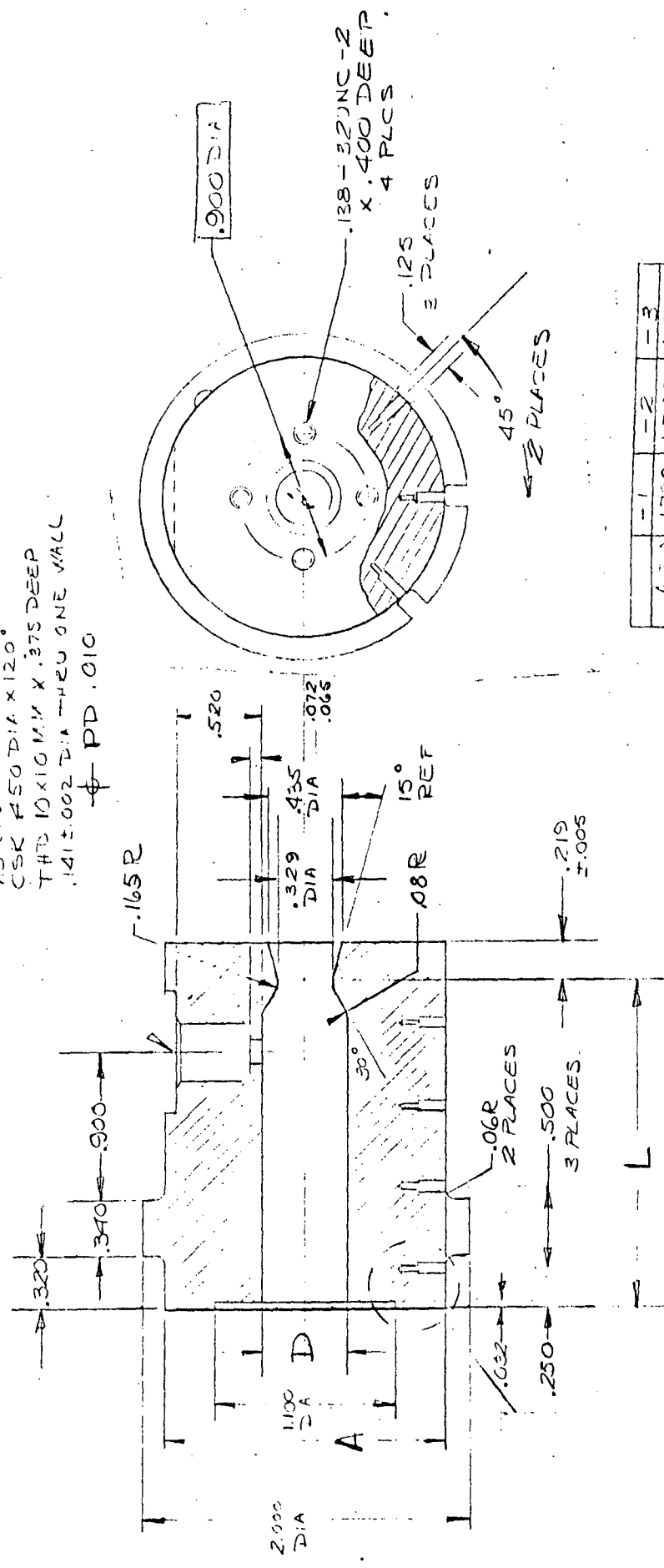
# SWIRL ELEMENT COMBUSTION



- (1) REGION OF HIGH MASS TRANSFER; COMBUSTION INITIATION.
- (2) REGION OF HIGH DIFFUSION RATES; PROBABLE COLLAPSE OF OXIDIZER HOLLOW CONE.
- (3) CONTINUED ROTATION OF OXIDIZER-RICH CORE PROMOTES RADIAL DIFFUSION.

# HOT FIRE CHAMBERS

SF .75 DIA TO DEPTH  
SHOWN  
TAP DRILL .355 DIA  
AS SHOWN  
CSK #50 DIA X 120°  
THE 10 X 10 MM X .375 DEEP  
.141 ± .002 DIA THRU ONE WALL  
Φ PD .010



	-1	-2	-3
A DIA	1.720	1.720	1.615
B	.27	.27	.27
D DIA	1.520	.520	.615
L	2.000	5.000	2.000